

SOFC materials characterization

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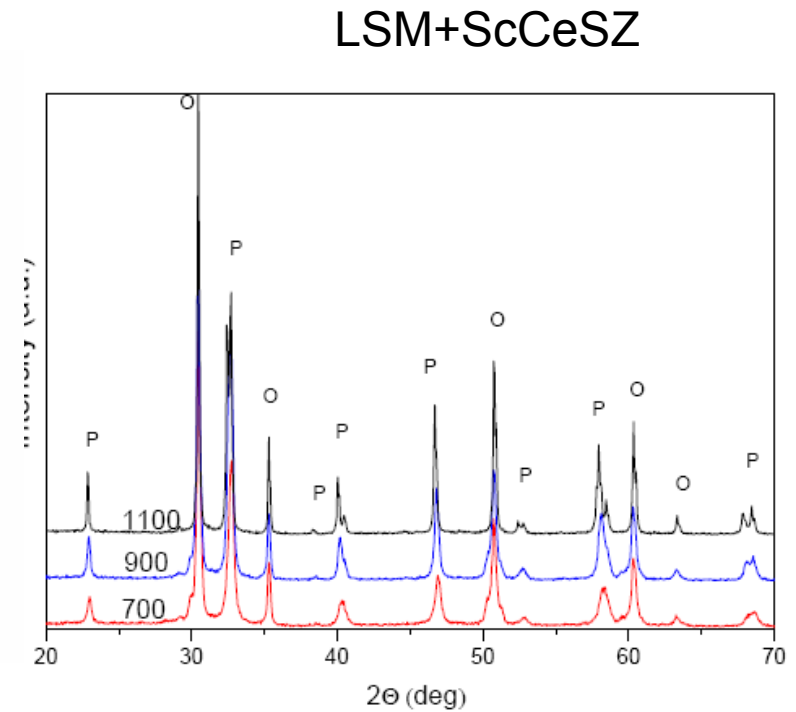
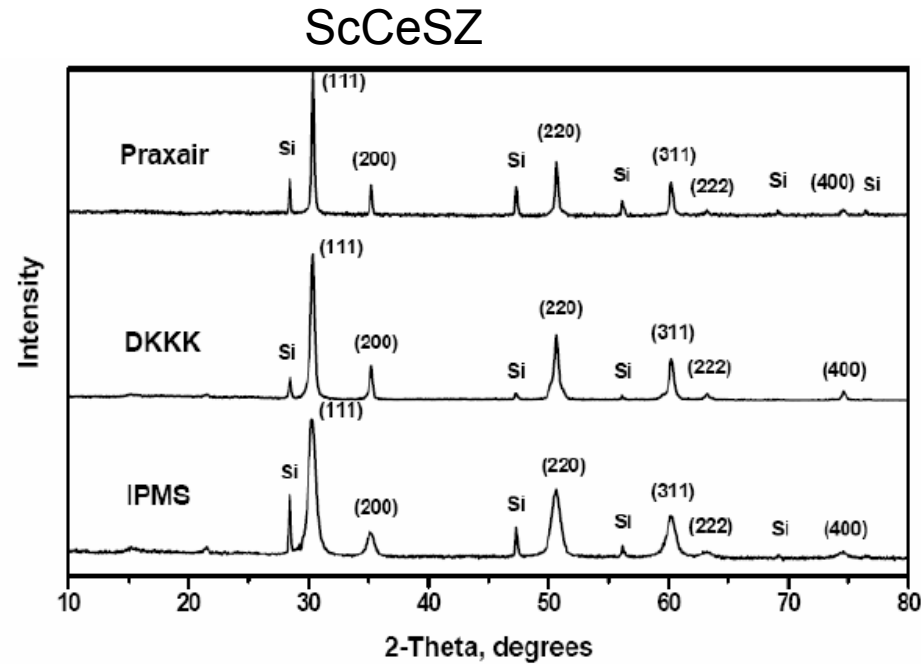
Basic characteristics determining performance of SOFC materials

- 1. Phase composition (XRD)
- 2. Real structure and microstructure (XRD, neutron diffraction, WAXS, TEM and SEM with EDX, EXAFS, FTIRS, Raman, MAS NMR, Mössbauer)
- 3. Texture (porosity, TPB length): Hg porosimetry, Ar adsorption isotherms, X-ray SAS, elemental mapping
- 4. Surface properties (composition, structure): XPS, SIMS
- 5. Transport characteristics (impedance)
- 6. Oxygen mobility, bonding strength and reactivity of surface sites (oxygen isotope exchange, TPD, microcalorimetry, weight and conductivity relaxation)

XRD

- Basic principle: diffraction of X-rays from certain planes of crystallites results in peak situated at some diffraction angle 2θ
- Peak Integral intensity determined by electronic density of planes (metal cations), broadening by crystal sizes in this direction and extended defects (stacking faults, twins, microstrains)
- Standard technique: commercial diffractometers, diffraction from a packed layer of polycrystalline samples, Cu K_{α} radiation, Scherrer equation etc.
- Sophisticated XRD technique: synchrotron radiation, much higher precision

Typical XRD diffraction patterns



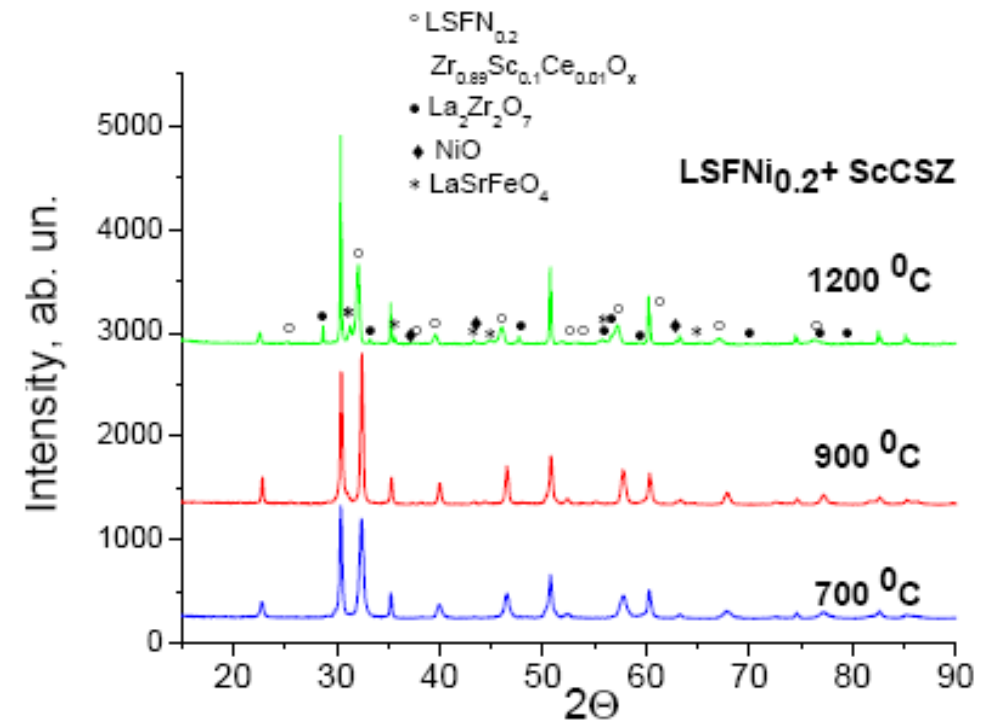
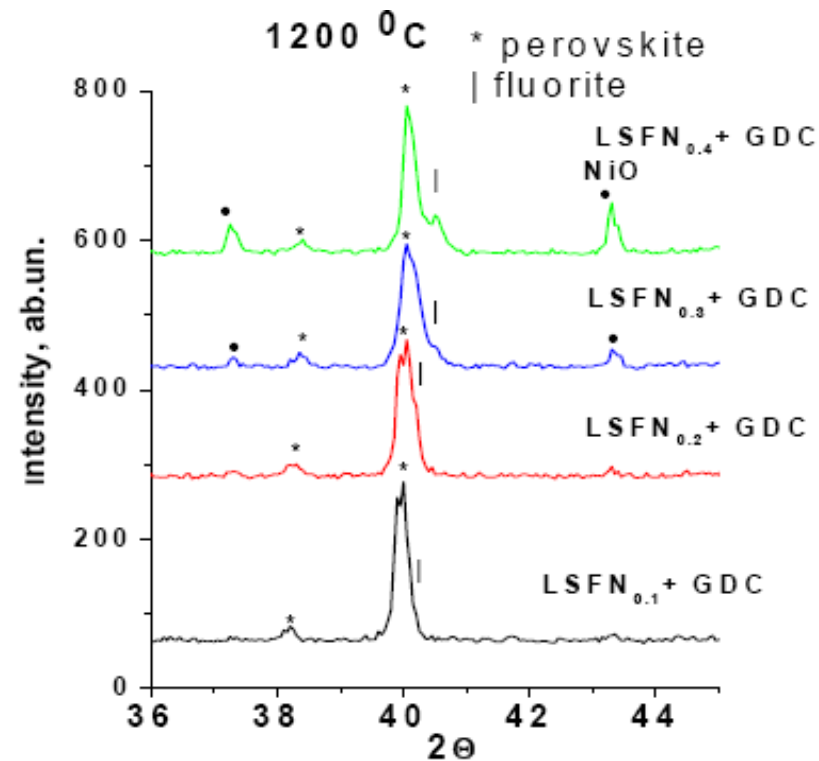
New phases are absent in LSM-ScCeSZ nanocomposites

LSM-ScCeSZ

Sintering T_c (°C)	Fluorite		Perovskite			
	D XRD, nm	Lattice parameter (Å)	D XRD, nm	Lattice parameter (Å)		
		a		a		c
700	12.6	5.0927	32.8	5.499		13.365
900	23.5	5.0965	48.0	5.513		13.378
1100	52.3	5.0990	70.5	5.526		13.381

Nanodomains. LSM and ScCeSZ parameters increase with sintering T due to La incorporation into F and Sc/Zr incorporation into B positions of P

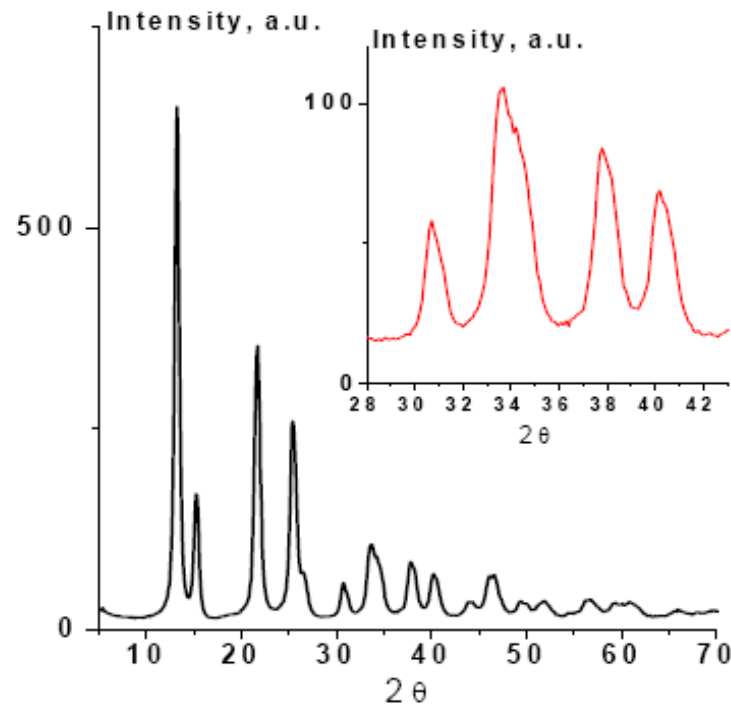
Detection of new phases during sintering



Segregation of NiO phase from LSFN –GDC nanocomposite

Formation of pyrochlore La₂Zr₂O₇ phase in LSFN-ScCeSZ nanocomposite

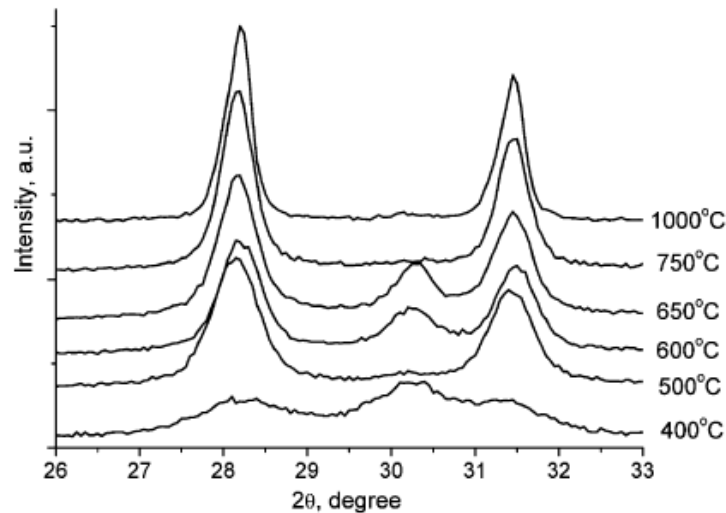
XRD on Synchrotron Radiation (SR)



XRD pattern of $\text{Ce}_{0.5}\text{Zr}_{0.5}\text{O}_2$ at $\lambda=0.703 \text{ \AA}$

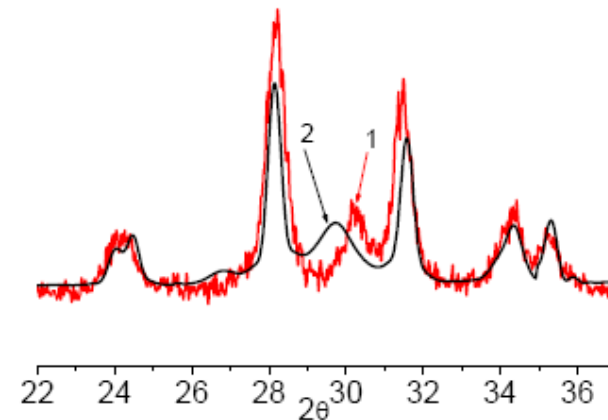
Strong asymmetry of diffraction peaks due to coexistence of domains enriched either by Ce or Zr cations

Modeling XRD patterns: ZrO_2 case



Experimental diffraction patterns of zirconia samples from Zr hydroxide calcined at different temperatures

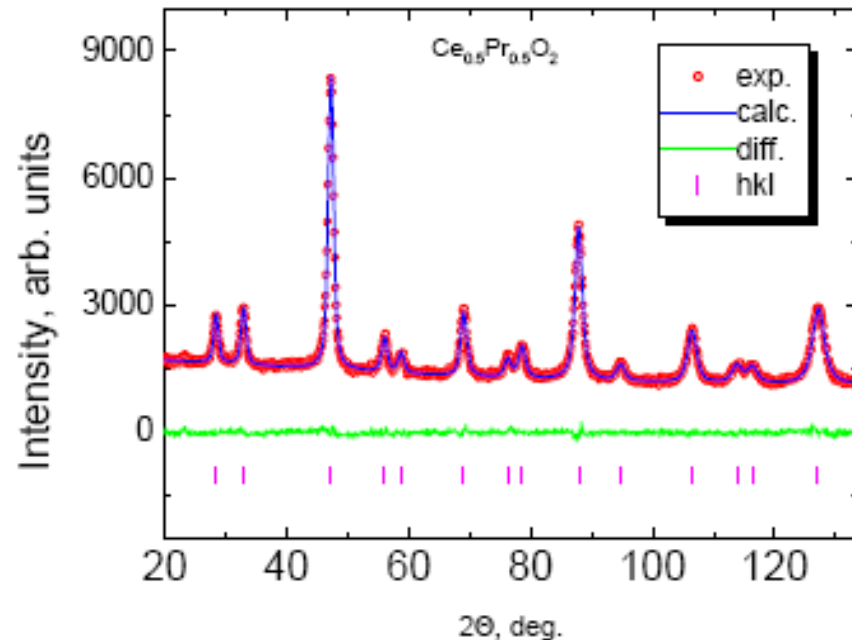
Experimental (1) and simulated diffraction pattern (2) for sample calcined at 650 °C



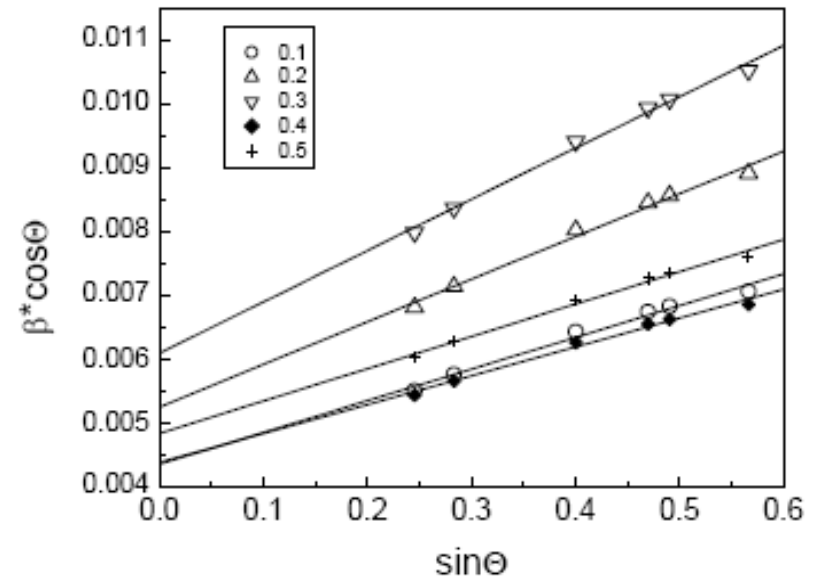
Modeling of the X-ray diffraction patterns for multiply twinned nanoparticles of monoclinic phase as revealed by TEM. The structure of the monoclinic phase can be considered as comprised of alternating layers of oxygen and zirconium layers situated along the (001) plane. In modeling, the crystallites were considered as formed by stacked alternating slabs with a mirror symmetric structure \Rightarrow appearance of fragments with a structure of c- ZrO_2 (peak at $2\theta \sim 30.2^\circ$)

Neutron Powder Diffraction (NPD): $\text{Ce}_{1-x}\text{Pr}_x\text{O}_{2-\delta}$

Typical diffraction pattern and its fitting



Angle dependence of peaks HW



NPD is sensitive to oxygen anions, so allows to estimate disordering of anion sublattice

Angle dependence analysis allows to estimate separately domain sizes and microstrains density

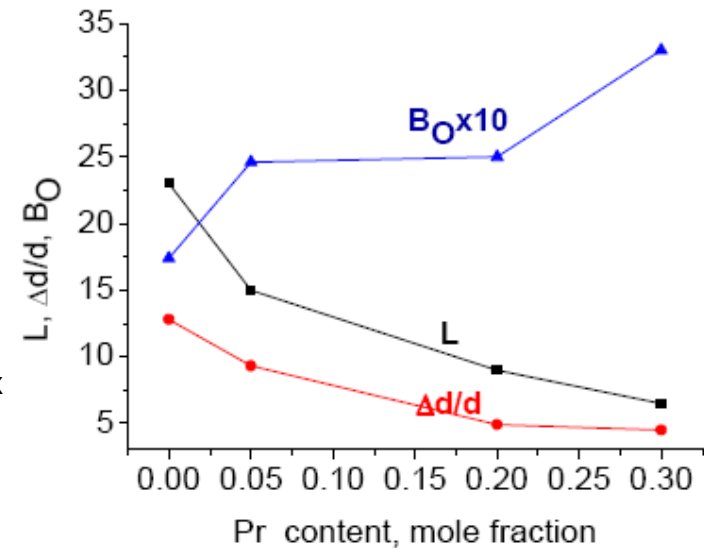
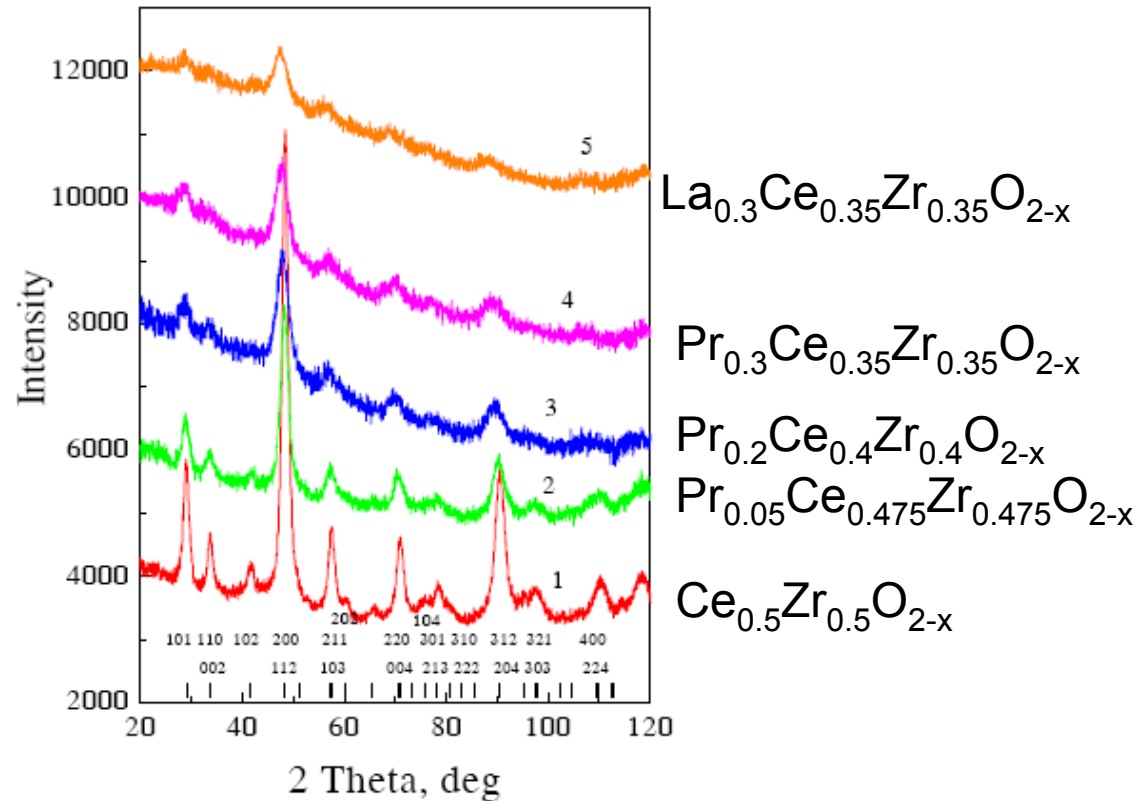
NPD: detailed characteristics of real structure

Табл.1. Structural parameters, interatomic distances, microstrain density, particle size and intensity of diffuse scattering for $\text{Ce}_{1-x}\text{Pr}_x\text{O}_2$ samples*

Pr content, x	0	0.1	0.2	0.3	0.4	0.5
a , Å	5.4108(2)	5.4159(7)	5.4199(8)	5.421(1)	5.4128(6)	5.4120(7)
B , Å ⁻² Ce/Pr O	0.04(4) 0.12(4)	0.11(5) 0.41(4)	0.21(5) 0.48(4)	0.34(6) 0.57(5)	0.23(5) 0.48(4)	0.29(5) 0.60(4)
$L(\text{Ce-O})$, Å (O-O) , Å	2.3430(1) 2.7054(1)	2.3451(2) 2.7079(4)	2.3469(2) 2.7099(4)	2.3472(3) 2.7104(5)	2.3438(2) 2.7064(3)	2.3435(2) 2.7060(4)
χ^2	2.33	1.54	1.54	1.28	1.62	1.52
R_p	3.26	2.24	1.83	1.74	2.46	2.35
R_{wp}	4.21	2.86	2.34	2.20	3.14	2.99
R_{Br}	1.71	2.20	2.71	2.26	2.58	1.68
R_f	1.02	1.43	1.77	1.50	1.64	1.03
Microstrains		0.00497	0.00668	0.00804	0.00452	0.00506
Particle size, nm		35	30	25	35	32
Intensity of diffuse scattering, rel. un	850	1650	2540	2410	1350	1370

* Space group Fm3m.. B - isotropic temperature parameter for the atom. R_p , R_{wp} , R_b and R_f - the conventional factors which show the quality of the agreement between observed and calculated data.

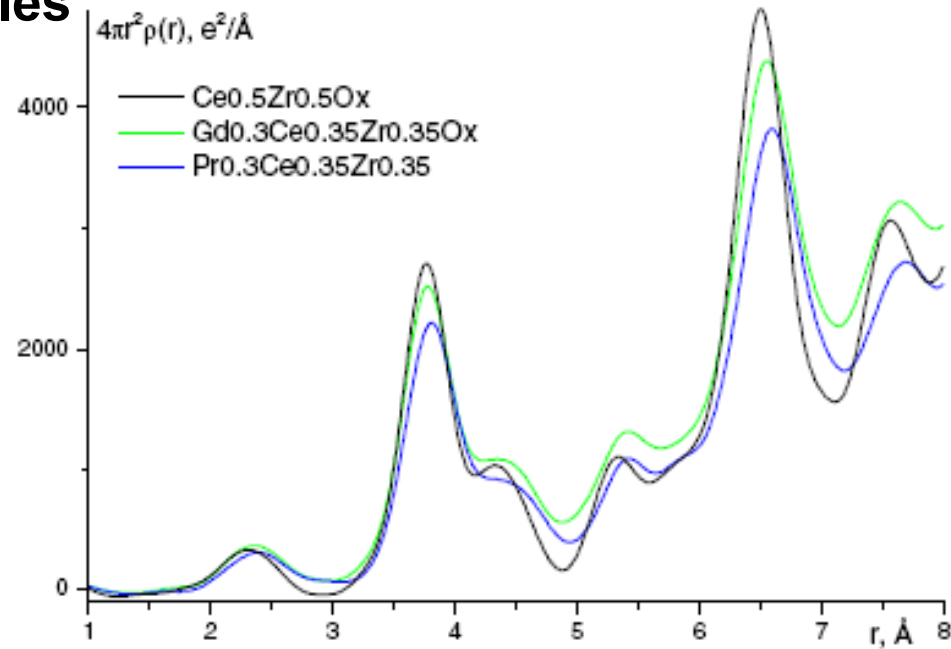
NPD for $\text{Ln}_x(\text{Ce}_{0.5}\text{Zr}_{0.5})_{1-x}\text{O}_{2-\delta}$



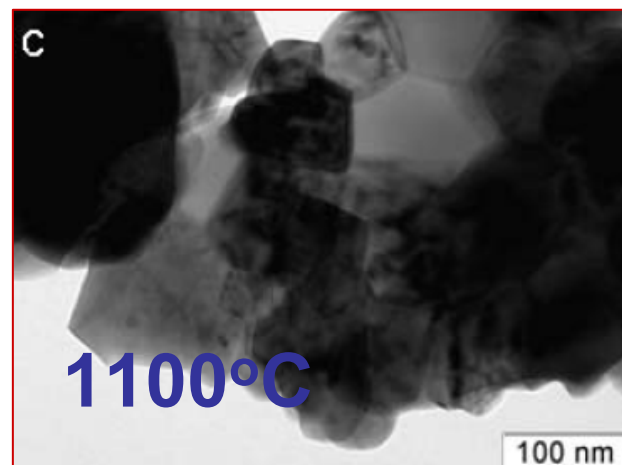
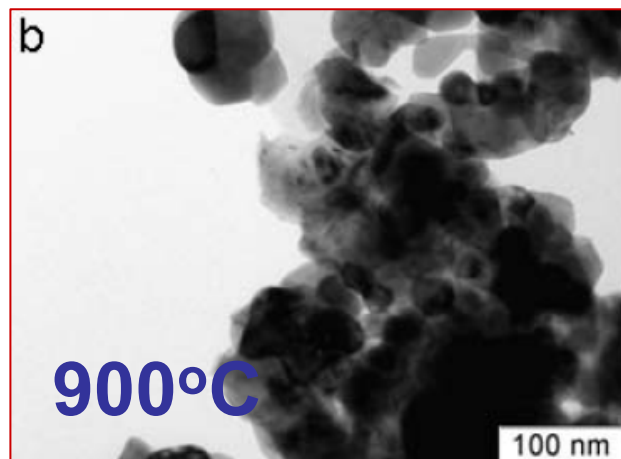
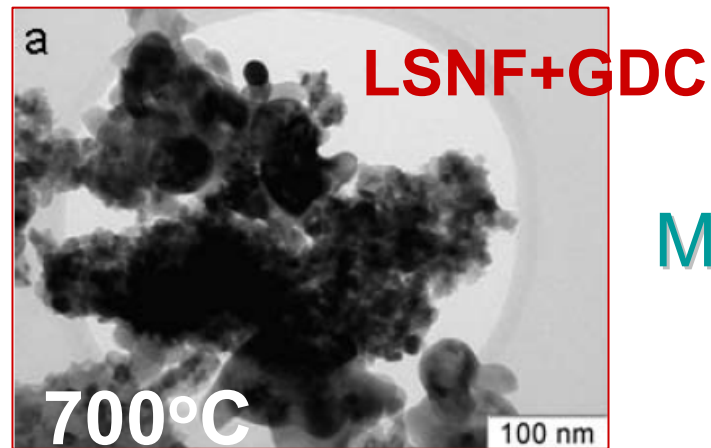
Disordering of oxygen sublattice is reflected in thermal parameter B_O
 Peaks broadening is determined by decreasing domain sizes L with Pr content
 Microstrains density $\Delta d/d$ decreases with doping due to more uniform distribution of Ce and Zr between neighboring domains

WAXS

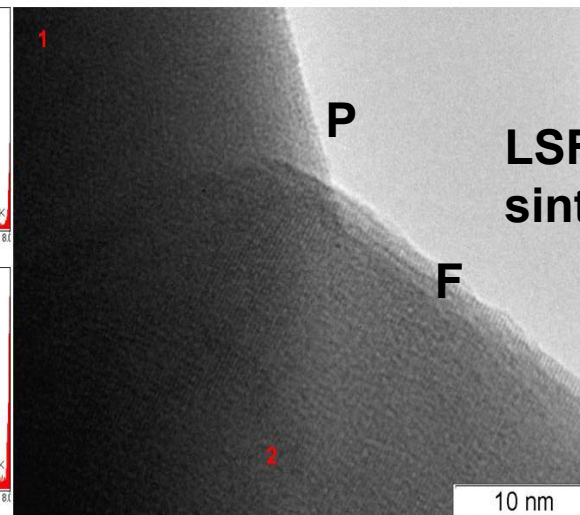
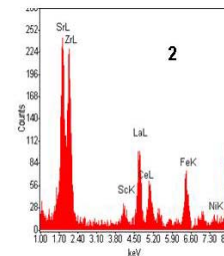
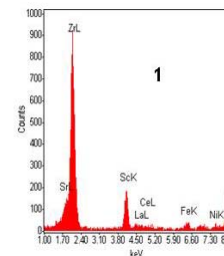
Radial distribution function curves for ceria-zirconia samples



Peak position determined by distances in the cell, area –by coordination numbers



Microstructure of cathode materials by Transmission Electron Microscopy (TEM)

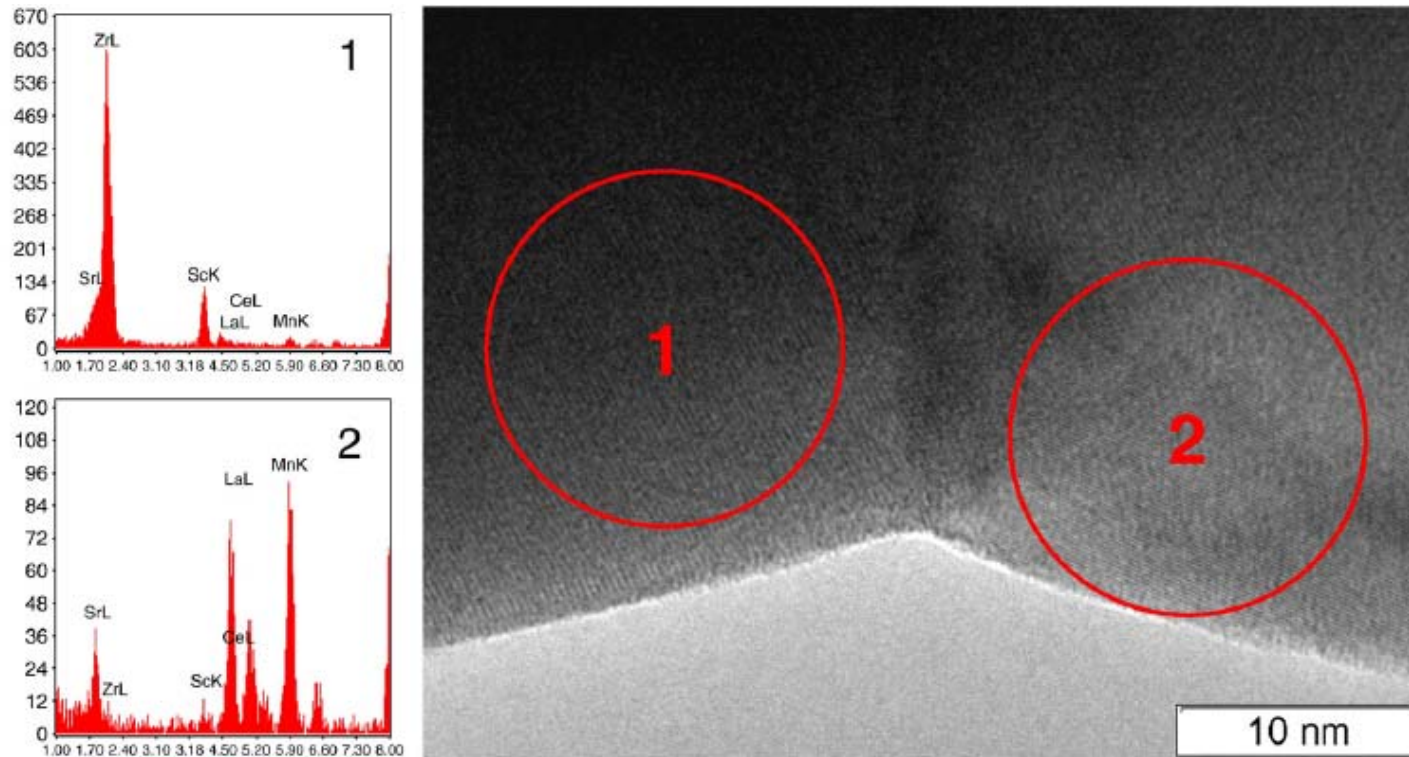


**LSF_{Ni0.2}-ScCeSZ
sintered at 1200 °C**

**Coherent
P-F domains
stacking**

**Uniformly intermixed particles of both phases,
A lot of P-electrolyte interfaces
Annealing pores with $T_{\text{sint.}}$, more interfaces**

TEM with EDX-local elemental analysis



EDX spectra of neighboring fluorite (1) and perovskite (2) domains in LSM–ScCeSZ composite sintered at 1100 °C.

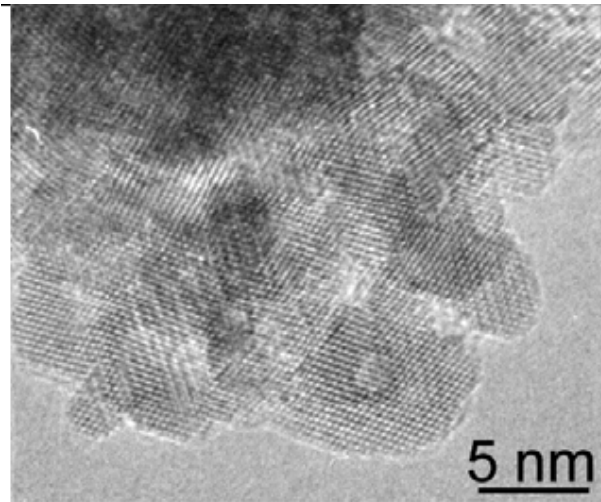
Observed lattice spacing: 2.55 Å—(200) planes of $\text{Sc}_{0.2}\text{Ce}_{0.01}\text{Zr}_{0.79}\text{O}_{2-\delta}$ (1) and 1.58 Å—(132) planes of $\text{La}_{0.8}\text{Sr}_{0.2}\text{MnO}_3$ (2).

Domain composition : $\text{La}_{0.07}\text{Sr}_{0.07}\text{Sc}_{0.16}\text{Ce}_{0.006}\text{Mn}_{0.04}\text{Zr}_{0.73}\text{O}_{2-\delta}$ (1) and $\text{La}_{0.73}\text{Sr}_{0.16}\text{Sc}_{0.02}\text{Zr}_{0.014}\text{MnO}_{3+\delta}$ (2).

Redistribution of elements between domains of perovskite and electrolyte

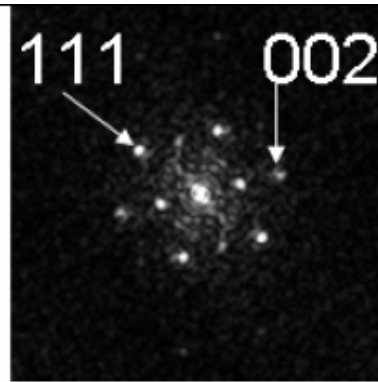
TEM to assess surface planes in nanoparticles:

ZrO₂ case

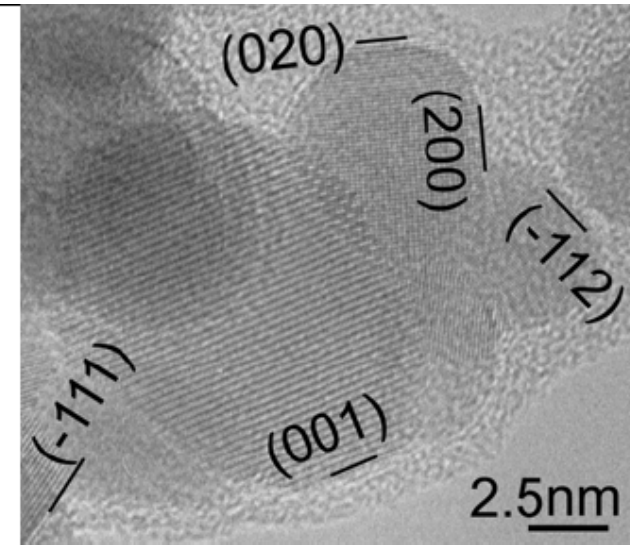


a

Aggregates of oriented m-ZrO₂ nanoparticles (a) and corresponding digital diffraction pattern (DDP) with reflections shown by arrows

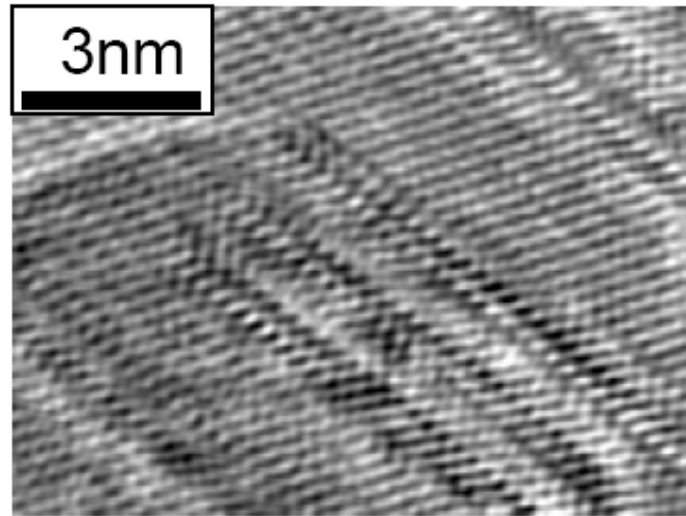


b

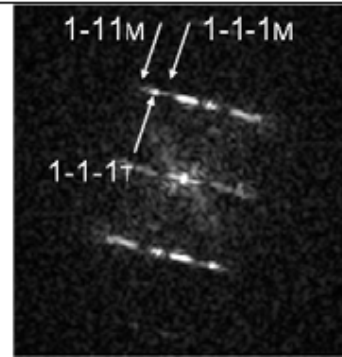


Rounded particles of m- ZrO₂ in sample calcined at 500 °C; the types of surface faces are indicated.

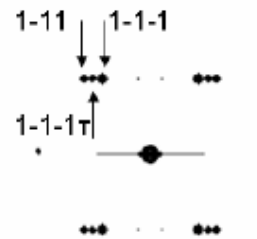
TEM to detect extended defects: ZrO_2 case



a

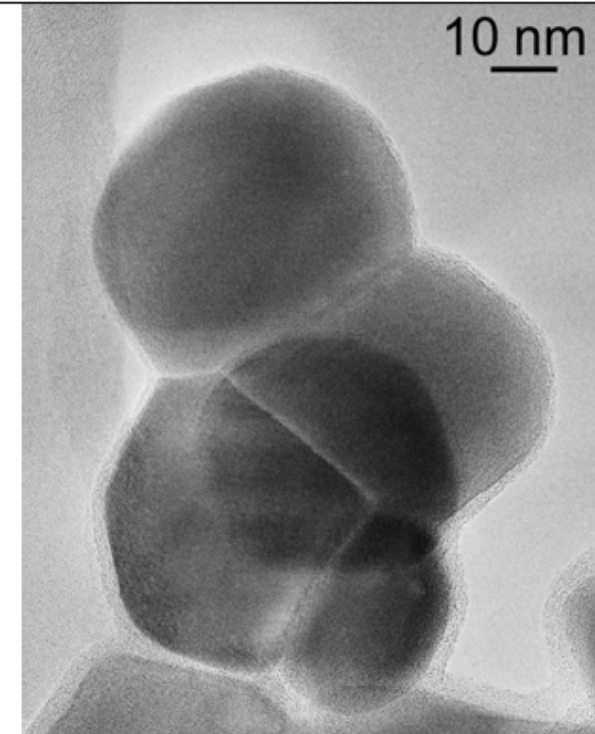


b



c

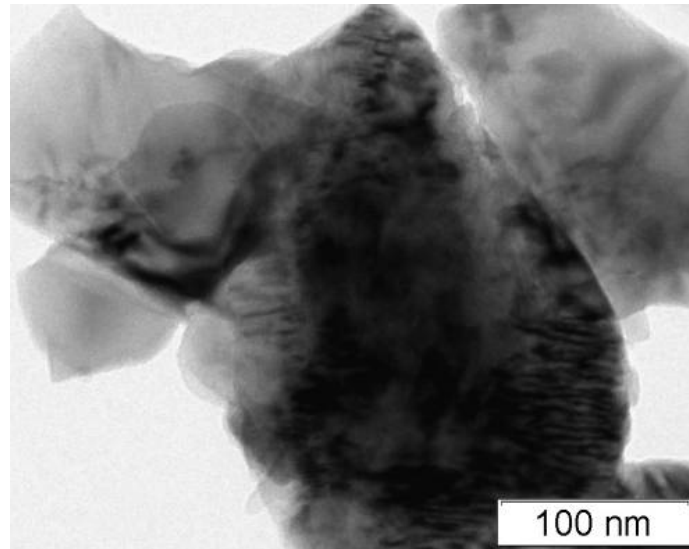
HRTEM image of the multiply twinned particle with a small (~ 1 nm) distance between twinning planes (a); DDP from this region in $[110]$ projection (b) and its modeling for the mixture of m- and t-phases (c).



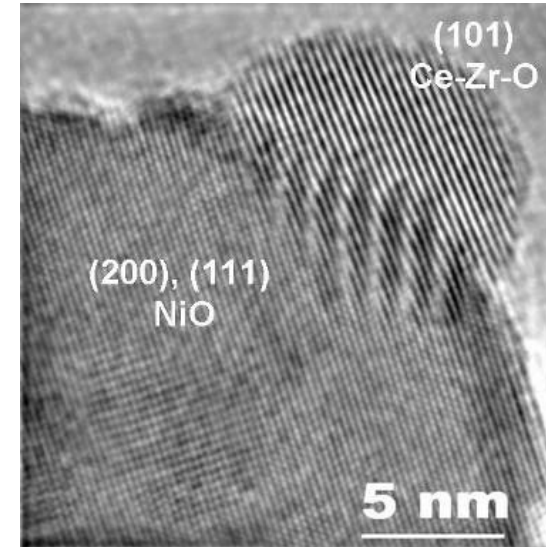
TEM image of the particle of 1000 °C sample with separate twins visible.

Microstructure by TEM: promoted anode materials

Perovskite LaPrMnCrO layers on NiO



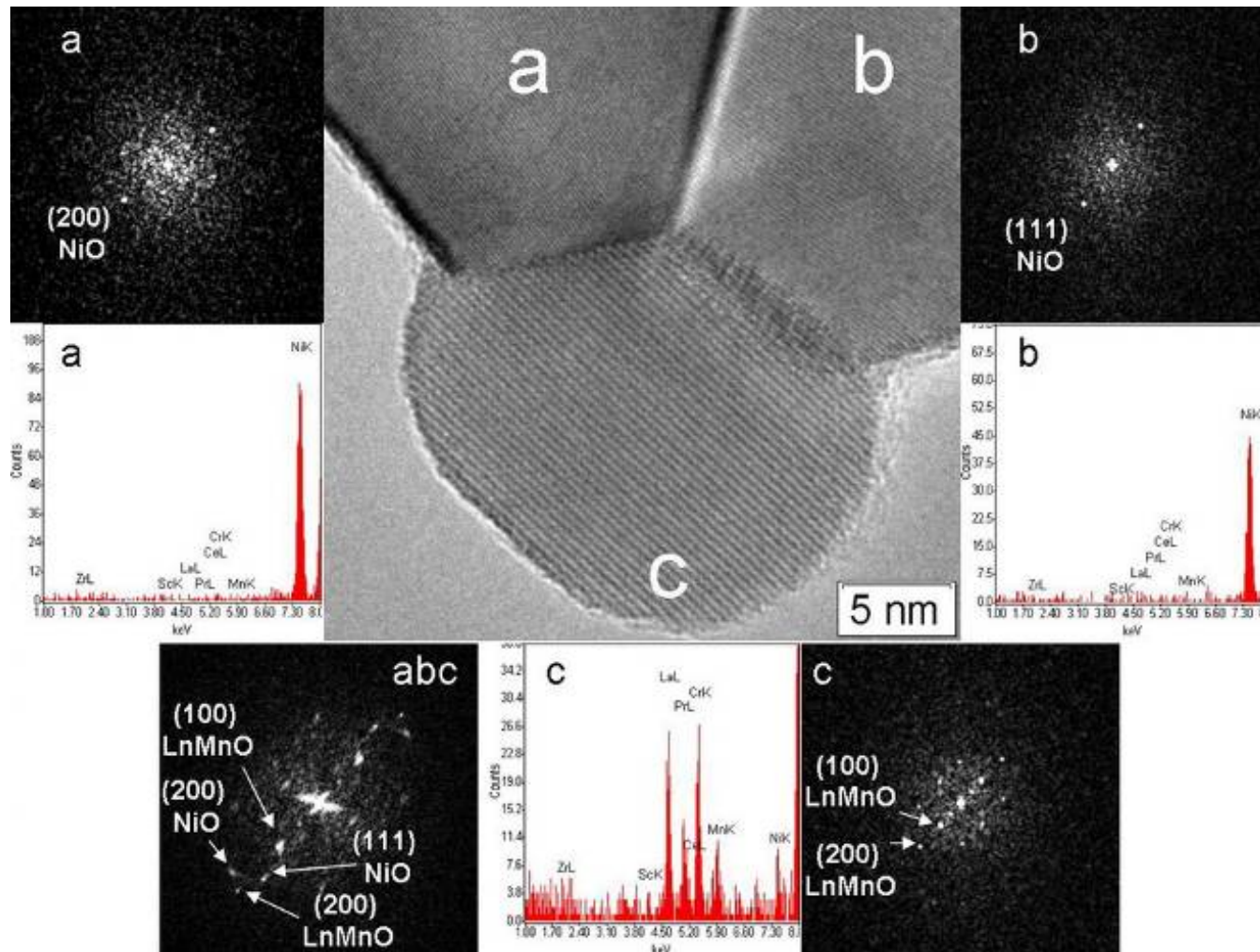
Fluorite layers on NiO



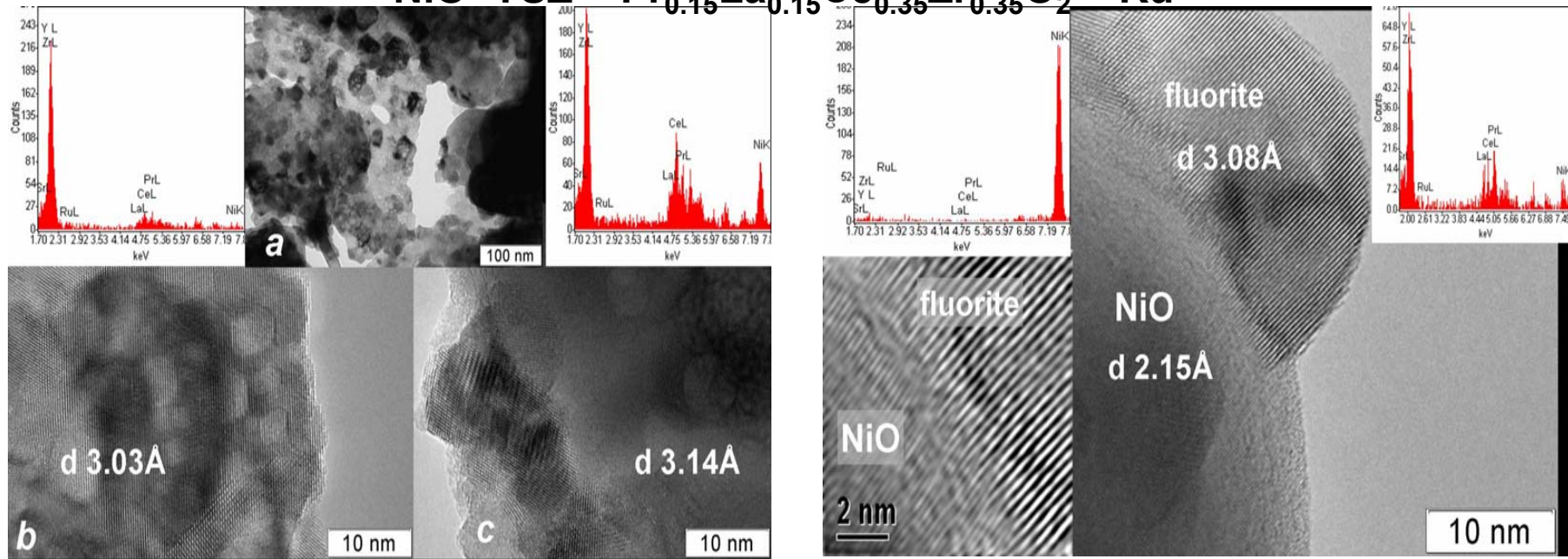
Good decoration and epitaxy required to prevent coking in CH_4 steam reforming

Microstructure by TEM: doped anode materials

Coherently stacked perovskite LnMnCrO and NiO domains



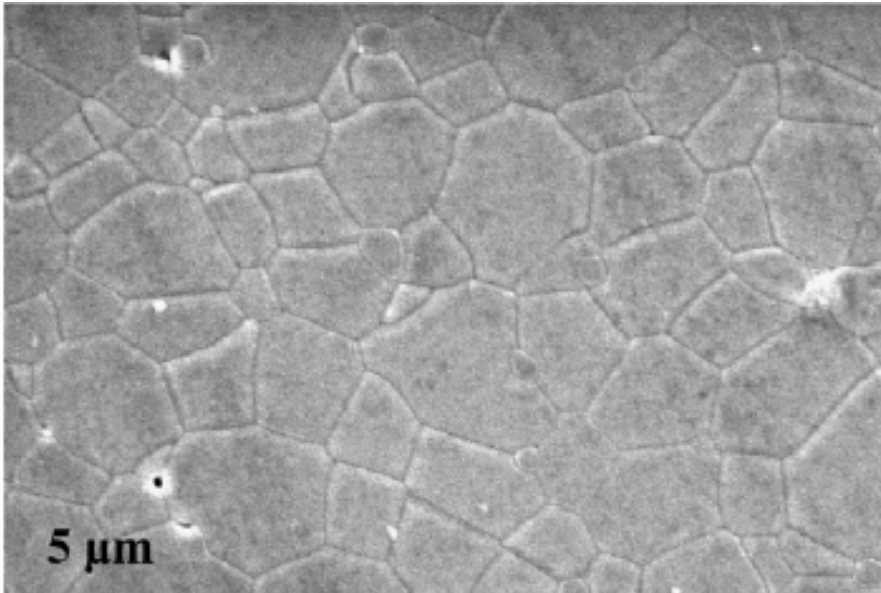
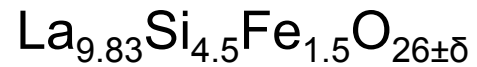
Microstructure by TEM:doped anode materials



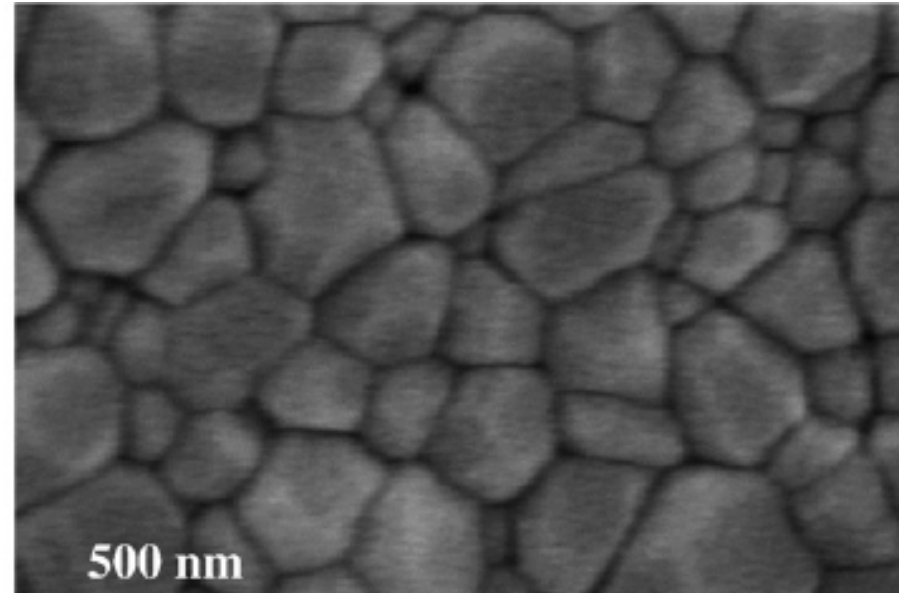
a- macro/mesoporous aggregates of particles;
 b-disordered nanodomain ZrO_2 particle containing internal nanopores and respective EDX spectrum;
 c –disordered nanodomain particles of fluorite-like oxide promoter on the surface of NiO particle and respective EDX spectrum;
 d-contact area between NiO and YSZ particle modified by the elements of complex oxide promoter.

⇒ strong interaction between all phases of anode composite material with redistribution of components between phases

SEM: density and crystallinity of electrolyte layers



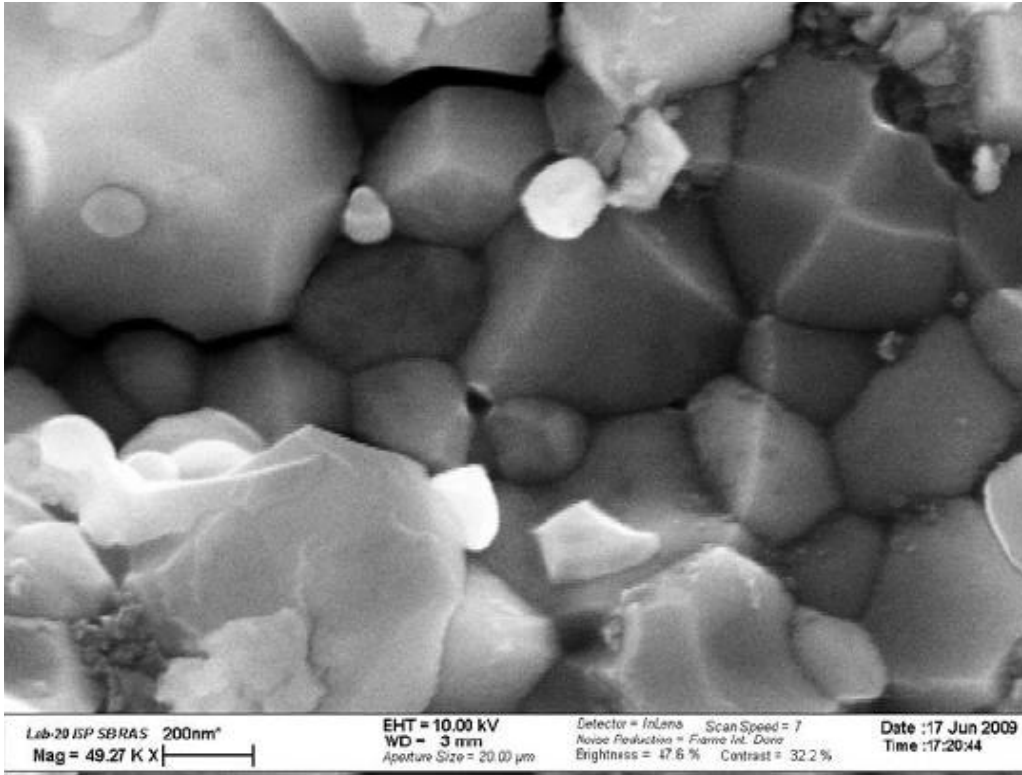
Conventional sintering 1500 °C



Spark-plasma sintering 1100 °C.

Much smaller domain sizes in ceramics sintered by advanced techniques

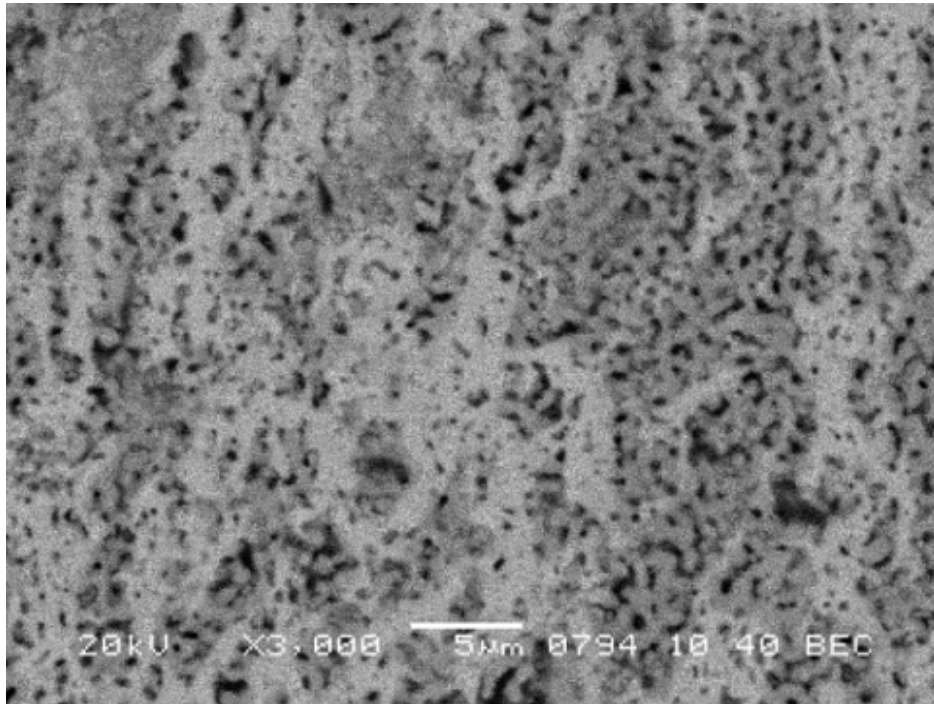
SEM: cathode nanocomposites



SEM image of the cleaved surface of LSFN-GDC pellet sintered at 1200 °C.

Surprising crystallographic ordering of interfaces, each detected particle is comprised of smaller P+F domains, could favor fast oxygen diffusion

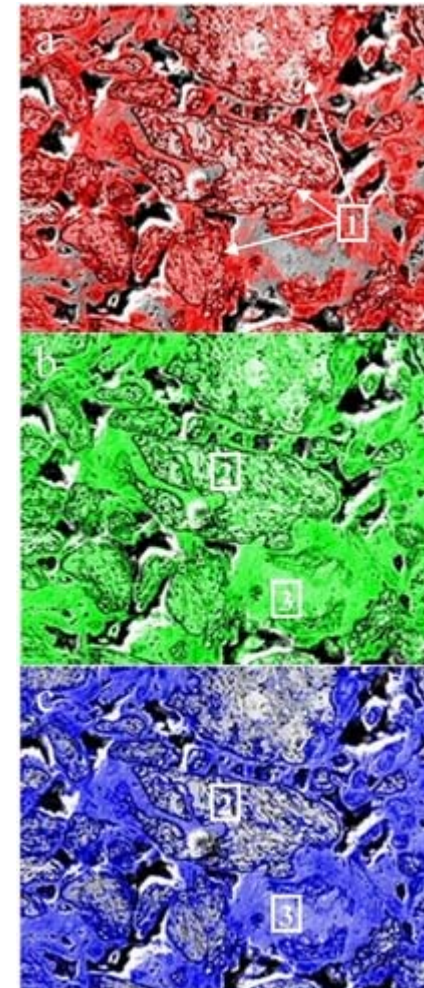
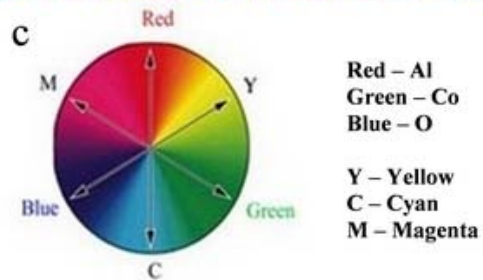
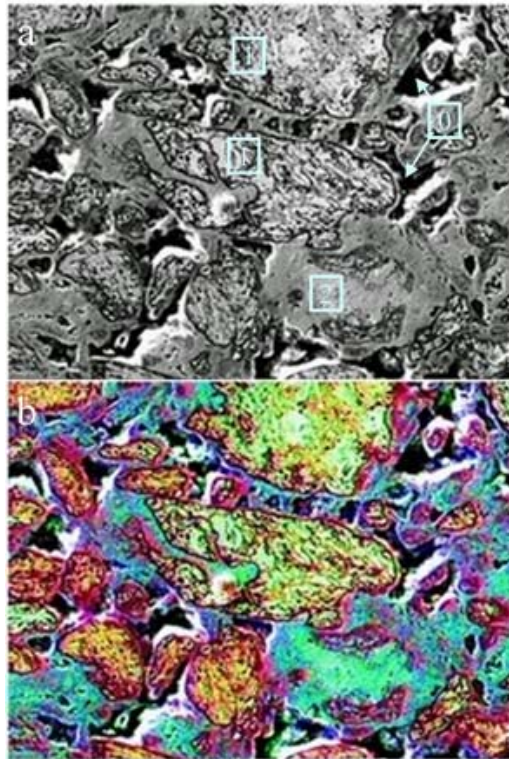
SEM in scattered electrons



$\text{LaFe}_{0.7}\text{Ni}_{0.3}\text{O}_3$ (50%) – $\text{Ce}_{0.9}\text{Gd}_{0.1}\text{O}_2$ (50%)

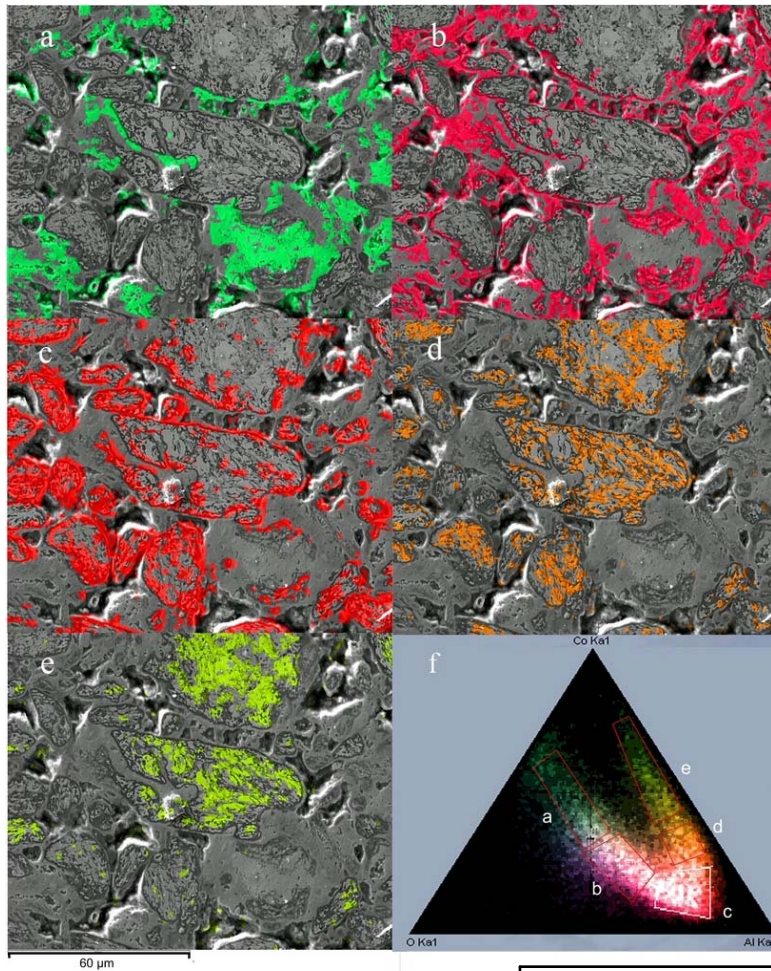
Control of uniformity of spatial distribution and percolation of ionic or electronic-conducting phases

SEM: elements spatial distribution in nanocomposites



Element distribution maps of Al (a), Co (b), O (c) from cermet surface superimposed on SEM micrograph; 1 – alumina shell which encapsulates the metallic core; 2 – oxygen-free cores; 3 – high oxygen concentration matrix.

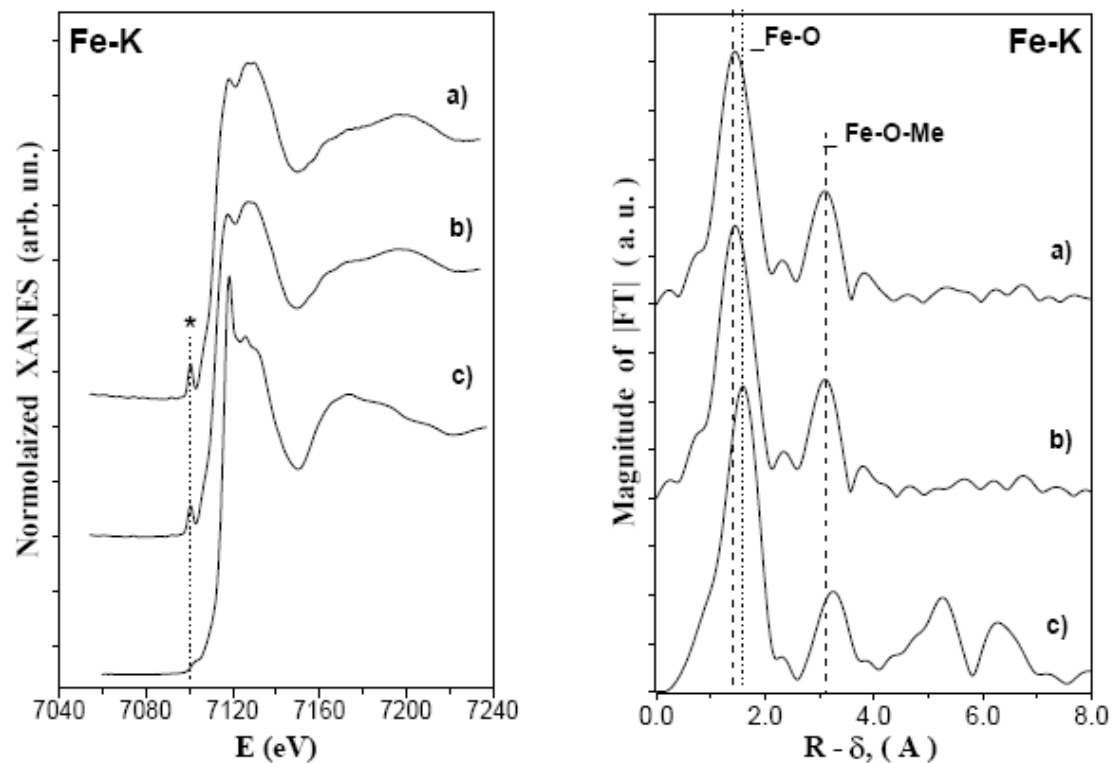
SEM: identification of surface phases by superposition of elemental maps



Composition of different fragments

Fragments in Fig. 12	O, at. %	Al, at. %	Co, at. %
a (emerald)	45.1	9.3	45.5
b (scarlet)	52.7	23.5	23.8
c (red)	42.2	39.8	18.1
d (orange)	20.1	36.7	43.2
e (green)	11.5	24.8	63.7

EXAFS: analysis of fine structure of X-ray absorption edges caused by scattering of emitted electrons

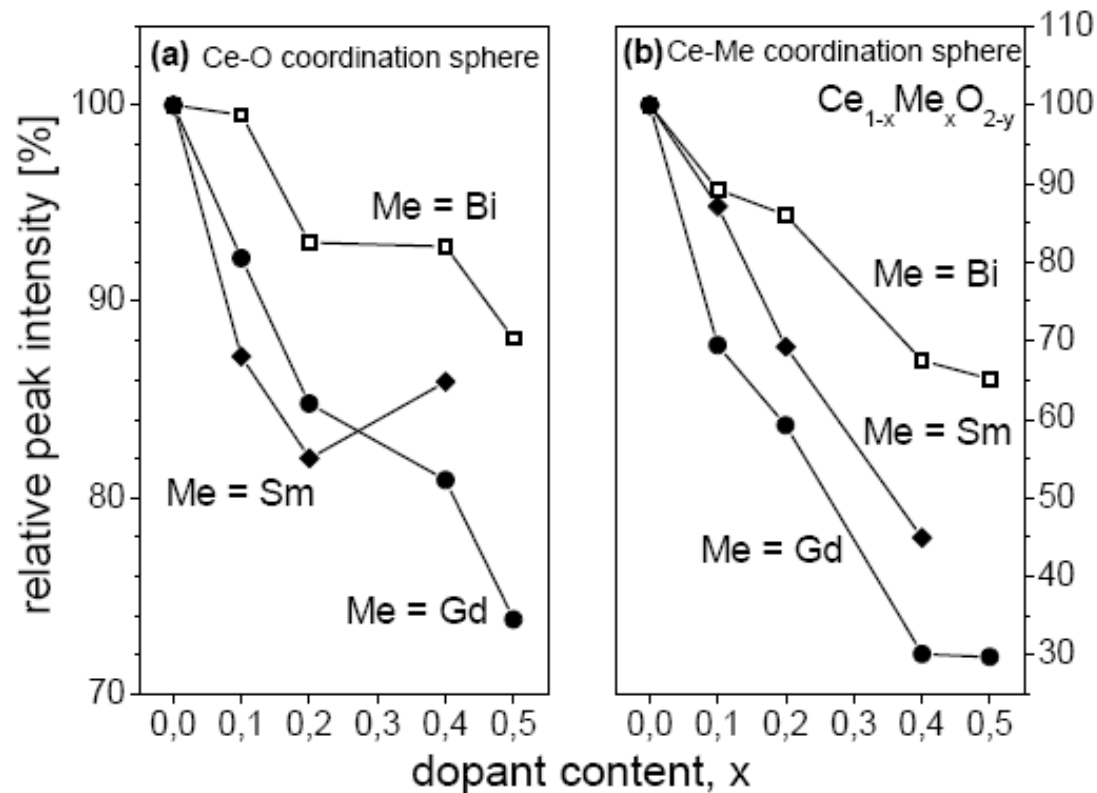


Allows to estimate distances and coordination numbers in different lattice positions

XANES spectra (Fe-K edge)(left) and radial distribution function curves (right) describing Fe local arrangement for samples: a - $\text{La}_{10}\text{Si}_4\text{Fe}_2\text{O}_{26}$, b - $\text{La}_{9.83}\text{Si}_{4.5}\text{Fe}_{1.5}\text{O}_{26}$, c - LaFeO_3 .

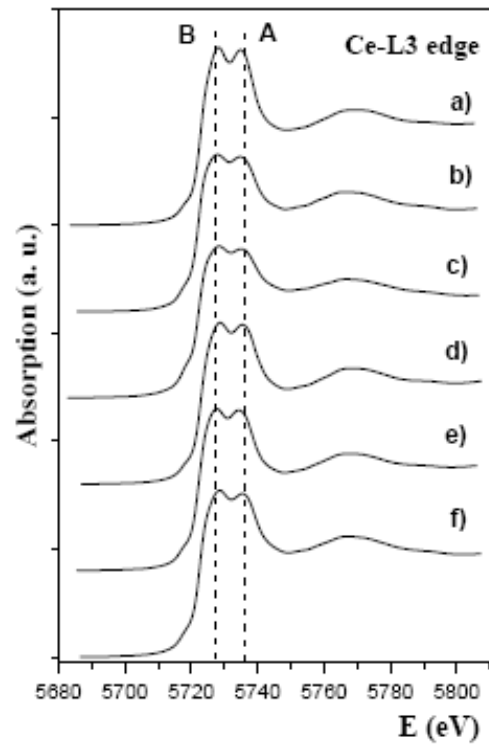
Tetrahedral coordination of Fe^{3+} cations in La silicates and octahedral in perovskite

EXAFS: effect of ceria doping on local structure

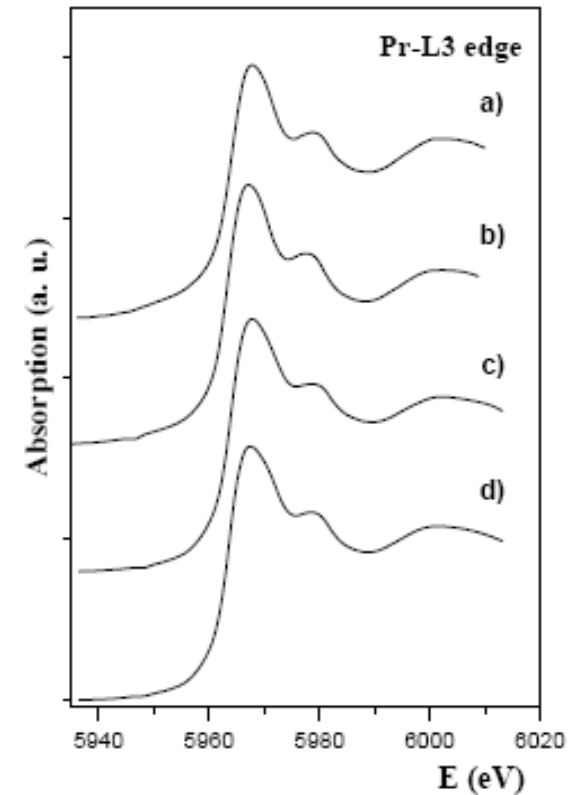


Decline Ce-O CN with doping level \Rightarrow rearrangement of coordination polyhedra,
not simple generation of randomly distributed anion vacancies

XANES: charge state



Pr content 0, 10, 20, 30, 40 and 50 at. %

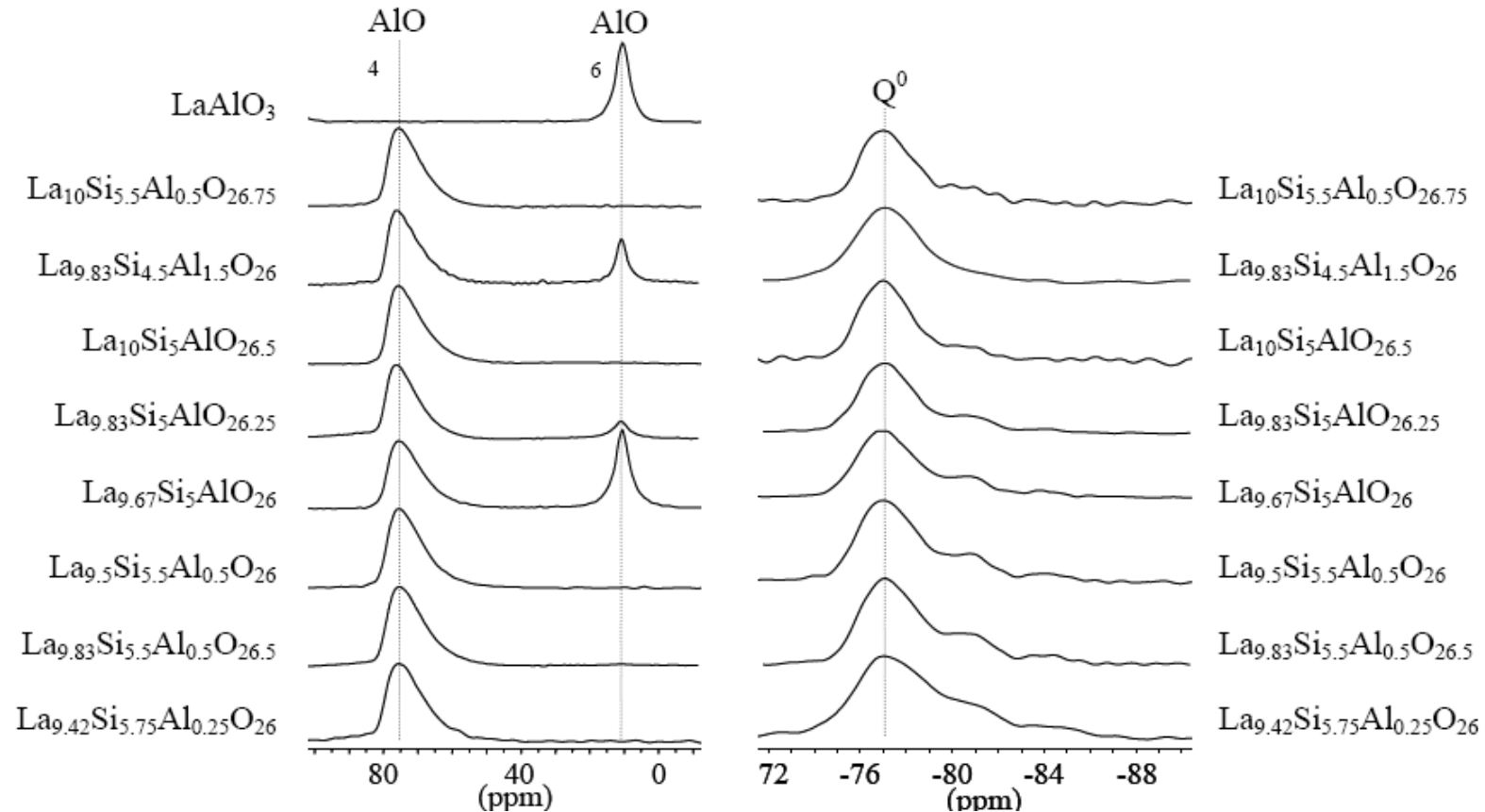


Pr content 20, 30, 40 and 50 at. %

Ce in 4+ state, Pr in both 3+ and 4+ state

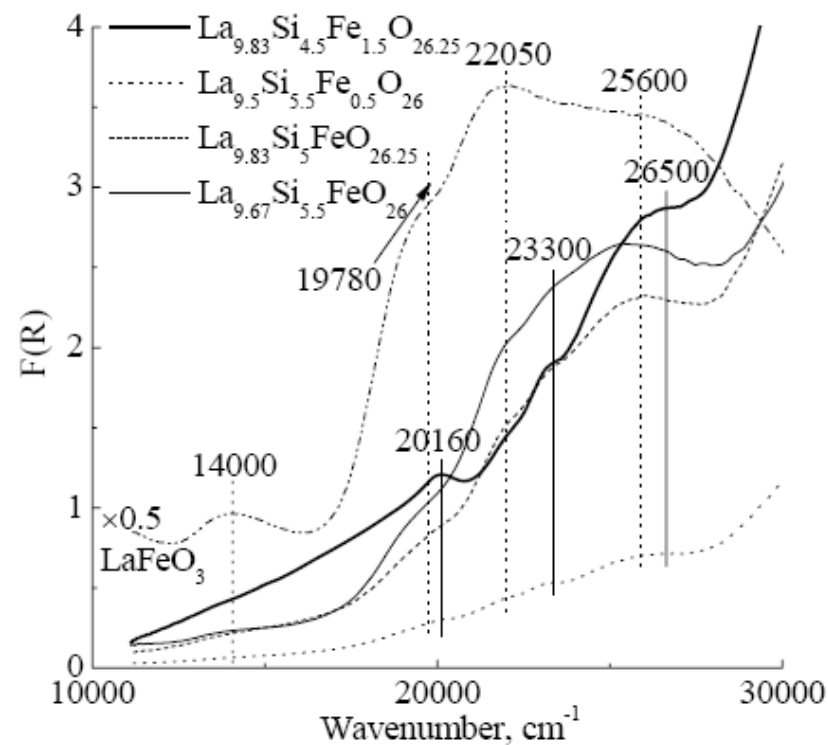
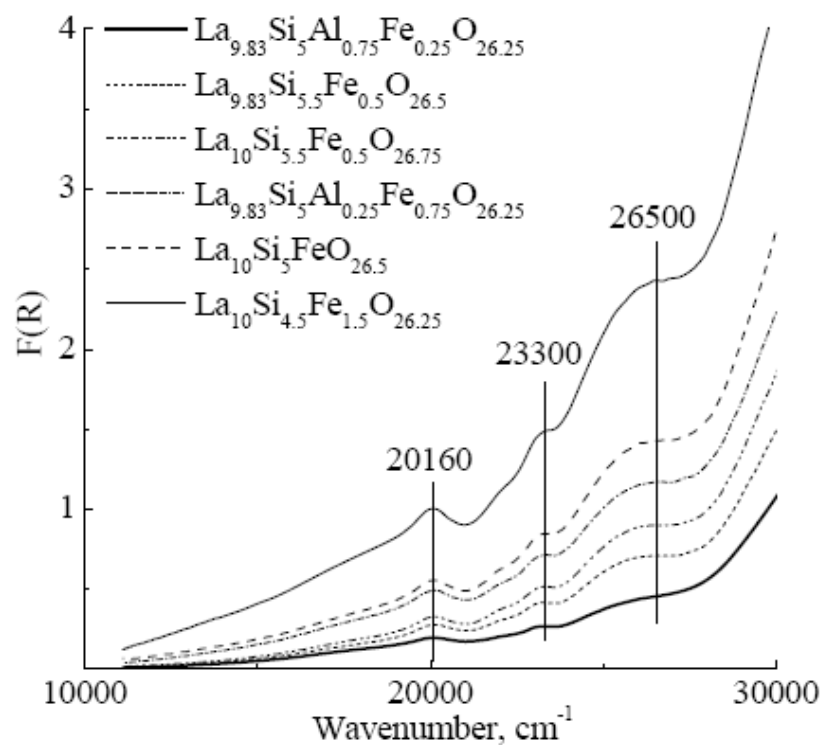
Nuclear Magnetic Resonance (NMR)

^{27}Al (left) and ^{29}Si (right) MAS NMR spectra of Al-doped systems



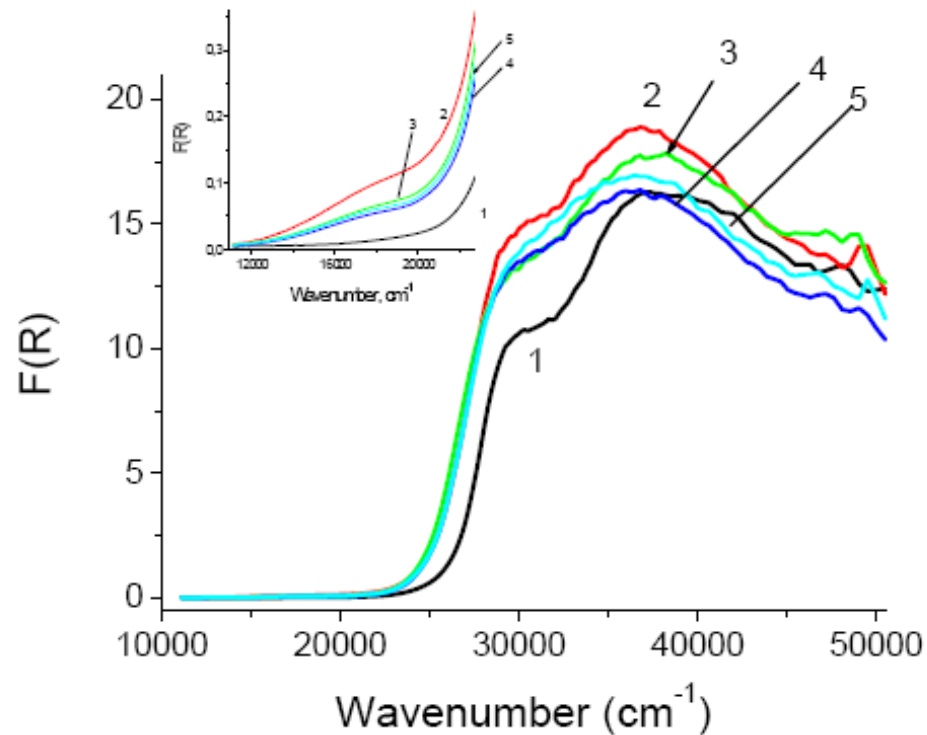
Band position depends on oxygen coordination sphere. Al in substitution position in apatite structure – in Td, in LaAlO_3 admixture - in Oh
 Along with ideal isolated SiO_4 units (Q^0), condensed Si-O-Si groups are revealed by bands at more negative chemical shifts

UV-Vis: charge state and coordination of cations (d-d transitions), Me-O strength (charge transfer bands)



$\text{Fe}^{3+}_{\text{Td}}$ in substitution positions of apatites + admixture of LaFeO_3

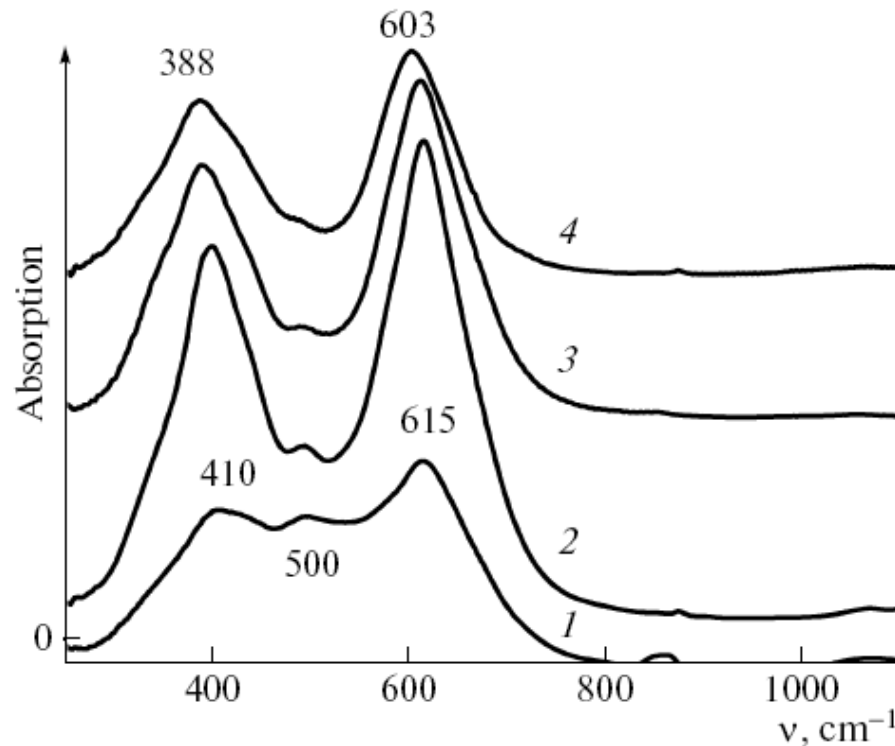
UV-Vis for doped ceria



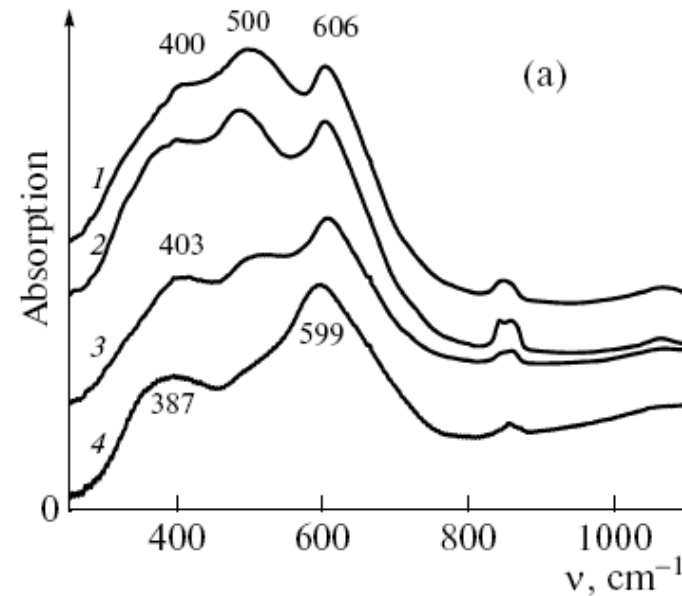
UV-Vis spectra of CeO_2 (1) and $\text{Ce}_{1-x}\text{Sm}_x\text{O}_{2-\delta}$ at $x=0.05$ (2), 0.1 (3), 0.15 (4) and 0.2 (5)

Shift of CTB to lower wave numbers with doping suggests deformation of coordination polyhedra leading to appearance longer Me-O distances

FTIRS of lattice modes: perovskites



IR spectra of (1) $\text{LaMnO}_{3.40}$, (2) $\text{LaMnO}_{3.24}$, and (3) $\text{LaMnO}_{3.19}$, and (4) after removal of a 0.5 monolayer of oxygen by thermodesorption in a helium flow at 650°C.

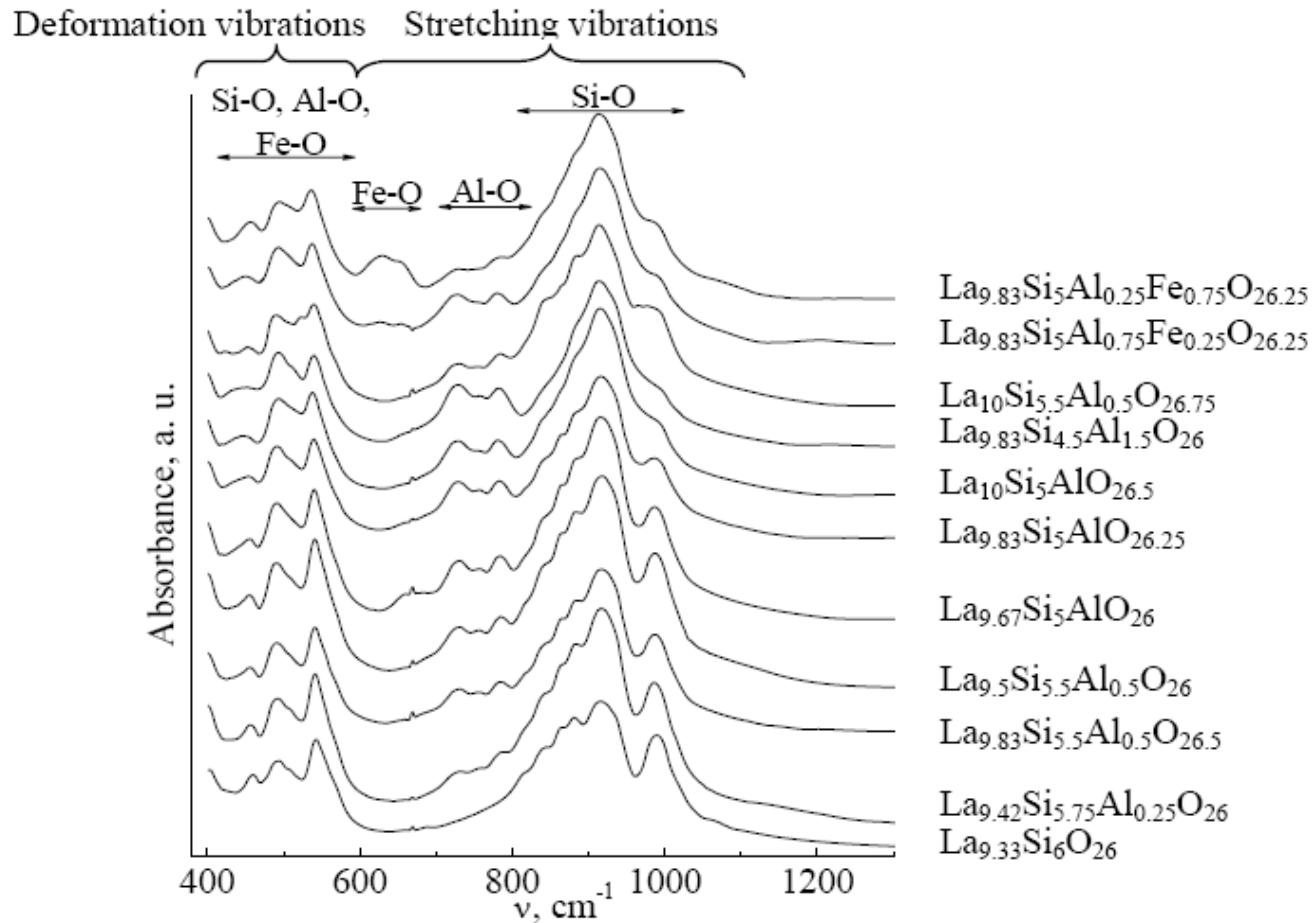


(1) LaCeMn , (2) LaFeMn , (3) LaBiMn , and (4) LaSrBiMn calcined at 500 C

Number of bands is determined by the local symmetry of the lattice.

Strong distortion in low-temperature manganites due to cation vacancies: band at $\sim 500 \text{ cm}^{-1}$

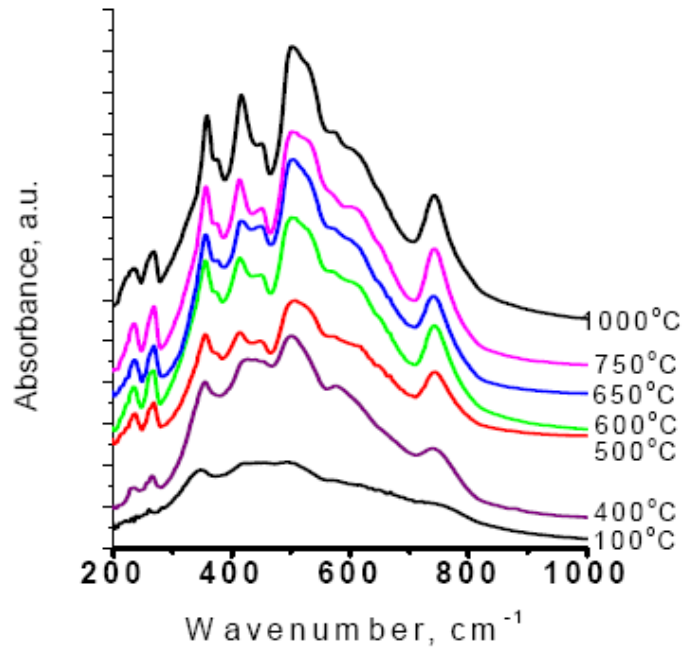
FTIRS of lattice modes: apatites



Splitting of Si-O stretching vibrations due to condensation of SiO_4 groups

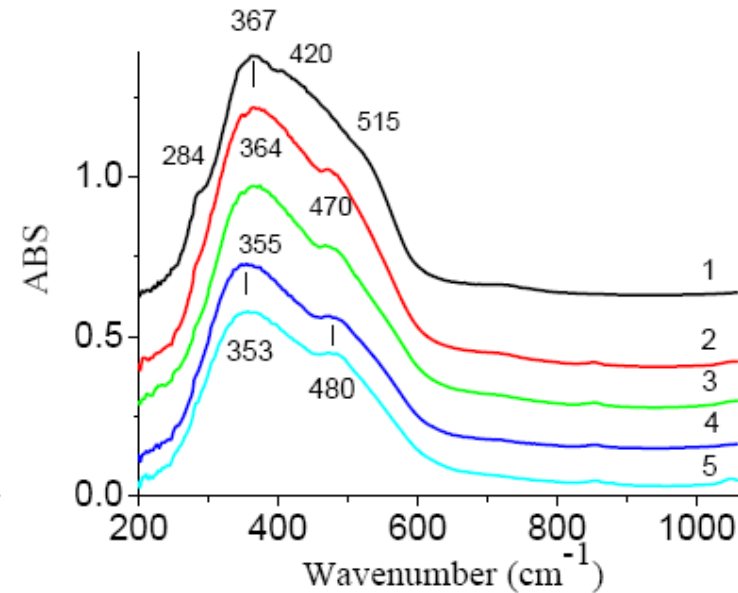
FTIRS of lattice modes

ZrO₂ from hydroxide



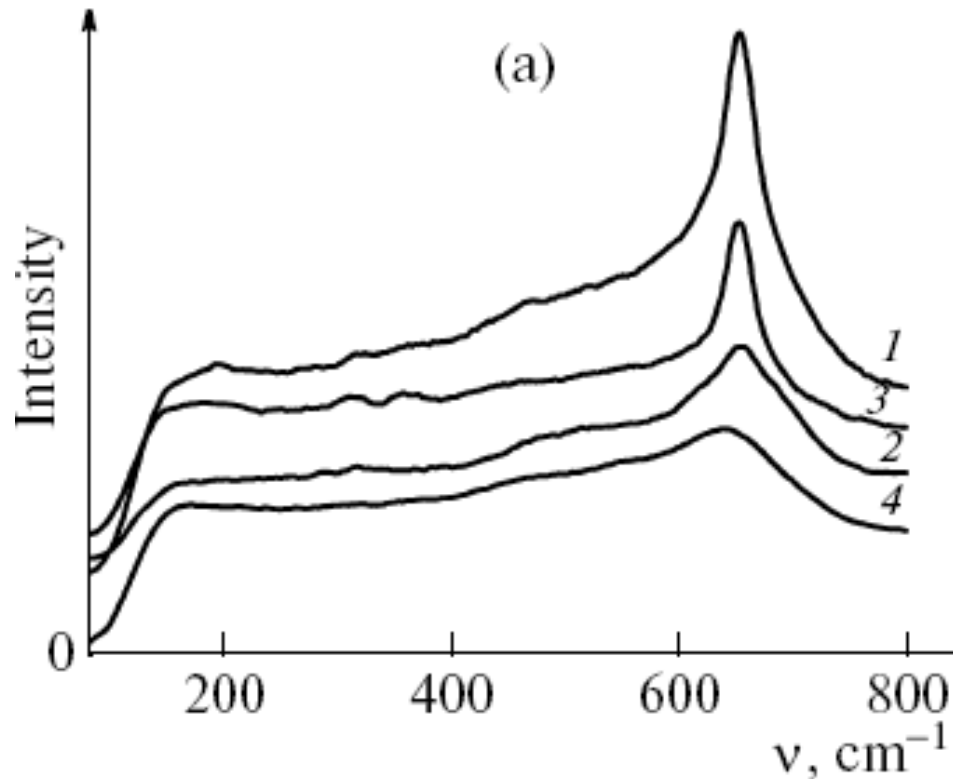
Strongly asymmetric oxygen coordination sphere in m-ZrO₂ (7-fold).

CeO₂ (1) and Ce_{1-x}Sm_x, at x=0.05 (2), 0.1 (3), 0.15 (4) and 0.2 (5).



Increase of Ce-O coordination sphere deformation with doping

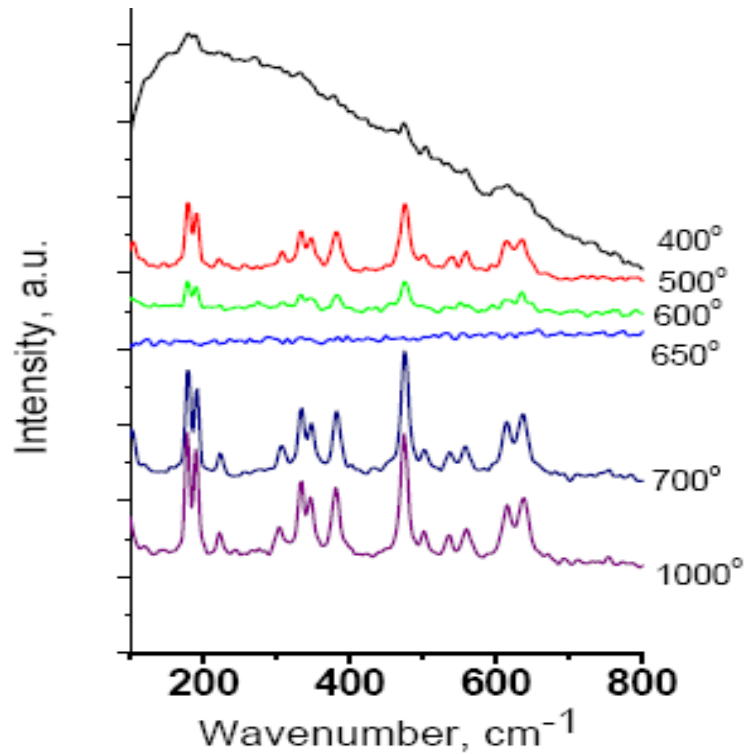
Raman (combined scattering of photons)



Excitation by 514.5 nm line
of Ar^+ laser
(1) LaCeMn , (2) LaFeMn ,
(3) LaBiMn , and (4)
 LaSrBiMn calcined at
 500°C ,

Number and intensity of lines is determined by local lattice symmetry
affected by the presence of defects and nanostructuring

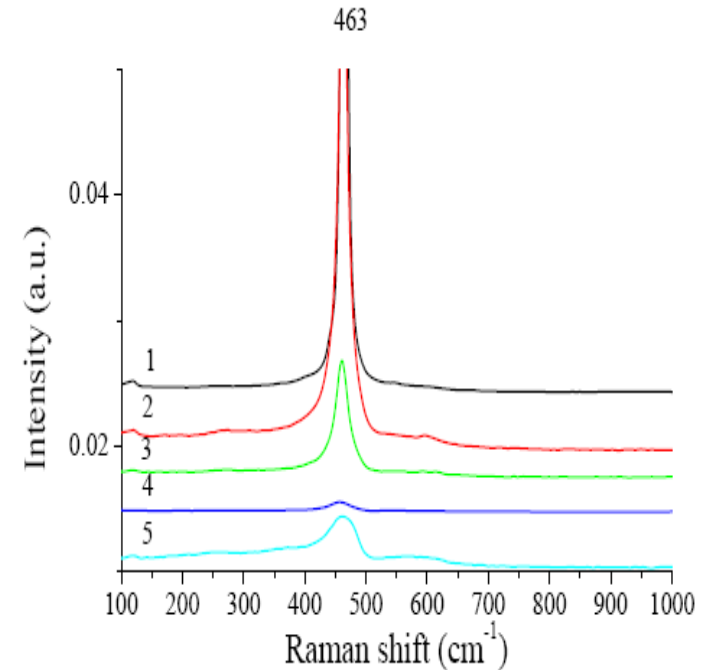
Band at $\sim 650 \text{ cm}^{-1}$ is due to presence of nanofragments with the structure of
layered perovskites in low-temperature manganites



Disappearance of Raman bands for samples with multiply twinned structure

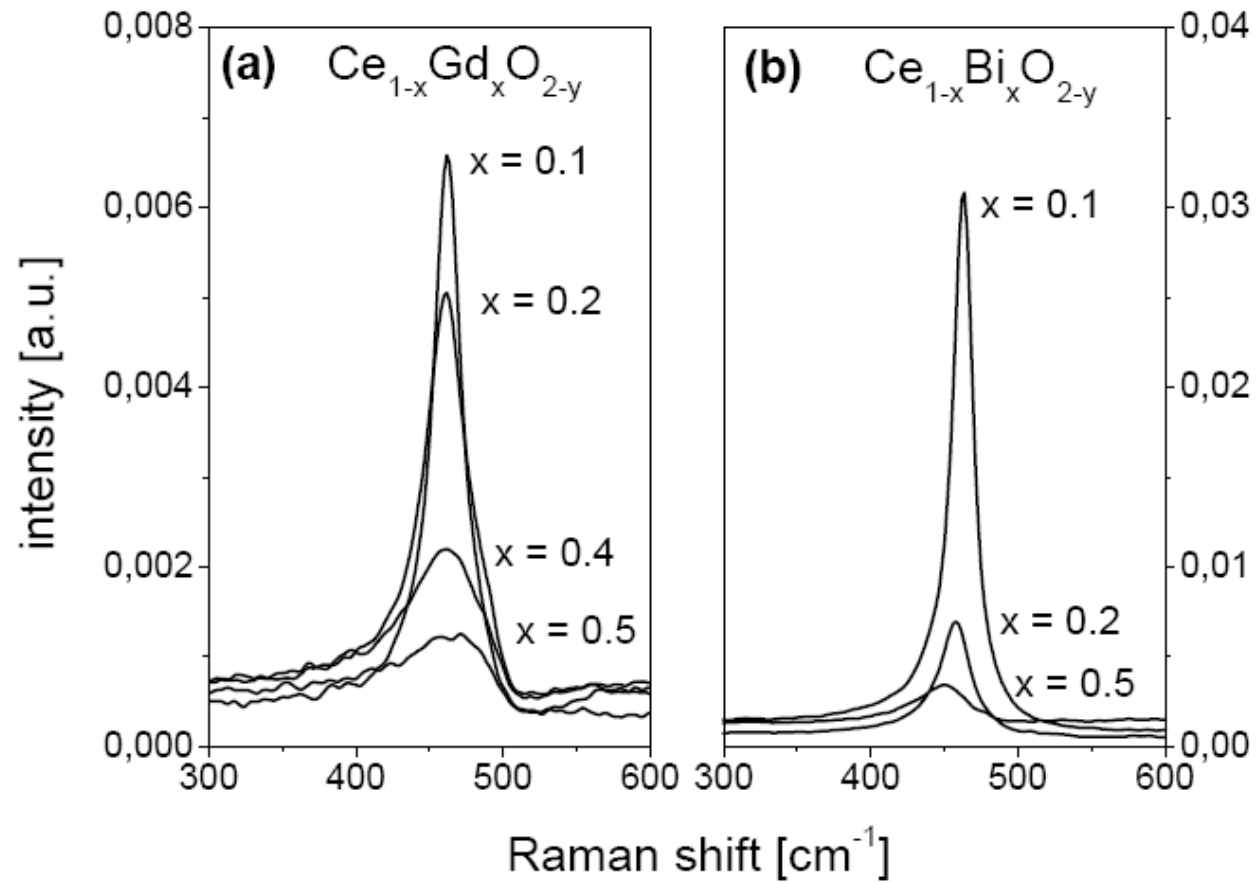
Raman

CeO₂ (1) and Ce_{1-x}Sm_x, at x=0.05 (2), 0.1 (3), 0.2 (4) and 0.4 (5).



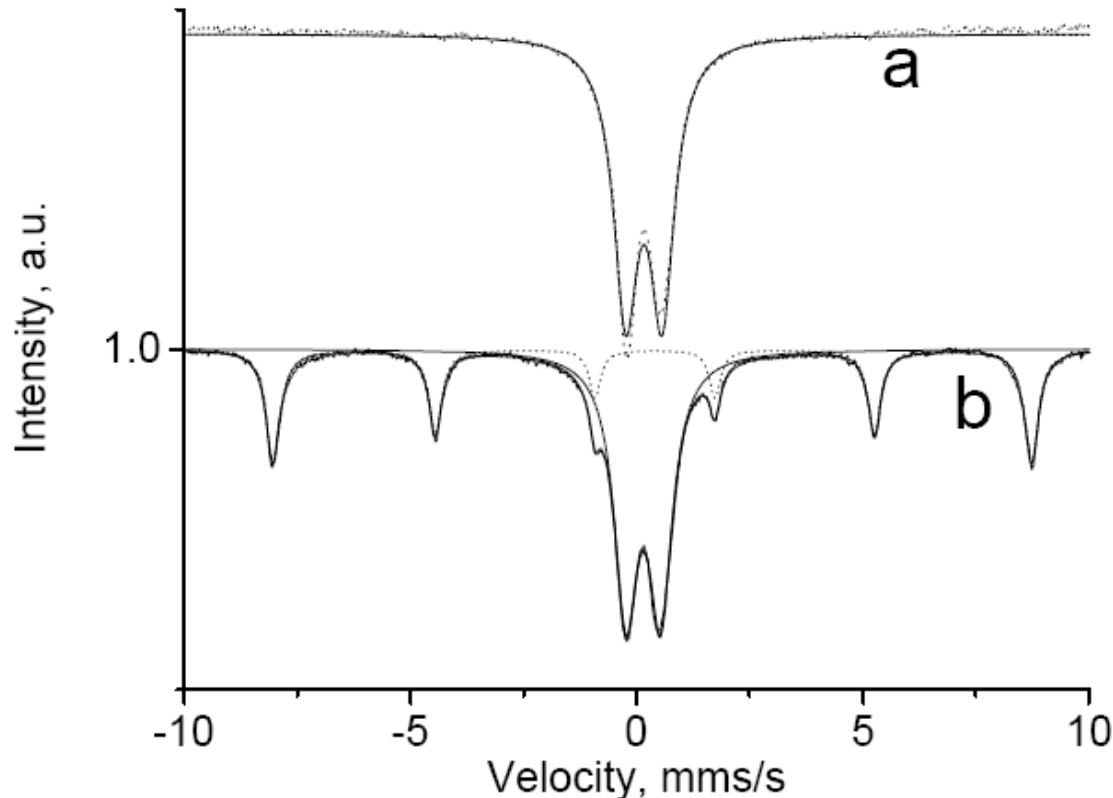
Decrease of Raman band intensity due to disordering up to x=0.2.
Splitting bands at x=0.4 due to local structure rearrangement.

Raman



Disordering with doping as well

Mossbauer spectroscopy



^{57}Fe absorbs γ -quantum emitted by Co isotope in a source.

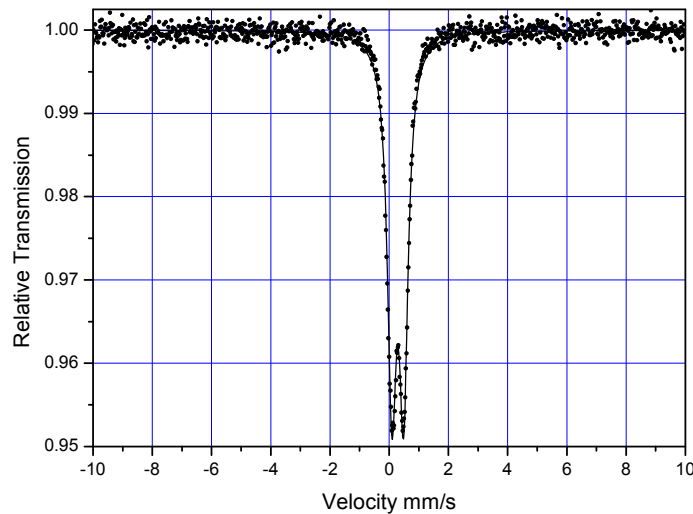
Absorption resonance depends upon matching initial and final states sensitive to charge, coordination and magnetic state of Fe nuclei in a target

$\text{La}_{9.83}\text{Si}_{5.5}\text{Fe}_{0.5}\text{O}_{26.5}$ (a) and $\text{La}_{10}\text{Si}_4\text{Fe}_2\text{O}_{26}$ (b).

Symmetrical doublet – isolated Fe^{3+} cations in distorted Td
Sextet - magnetically coupled Fe^{3+} cations in Oh (LaFeO_3)

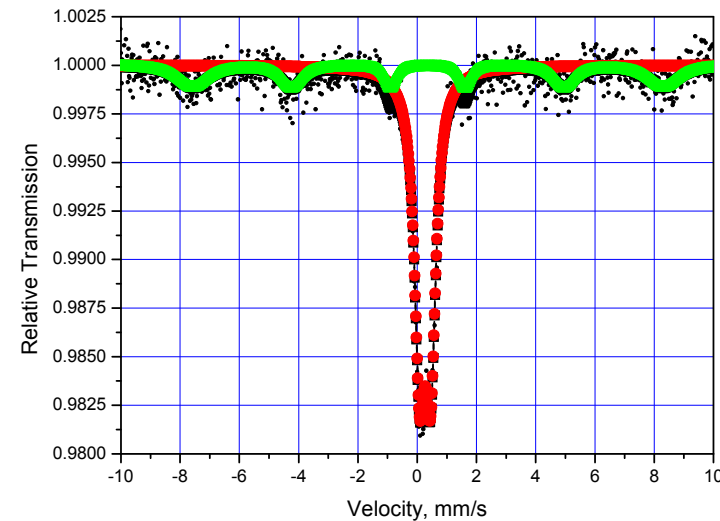
Mössbauer spectroscopy

LSNF 1200 °C



Doublet due to Fe dilution by Ni
Chem. shift 0.29(1) mm/s
Quadr. splitt. QS 0.40(1) mm/s

LSNF+GDC 1200 °C



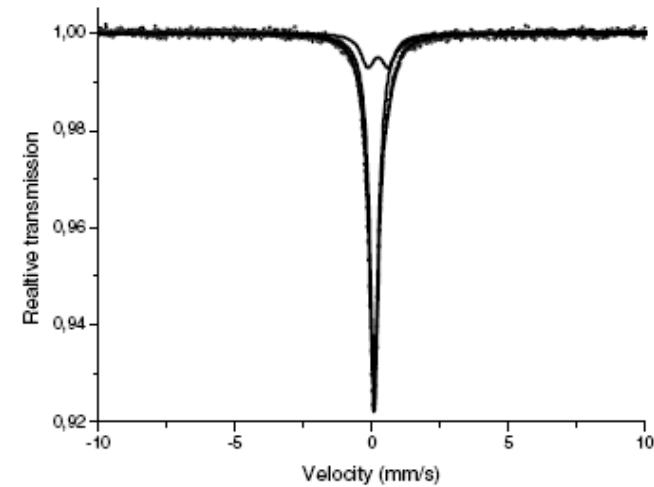
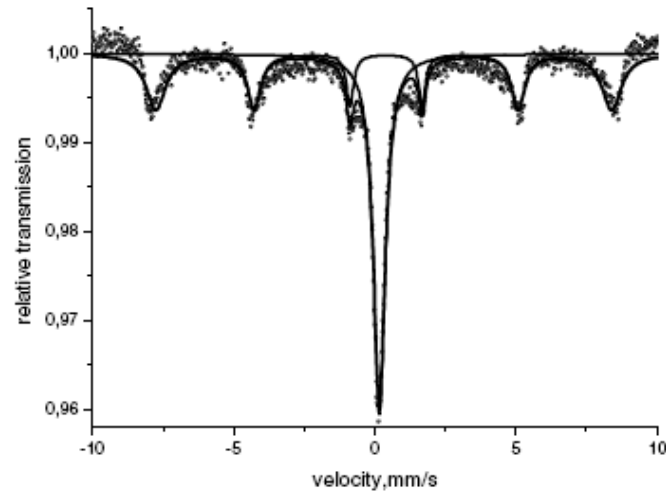
30% sextet :

H_{eff} 495 kOe, chem. shift 0.36, QS 0.00

70% doublet , chem. shift 0.27, QS 0.37

Local depletion of perovskite phase in nanocomposite by Ni due to its segregation as NiO or incorporation into GDC surface layers

Mössbauer spectroscopy



$\text{La}_{1-x}\text{Sr}_x\text{FeO}_{3-y}$ perovskites with $x=0.3$ (left) and $x=0.8$ (right)

Singlet is due to Fe^{4+} state

Mössbauer spectroscopy

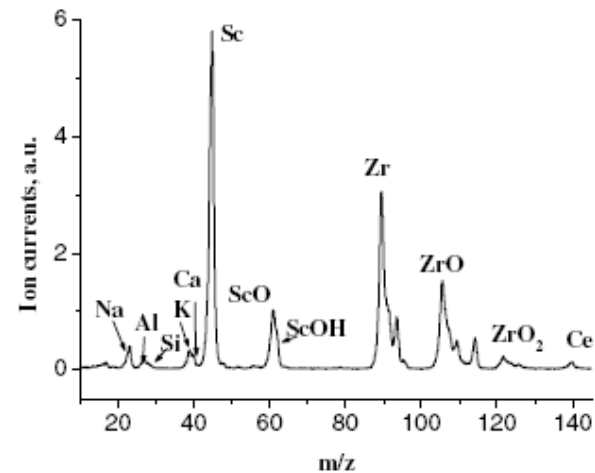
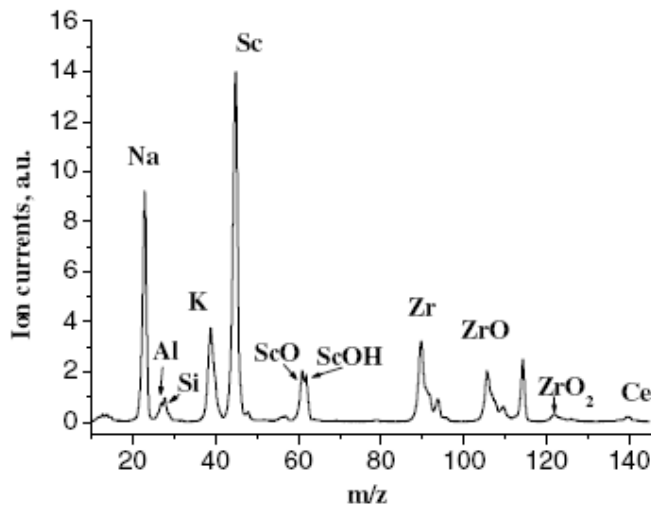
$\text{La}_{1-x}\text{Sr}_x\text{FeO}_{3-y}$ system

Components		O1 $\delta=0.37-0.36$		O2 $\delta=0.35$		D1 $\Delta\sim 0.3$	D2 $\Delta=0.15$	S	
Sample	$S_{\text{sp.}}$	H_{eff}	I, %	H_{eff}	I, %	I, %	I, %	δ	I, %
LaFeO_{3-y}	1.4	522	100						
$\text{La}_{0.8}\text{Sr}_{0.2}\text{FeO}_{3-y}$	3.1	511	27	425	66			0.17	7
$\text{La}_{0.7}\text{Sr}_{0.3}\text{FeO}_{3-y}$	2.6	503	51					0.16	49
$\text{La}_{0.4}\text{Sr}_{0.6}\text{FeO}_{3-y}$	1.3							0.14	100
$\text{La}_{0.2}\text{Sr}_{0.8}\text{FeO}_{3-y}$	0.9					21		0.09	79
SrFeO_{3-y}	0.1					9	44	0.03	47

Variation of coordination and charge state of Fe with composition

Secondary Ions Mass Spectrometry (SIMS)

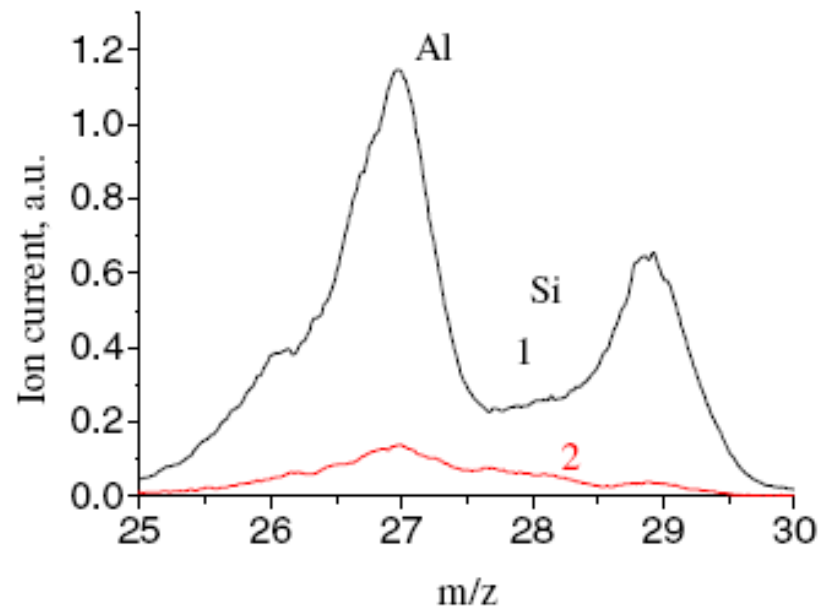
Surface layer is sputtered by ion beam (Ar^+), and emitted ion currents are analyzed by MS



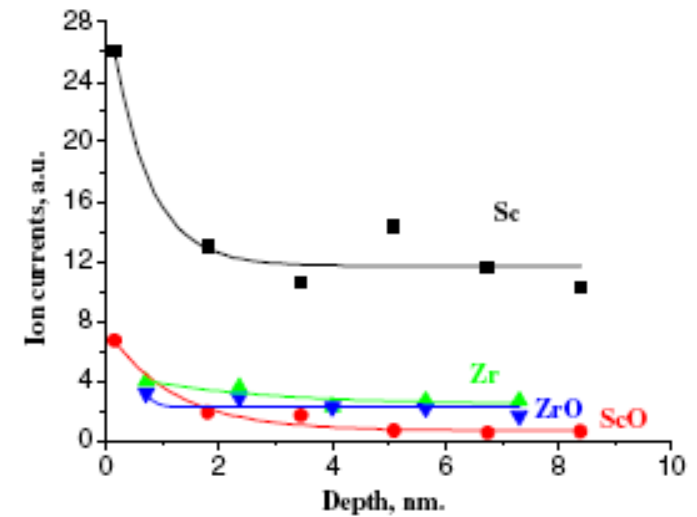
Typical mass-spectra for the surface layer (left) and the bulk (right) of ScCeSZ (Praxair) sample

+ admixed cations, + MeO^+ ions etc

SIMS



Comparison of the Al and Si content in the bulk (1) and in the surface layer (2) of ScCeSZ (DKKK) sample



Variation of the ion currents with sputtering depth for DKKK sample

Surface is contaminated by admixed cations

SIMS

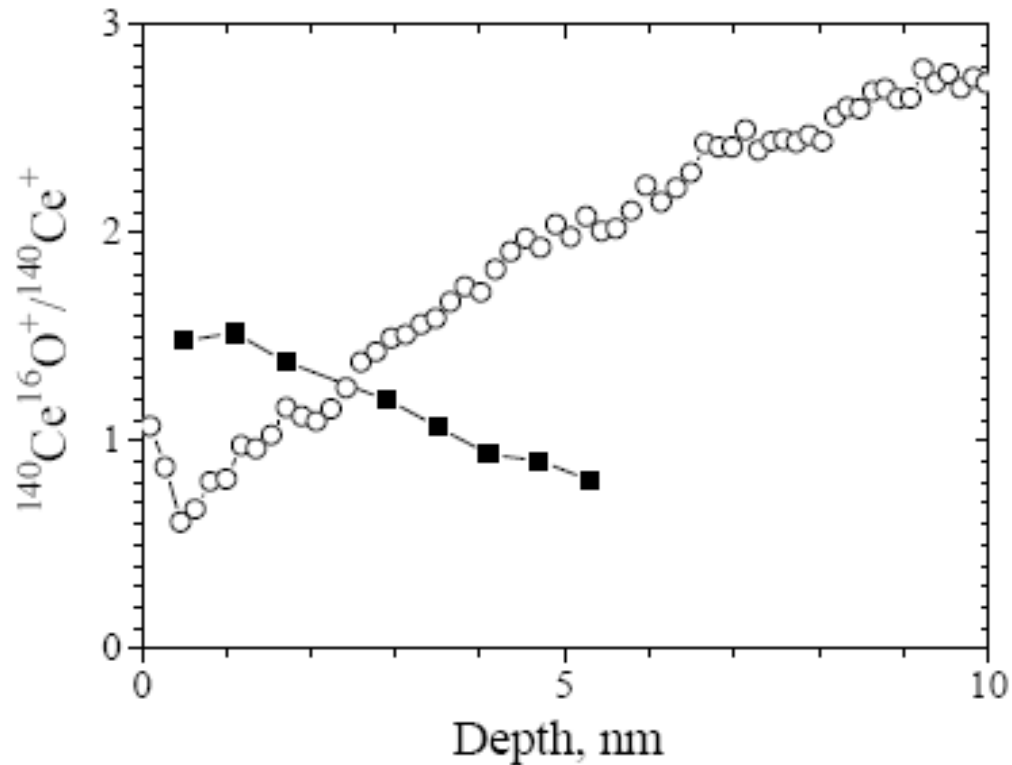
SIMS ratio of ion currents for doped ceria-zirconia samples

Sample	Zr^+/Ce^+		$(\text{La,Gd})^+/\text{Ce}^+$	
	Surface*	Bulk**	Surface*	Bulk**
$\text{Ce}_{0.5}\text{Zr}_{0.5}\text{O}_{2-y}$	0.12	0.11	-	-
$\text{Ce}_{0.4}\text{Zr}_{0.4}\text{La}_{0.2}$	0.15	0.25	0.55	0.55
$\text{Ce}_{0.35}\text{Zr}_{0.35}\text{La}_{0.3}$	0.20	0.35	0.9	0.9
$\text{Ce}_{0.4}\text{Zr}_{0.4}\text{Gd}_{0.2}$	0.25	0.30	0.08	0.08
$\text{Ce}_{0.35}\text{Zr}_{0.35}\text{Gd}_{0.3}$	0.15	0.25	0.10	0.10

* Within depth of 0.5-1 nm; **-after sputtering ~5-10 nm.

Surface is depleted by small Zr cations

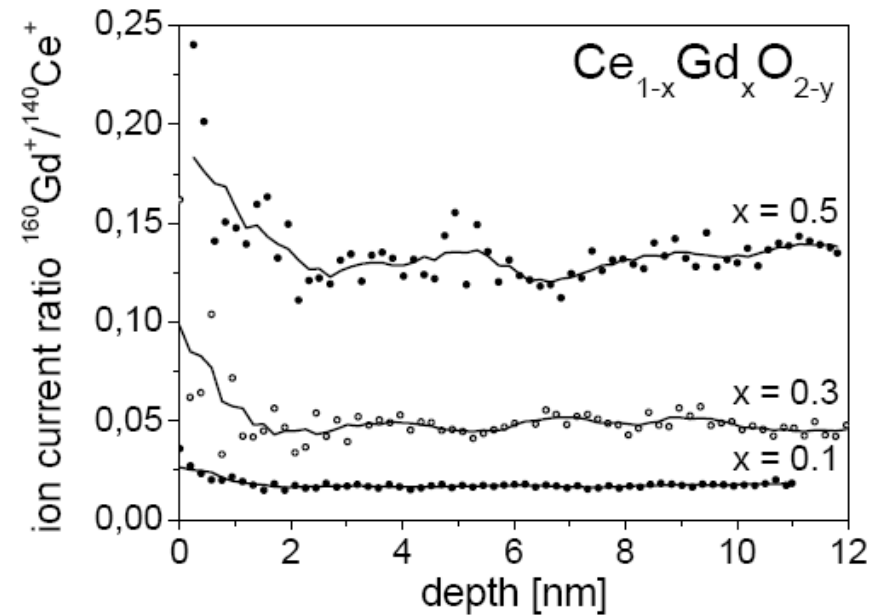
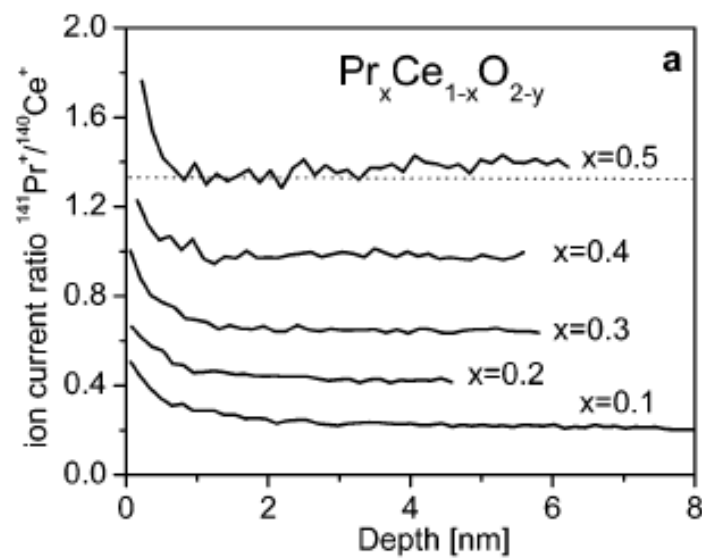
SIMS



Ratio of ion currents
 CeO^+/Ce^+ versus
sputtering depth for ceria-
zirconia samples doped
with 20 % La (circles) or
Gd (squares).

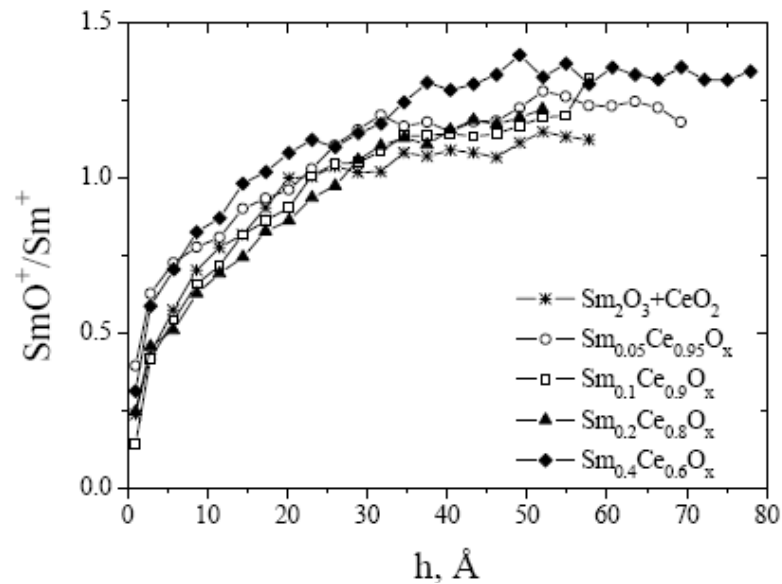
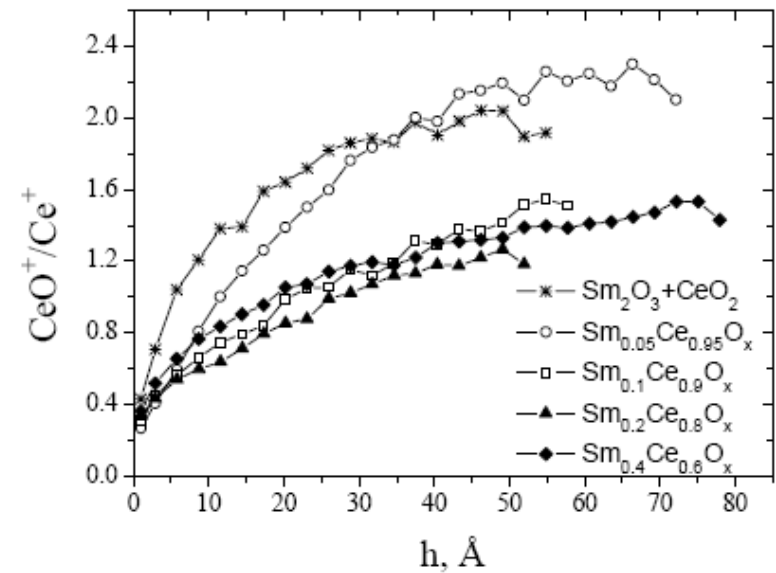
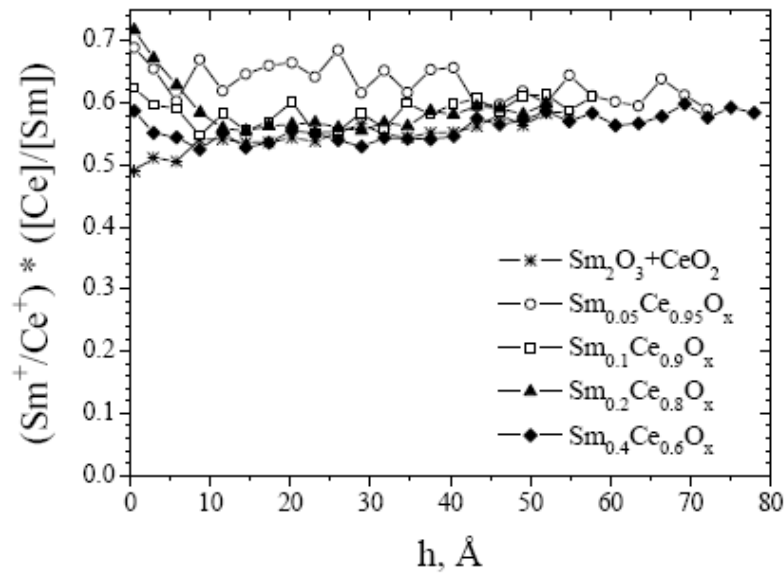
Average strength of Ce-O bond proportional to CeO^+/Ce^+ ion current ratio
strongly varies with the type of dopant and distance from the surface

Secondary Ions Mass Spectrometry (SIMS)



Enrichment of doped ceria surface layers by dopants

SIMS

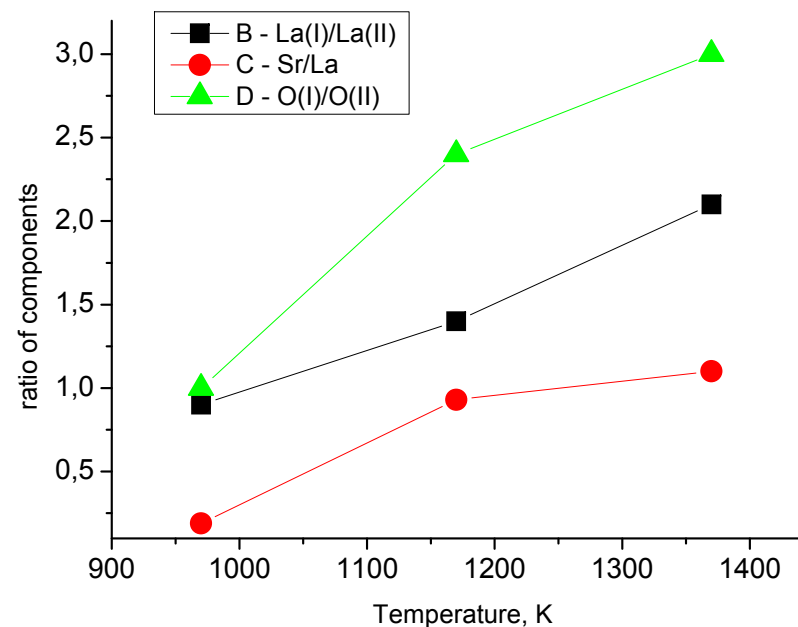
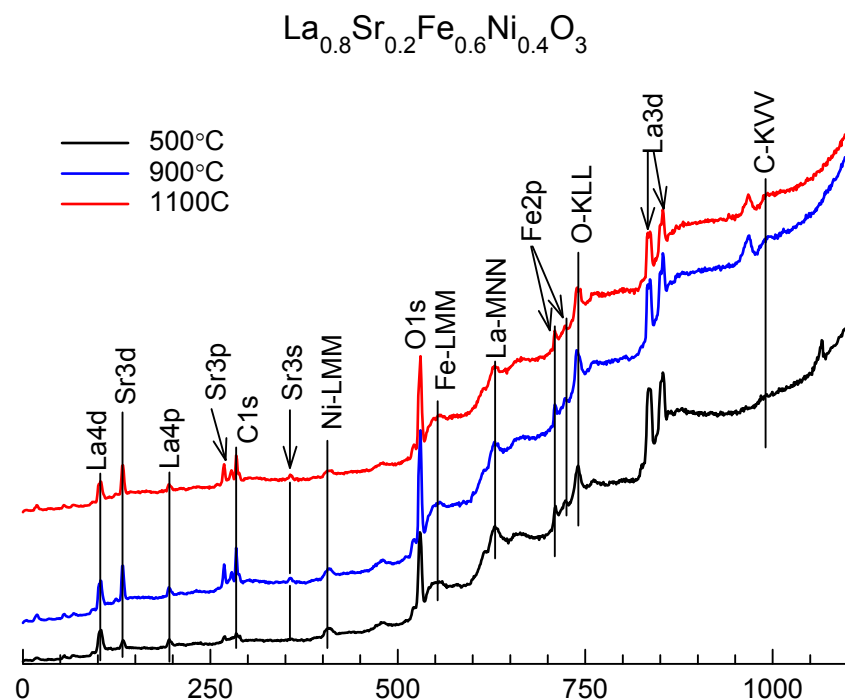


Decreased Me-O bonding strength in disordered surface layer of Sm-doped ceria
 \Rightarrow enhanced surface ion conductivity

X-ray Photoelectron Spectroscopy

- Principle: X-ray photon emits electron from different energetic levels of surface atoms, kinetic energy of electrons determined by detector allows to estimate binding energy of a given energy level (function of charge state and coordination sphere), their intensity –surface concentration of elements within probing depth.

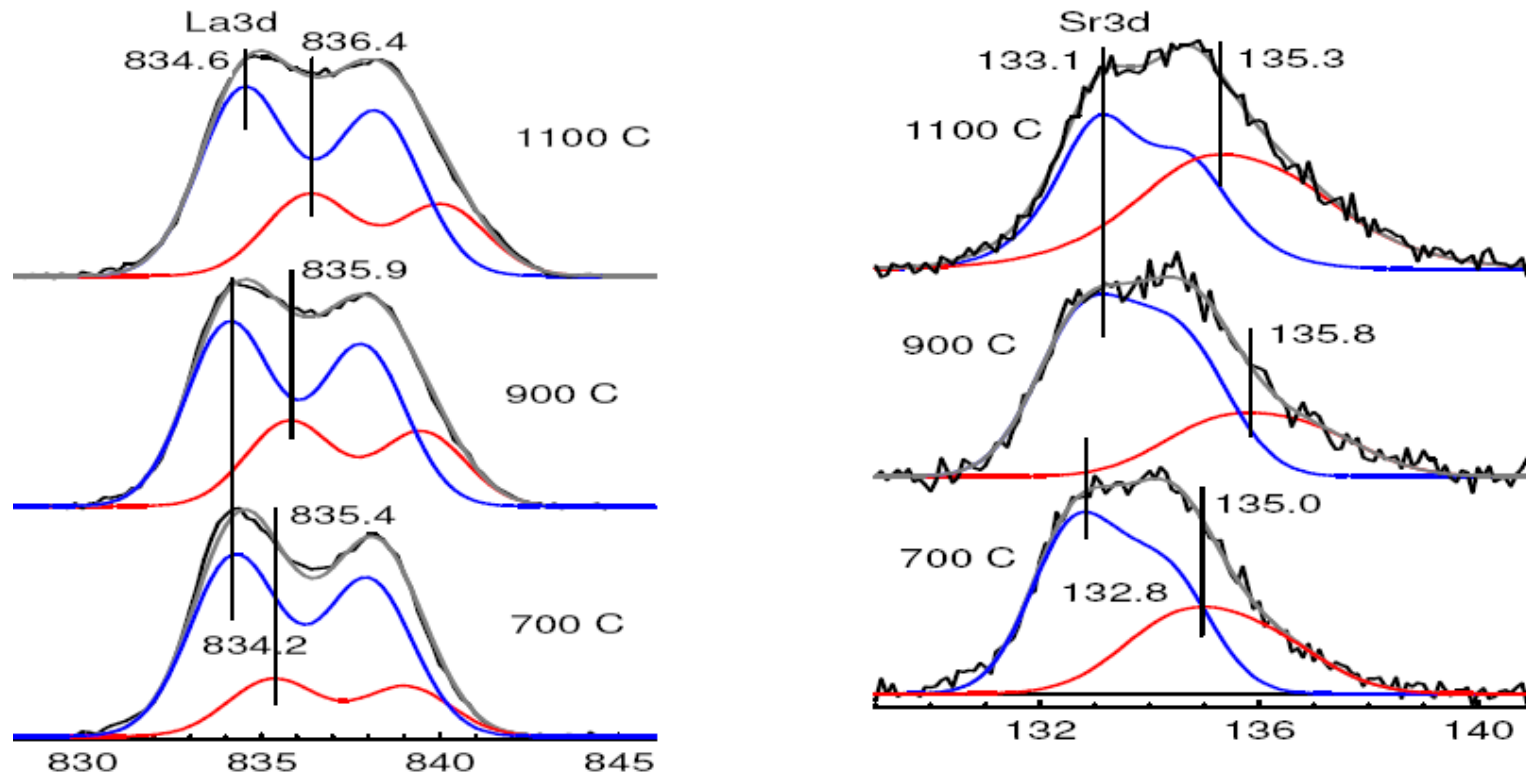
Surface composition by XPS for Sr-doped perovskites



Plenty of carbonates in the surface layer, progressive Sr segregation on the surface with \uparrow annealing T, two forms of oxygen –ionic and covalent, + two states of La differing by BE/effective charge. \Rightarrow modification of surface layer due to segregated Sr, could result in degradation at IT range

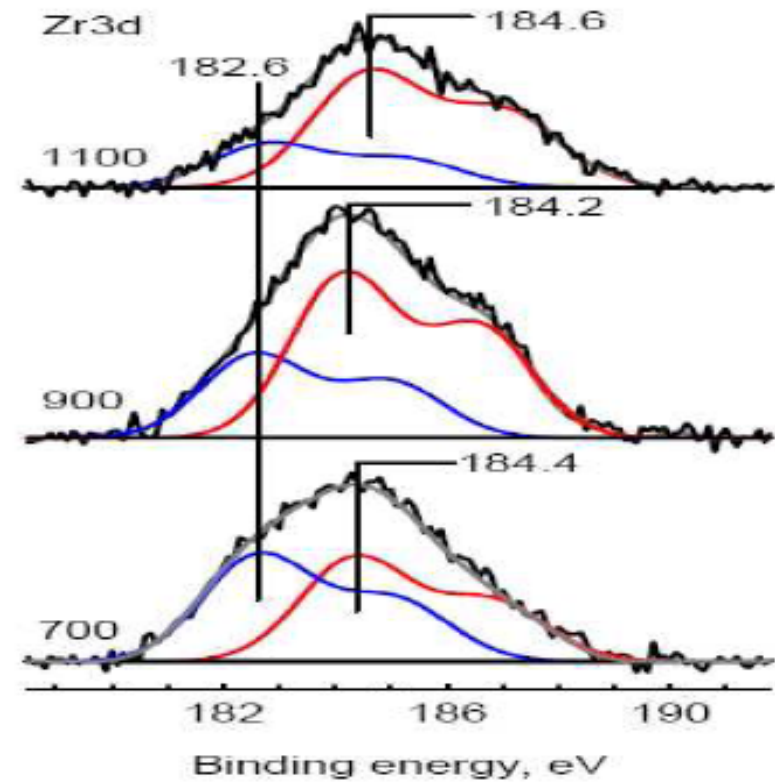
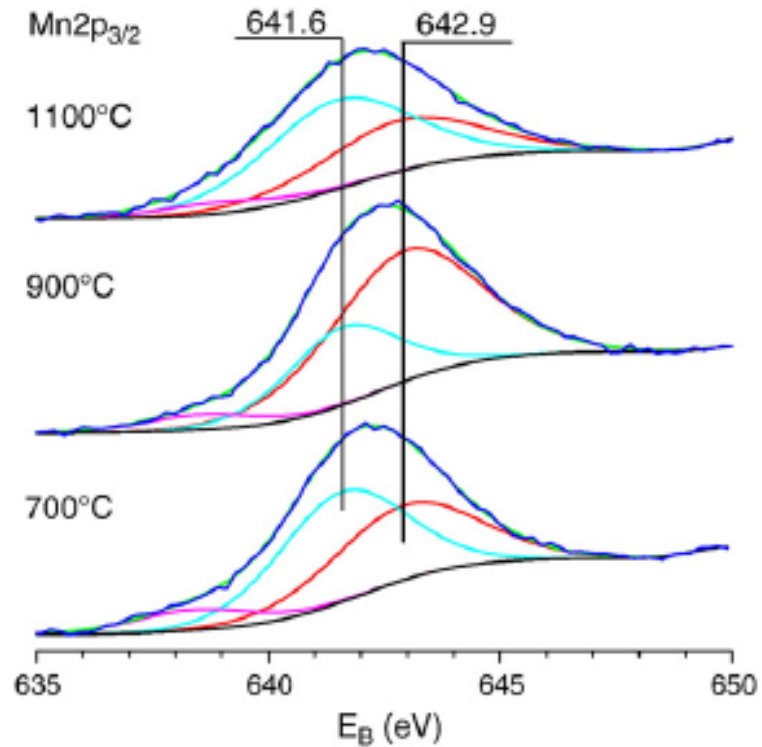
XPS: nanocomposites

XPS spectra of La and Sr cations in the surface layer of LSM-ScCeSZ nanocomposites sintered at different temperatures



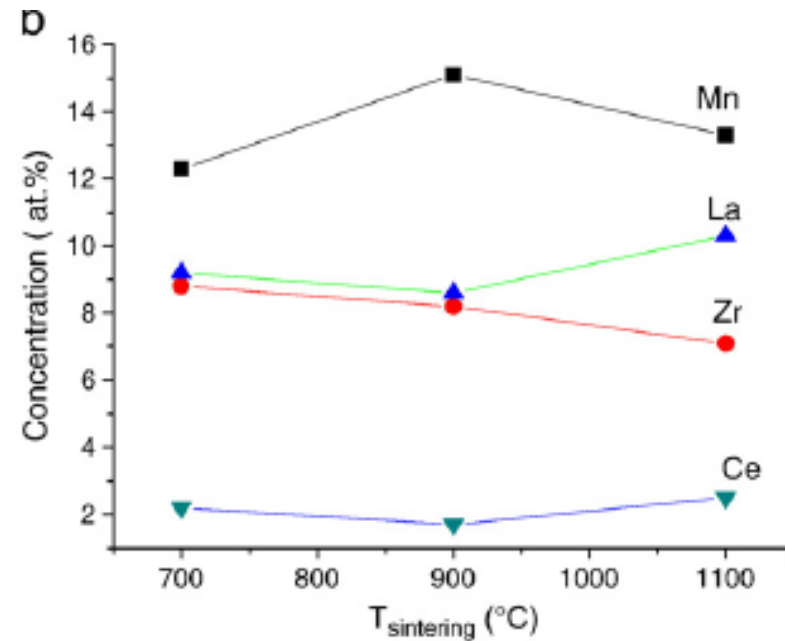
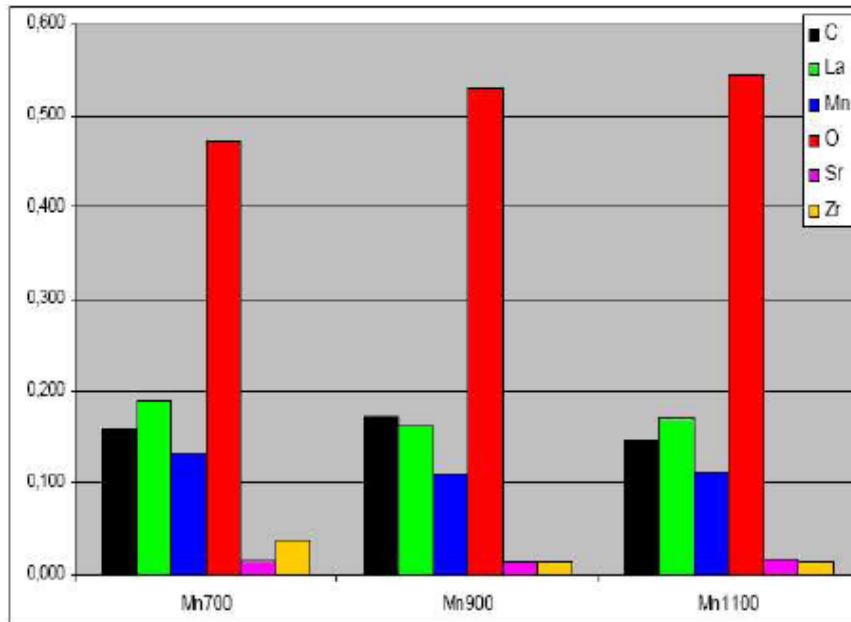
Two states of cations redistributed between P and F phases

XPS



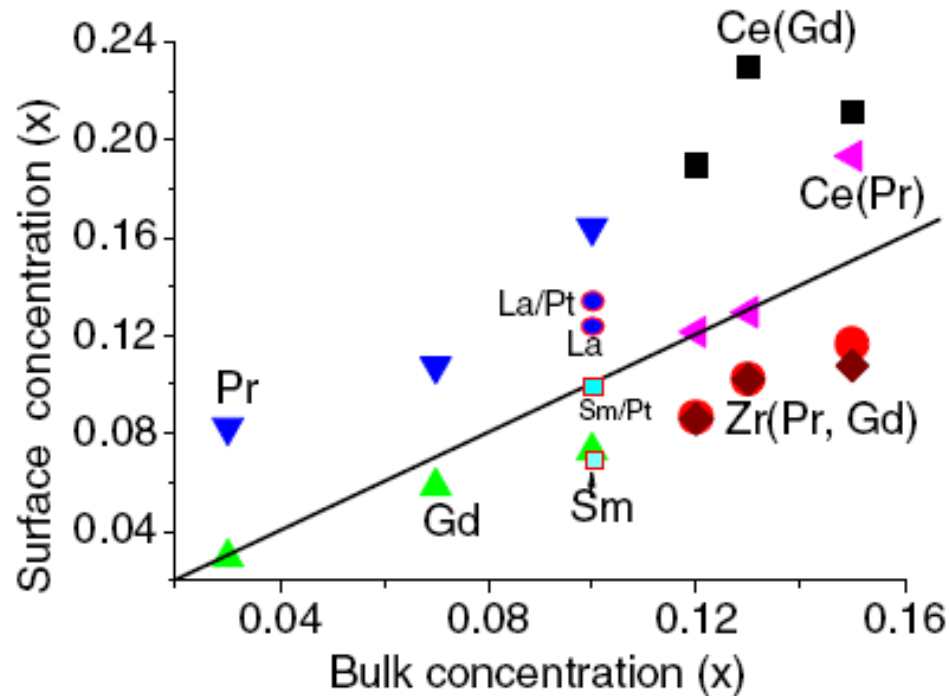
Two types of Zr and Mn cations differing by local coordination numbers and effective charge

XPS: surface composition



Carbon is present on the surface (carbonates)
Mn and La are transferred onto ScCeSZ surface

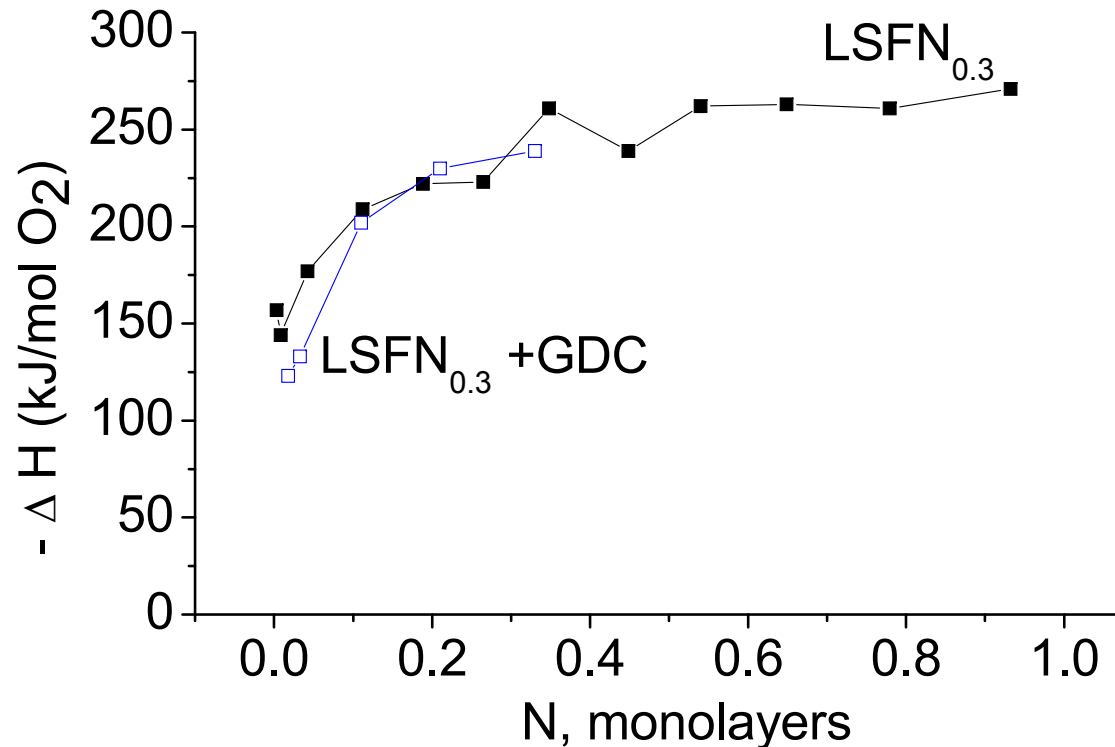
XPS: surface segregation



Surface (XPS) vs bulk composition for doped ceria – zirconia samples (type of doping cation indicated in parenthesis). La/Pt (Sm/Pt) - samples with supported Pt (1.4wt.%).

Segregation of big cations in the surface layer

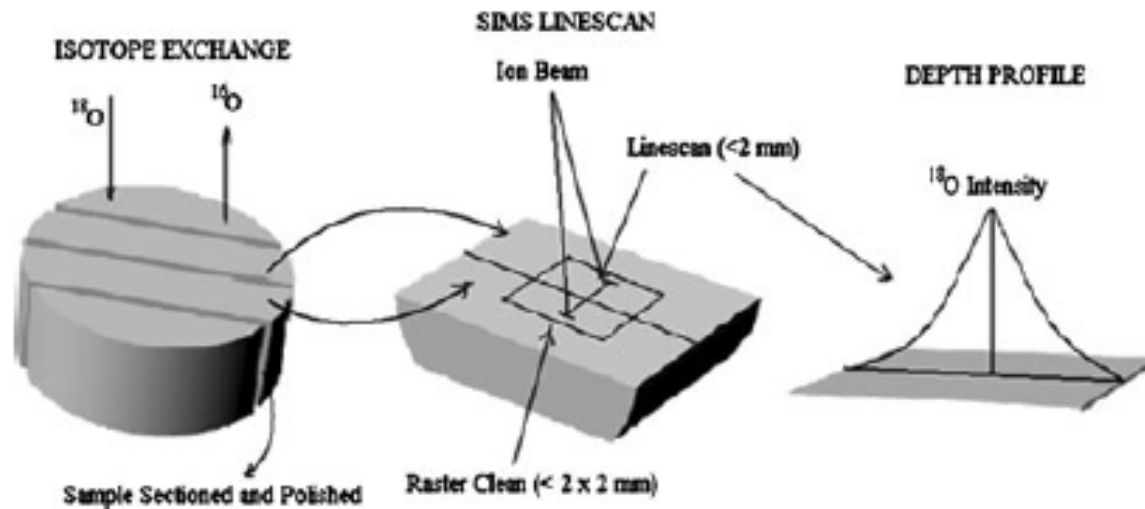
Oxygen bonding strength by calorimetry



Heat of oxygen adsorption vs. amount of desorbed O_2 for $LSFN_{0.3}$ and $LSFN_{0.3} + GDC$ composite sintered at 1200 °C and pretreated in He at 750°C. Pulses of O_2 in He at 450 °C.

Broad variation of adsorption heats, hence, oxygen bonding strength

Transport properties: Tracer diffusion coefficient of oxide ions by SIMS



Sample is exchanged with $^{18}\text{O}_2$, then surface layer is sputtered by ion beam and ^{18}O depth profile is analyzed

$$C'(x, t) = \frac{C(x, t) - C_{bg}}{C_g - C_{bg}} = \text{erfc}\left[\frac{x}{2\sqrt{D^*t}}\right] - \left[\exp\left(\frac{kx}{D^*} + \frac{k^2t}{D^*}\right) \times \text{erfc}\left(\frac{x}{2\sqrt{D^*t}} + k\sqrt{\frac{t}{D^*}}\right)\right]$$

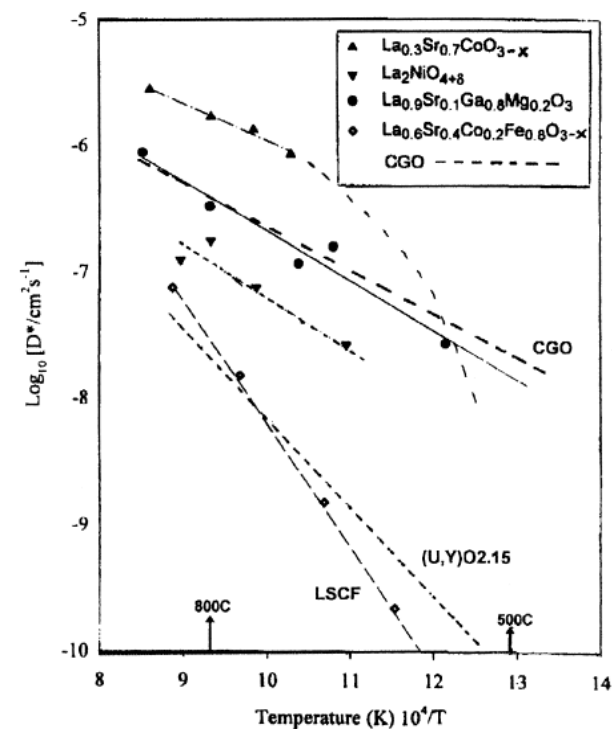
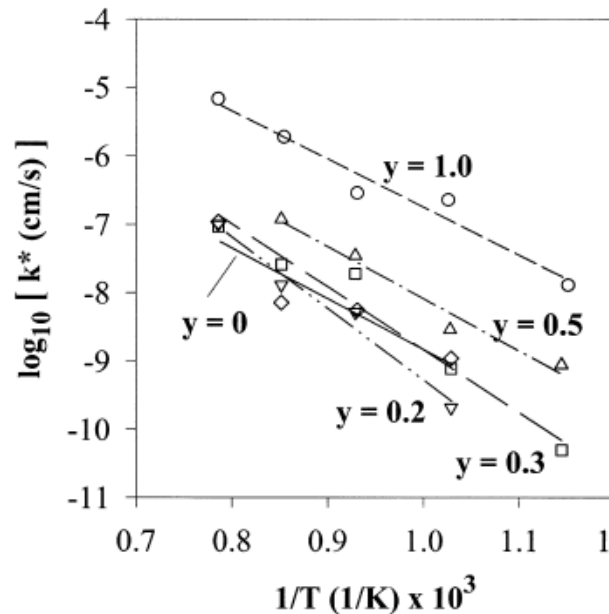
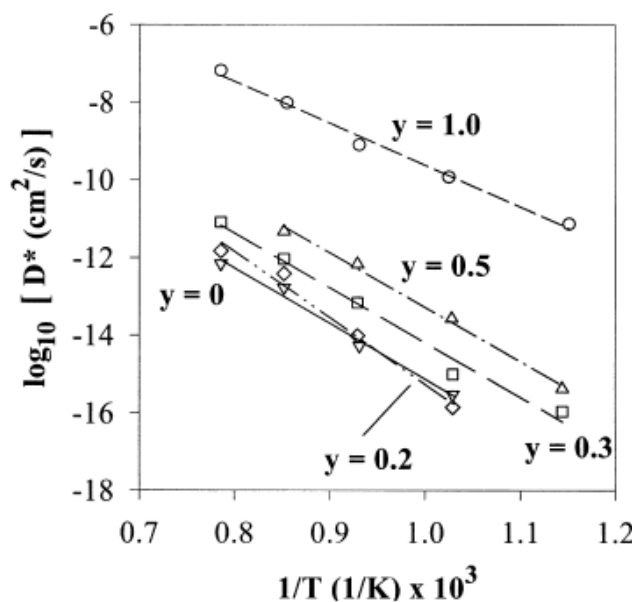
D^* -oxygen self-diffusion coefficient, k - surface exchange coefficient

$$k(c_g - c_s) = -D \left. \frac{\partial C(x)}{\partial x} \right|_{x=0}$$

characterizing the rate of surface exchange reaction

Scale of D and k variation

La –Sr- Mn- Co- O perovskites



Broad variation controlled by defect structure, oxygen bonding strength and mechanism of oxygen migration

Diffusion parameters by weight and conductivity relaxations at pO₂ change –dense ceramics

$$\frac{\partial C}{\partial t} = \frac{1}{r} \frac{\partial}{\partial r} \left(D_{\text{chem}} \frac{\partial C}{\partial r} \right) \text{ for } r \text{ direction}$$

$$-D_{\text{chem}} \frac{\partial C}{\partial r} \Big|_{r=\pm a} = k_{\text{chem}}(C - C_{\infty}),$$

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial y} \left(D_{\text{chem}} \frac{\partial C}{\partial y} \right) \text{ for length direction}$$

$$-D_{\text{chem}} \frac{\partial C}{\partial y} \Big|_{y=\pm l} = k_{\text{chem}}(C - C_{\infty})$$

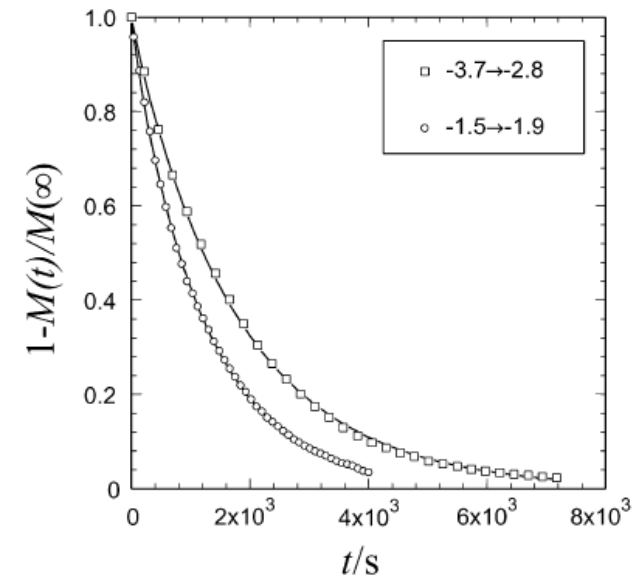
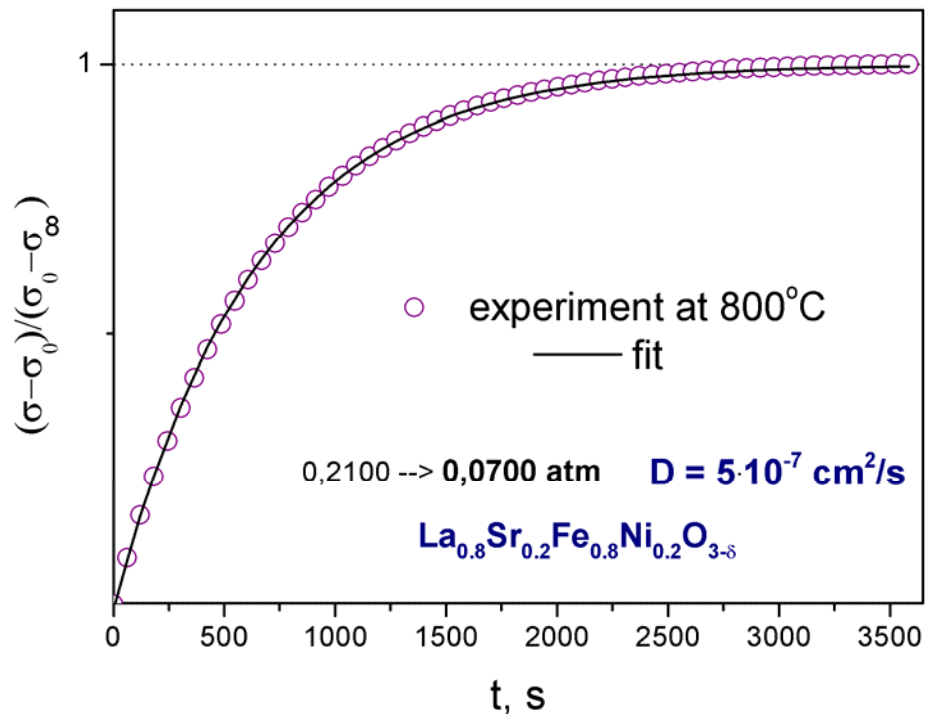
$$\begin{aligned} \frac{M(t)}{M(\infty)} = & 1 - \sum_{n=1}^{\infty} \sum_{m=1}^{\infty} \frac{4L_c^2 \exp(-\beta_n^2 D_{\text{chem}} t / a^2)}{\beta_n^2 (\beta_n^2 + L_c^2)} \\ & \times \frac{2L_p^2 \exp(-\gamma_m^2 D_{\text{chem}} t / l^2)}{\gamma_m^2 (\gamma_m^2 + L_p^2 + L_c^2)} \end{aligned}$$

$$\begin{aligned} \frac{\sigma_t - \sigma_0}{\sigma_{\infty} - \sigma_0} = & 1 - \sum_{i=1}^{\infty} \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \frac{2L_1^2 \exp(-\beta_i^2 \tilde{D}_0 t / h^2)}{\beta_i^2 (\beta_i^2 + L_1^2 + L_1)} \\ & \times \frac{2L_2^2 \exp(-\gamma_m^2 \tilde{D}_0 t / w^2)}{\gamma_m^2 (\gamma_m^2 + L_2^2 + L_2)} \times \frac{2L_3^2 \exp(-\delta_n^2 \tilde{D}_0 t / l^2)}{\delta_n^2 (\delta_n^2 + L_3^2 + L_3)} \end{aligned}$$

$$\frac{\sigma(t) - \sigma(0)}{\sigma(\infty) - \sigma(0)} = 1 - \sum_{n=0}^{\infty} \frac{8}{(2n+1)^2 \pi^2} \exp \left[\frac{-(2n+1)^2 \pi^2 D_{\text{chem}} t}{4l^2} \right]$$

More simple if limited by diffusion

Typical conductivity and weight relaxations

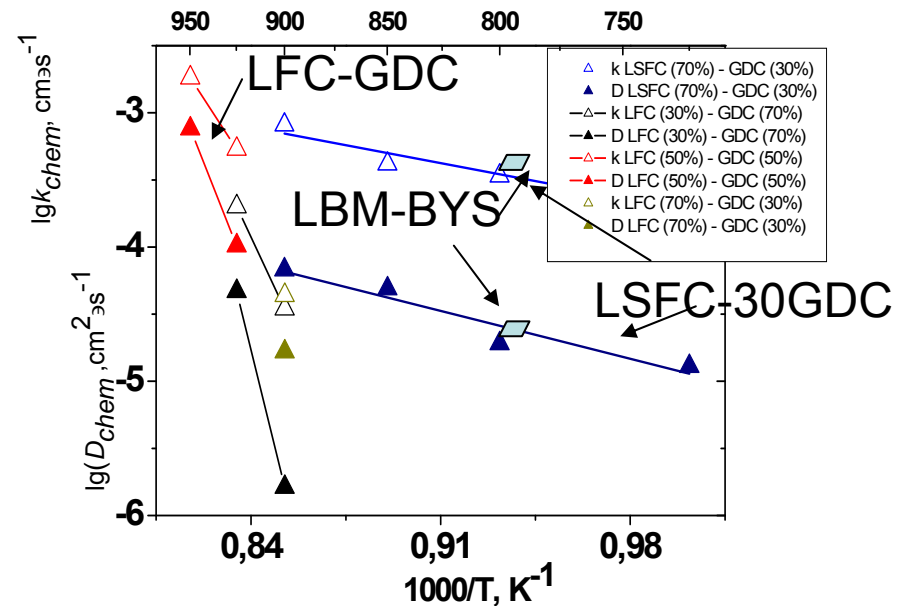
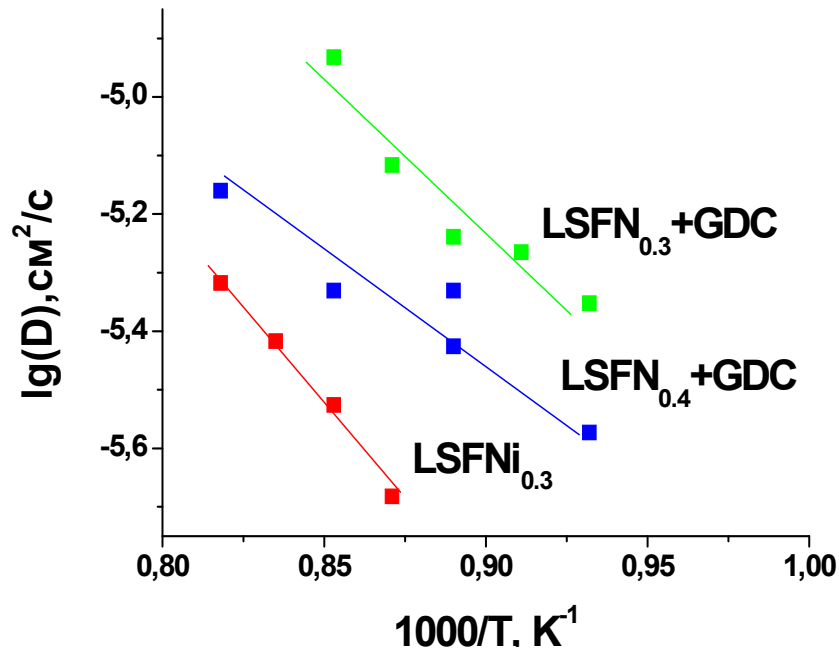


$$K_{\text{chem.}} = k^* \gamma; D_{\text{chem}} = D^* \gamma, \text{ where } \gamma = \frac{1}{2} \frac{\partial \ln P_{\text{O}_2}}{\partial \ln c_{\text{O}}}$$

Can be used only for MIEC materials able to change stoichiometry, i.e. adsorb/desorb oxygen

Estimation of D_{chem}

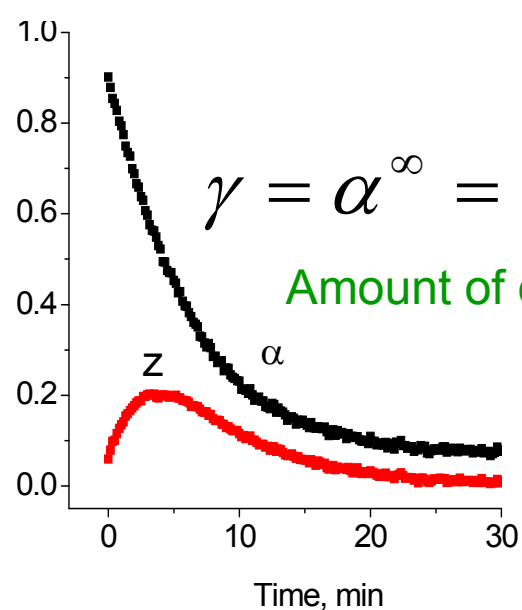
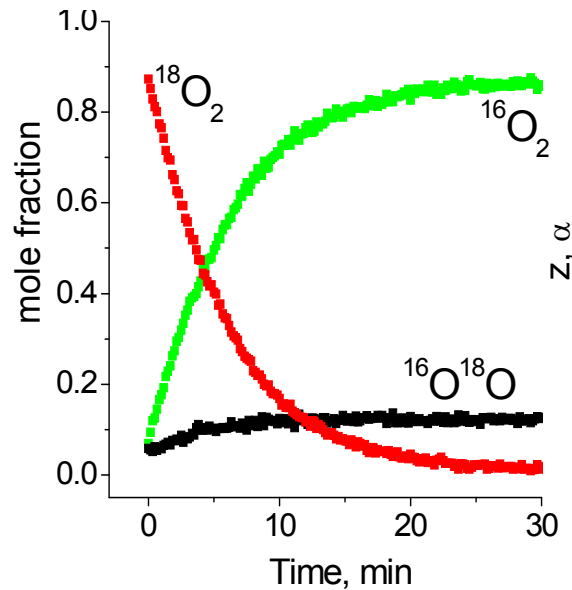
by weight loss relaxation



D is bigger in nanocomposite due to fast diffusion along perovskite-fluorite interface

Close values of D and k for LBM-BYS and LSFC-GDC known for the high oxygen mobility

Isothermal isotope exchange in static system: typical dependencies for LSCF-30%GDC powder



$$N_e = 2N \frac{\alpha^0 - \gamma}{\gamma}$$

$$\gamma = \alpha^\infty = \alpha_s^\infty \quad \text{equilibrium isotope fraction}$$

Amount of exchangeable oxygen > 100 ML

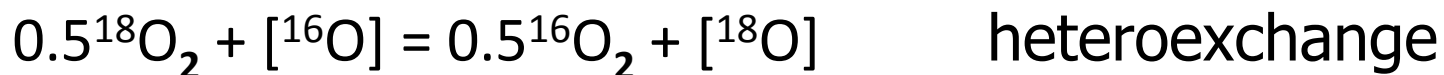
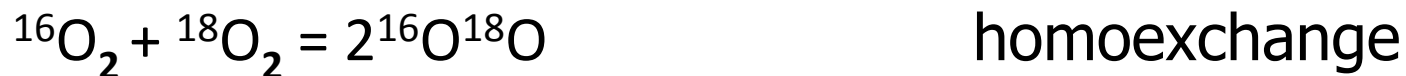
Dependence of $\alpha(t)$ is close to exponential \Rightarrow uniform oxygen \Rightarrow very fast bulk diffusion

$$Rt = -\frac{2N}{2N + N_e} \ln \frac{\gamma - \alpha}{\gamma - \alpha^0}$$

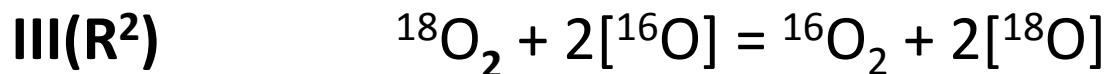
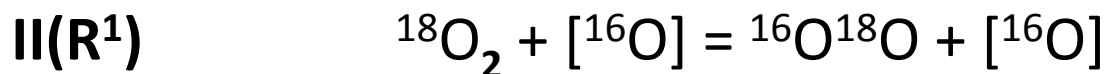
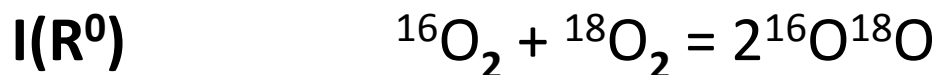
Simple estimation of R –specific rate of exchange as characteristic of surface reaction

Rate of heteroexchange ($R_0 = 5.8 \cdot 10^{17}$ molecules $O_2/s \cdot m^2$ at $550^\circ C$ and $P_{in} = 1.7$ Torr) is close to that for LSCF and is one of the highest for oxides
 $E_a \sim 80$ kJ/mol

Isotope exchange reactions by Muzykantov



Types of exchange mechanisms



Types and Mechanisms of Dioxygen Exchange by

Muzykantov

The reversible Steps of Gas–Surface–Bulk Processes realizing Exchange:

- 1) $O_2 + 2 Z_{ads} \leftrightarrow 2 ZO_{ads}$
- 2) $O_2 + Z_{ads} + ()_s \leftrightarrow ZO_{ads} + (O)_s$
- 3) $ZO_{ads} + ()_s \leftrightarrow Z_{ads} + (O)_s$
- 4) $(O)_s + []_v \leftrightarrow ()_s + [O]_v$

The ratio of the rates of these stages determines the shares of different types of exchange

Isotope-kinetic equations

by Muzykantov

x_0 – $^{16}\text{O}_2$ mole fraction, x_1 and x_2 – $^{16}\text{O}^{18}\text{O}$ и $^{18}\text{O}_2$, respectively

$$\alpha = 0.5x_1 + x_2$$

^{18}O fraction in gas

$$z = x_2 - \alpha^2$$

deviation from equilibrium binomial isotope distribution

$$\frac{\partial \alpha}{\partial t} = -r(\alpha - \alpha_s)$$

$$\frac{\partial z}{\partial t} = -kz + k_3(\alpha - \alpha_s)^2$$

$$r = 0.5k_2 + k_3$$

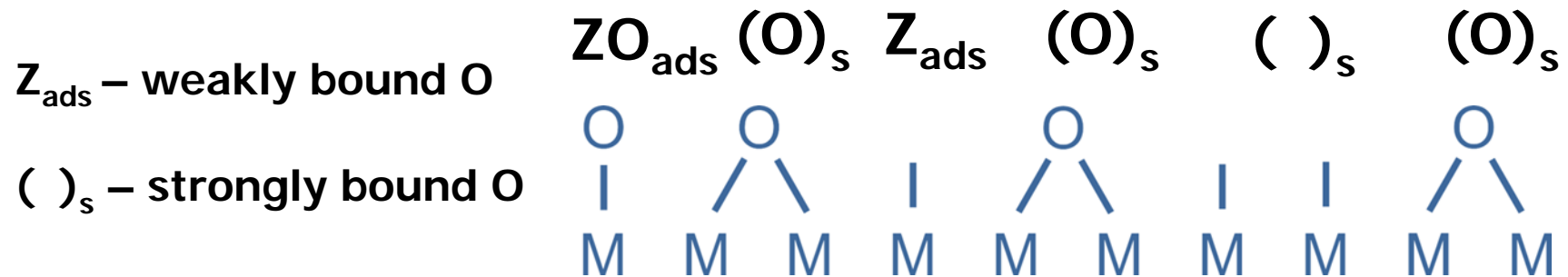
Rate of heteroexchange, $\langle \text{time} \rangle^{-1}$

$$k = k_1 + k_2 + k_3$$

Total rate of exchange, $\langle \text{time} \rangle^{-1}$

Surface forms by Muzykantov

Structure sensitivity of exchange due to variation of z_s and $()_s$ ratio
as dependent on chemistry and defect structure



System of equations for diffusion model of isotope exchange in closed system

$$N \frac{\partial \alpha}{\partial t} = -N_s R (\alpha - \alpha_s)$$

$$N_s \frac{\partial \alpha_s}{\partial t} = N_s R (\alpha - \alpha_s) - N_{bulk} \frac{D}{h^2} \frac{\partial \alpha_{bulk}}{\partial \eta} \bigg|_{\eta=0}$$

h-characteristic size of oxide particle

$$\frac{\partial \alpha_{obulk}}{\partial t} = \frac{D}{h^2} \frac{\partial^2 \alpha_{obulk}}{\partial \eta^2}$$

η -dimensionless depth of the oxide layer

$$N \frac{dx_1}{dt} = N_s R \left[(1-b)(\alpha(1-\alpha_s) + \alpha_s(1-\alpha) - x_1) + b(2\alpha_s(1-\alpha_s) - x_1) \right]$$

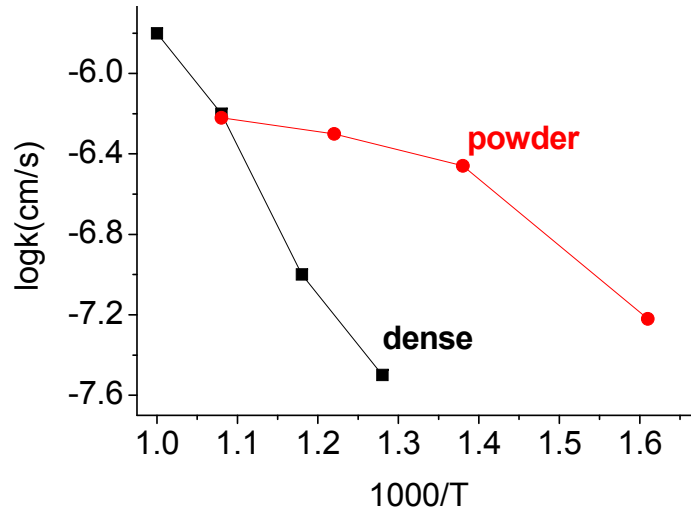
$$N \frac{dx_2}{dt} = N_s R \left[(1-b)(\alpha\alpha_s - x_2) + b(\alpha_s^2 - x_2) \right]$$

b- a share of the exchange mechanism III in the overall exchange rate R

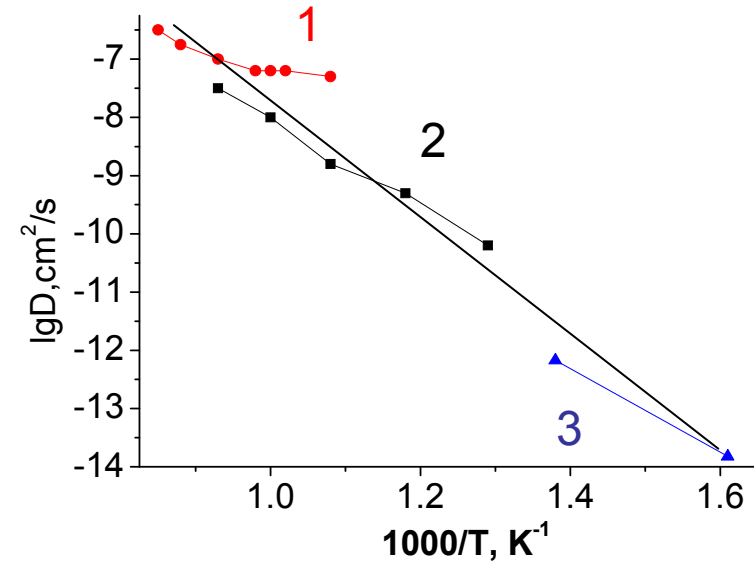
Initial and boundary conditions

$$\alpha = 0.96 \quad \eta = 0 \quad \alpha_{bulk} = \alpha_s \quad \alpha_{bulk} = 0 \quad \alpha_s = 0$$

Powders vs. dense ceramics: comparison for LSFC-GDC case studies



Powder-isotope exchange in static reactor; dense –SIMS IEP

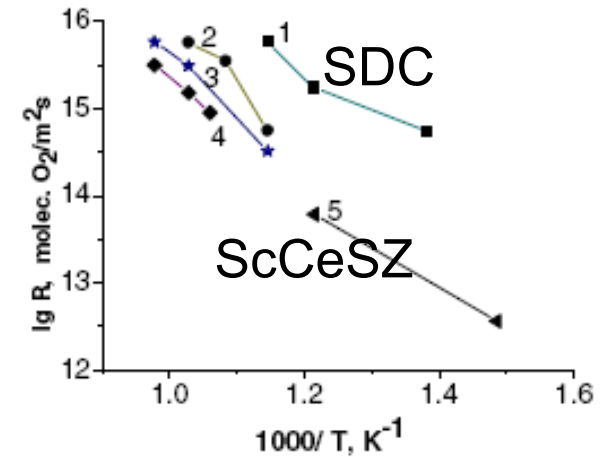
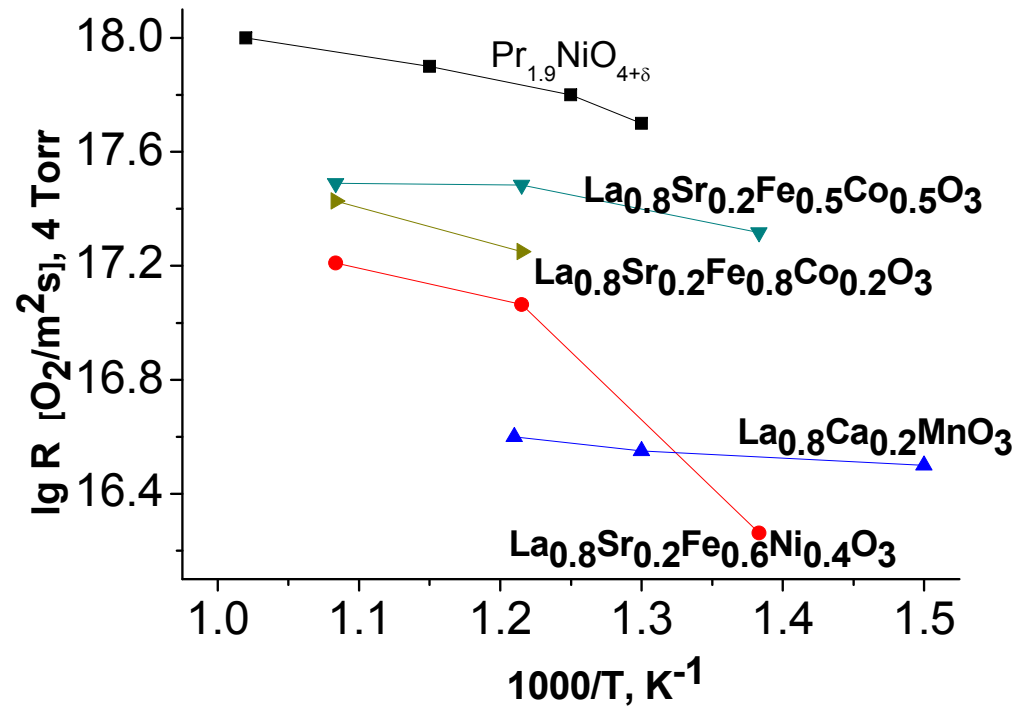


1-weight relaxation, pellet
2-SIMS IEP, pellet
3- isotope exchange, powder

Reasonable agreement in D as bulk property

Much higher sensitivity of k to surface state-defects, admixtures etc.

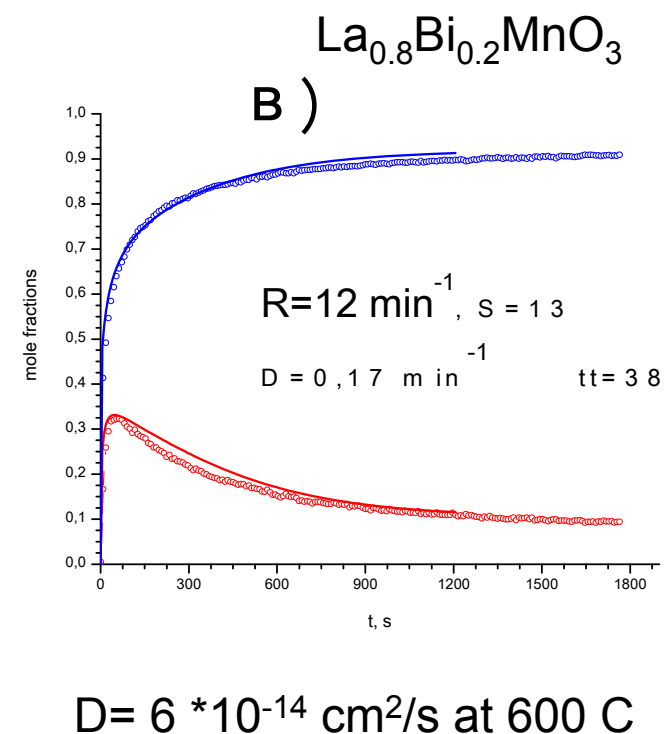
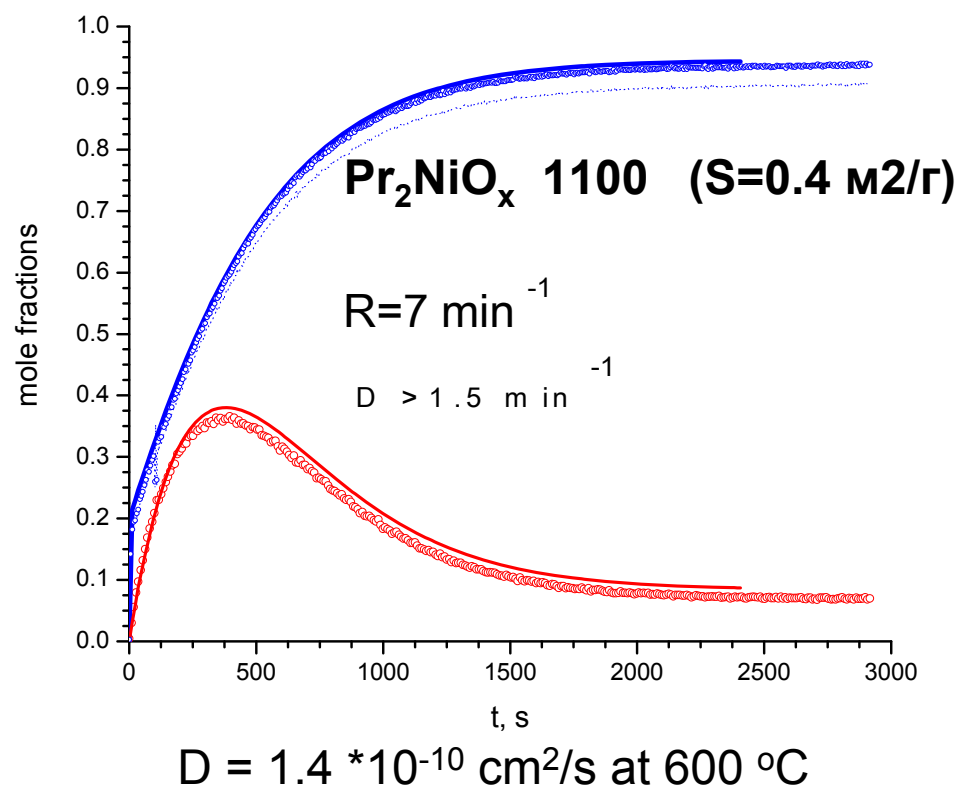
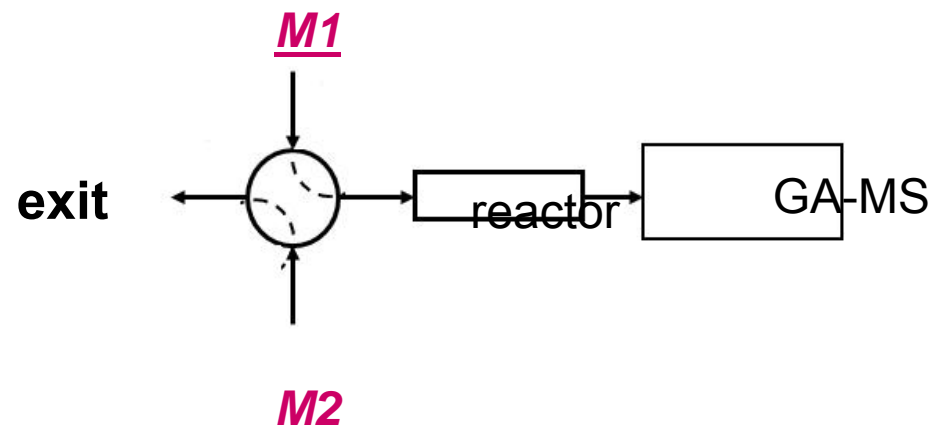
Scale of surface reactivity by the rate of oxygen heteroexchange



Variation of specific reactivity by two order of magnitude for perovskites
 Much lower reactivity of surface sites for electrolytes, especially doped zirconia

SSITKA (powders, flow reactor)

M1 - 1 % $^{16}\text{O}_2$ in He,
M2 - 1% $^{18}\text{O}_2$ or 1% $^{18}\text{CO}_2$ in He, plug flow reactor, contact time 0.01 s, 600-800 °C



SSITKA set of equations

$$c_{\text{O}_2} \left(\frac{\partial \alpha_g}{\partial t} + \frac{1}{\tau} \frac{\partial \alpha_g}{\partial \xi} \right) = -b \left(0.5 R^1 + R^2 \right) (\alpha_g - \alpha_s),$$

$$c_{\text{O}_2} \left(\frac{\partial f_{34}}{\partial t} + \frac{1}{\tau} \frac{\partial f_{34}}{\partial \xi} \right) = b R^0 (2\alpha_g (1 - \alpha_g) - f_{34})$$

$$+ b R^1 (\alpha_g (1 - \alpha_s) + \alpha_s (1 - \alpha_g) - f_{34})$$

$$+ b R^2 (2\alpha_s (1 - \alpha_s) - f_{34}),$$

$$\frac{\partial \alpha_s}{\partial t} = (0.5 R^1 + R^2) (\alpha_g - \alpha_s) - \frac{N_{\text{bulk}}}{N_s} \frac{D}{h^2} \frac{\partial \alpha_{\text{bulk}}}{\partial \eta} \bigg|_{\eta=0}$$

$$\frac{\partial \alpha_{\text{Obulk}}}{\partial t} = \frac{D}{h^2} \frac{\partial^2 \alpha_{\text{Obulk}}}{\partial \eta^2}.$$

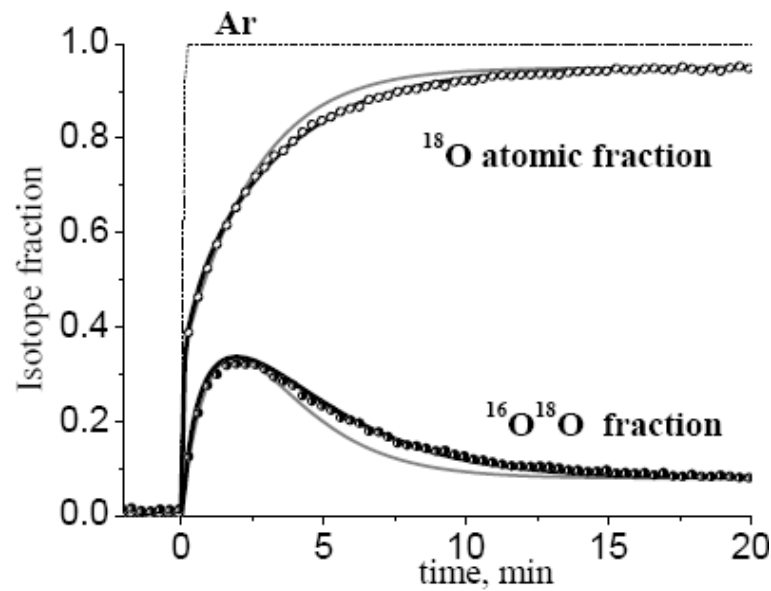
The initial and boundary conditions:

$$t = 0: \quad \alpha_g = 0, \quad f_{34} = 0, \quad \alpha_s = 0, \quad \alpha_{\text{bulk}} = 0,$$

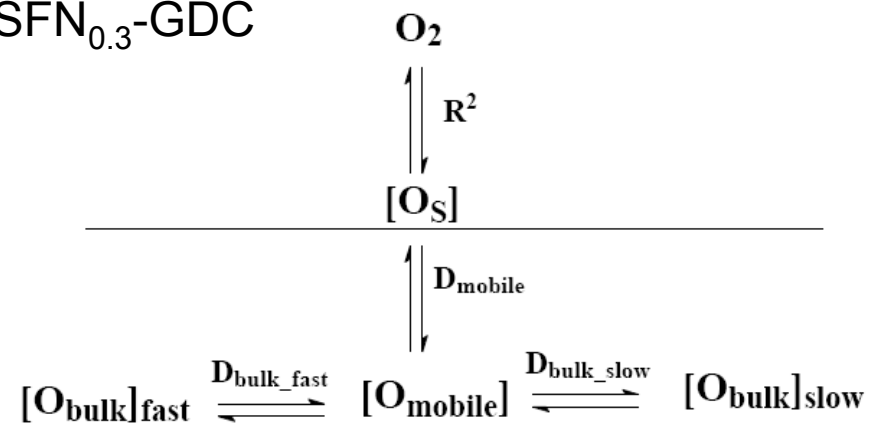
$$\xi = 0: \quad \alpha_g = \alpha_g^{\text{input}}, \quad f_{34} = f_{34}^{\text{input}},$$

$$\eta = 0: \quad \alpha_{\text{bulk}} = \alpha_s.$$

Oxygen isotope heteroexchange ($^{18}\text{O}_2$ SSITKA)



LSFN_{0.3}-GDC



T, °C	D_F , [cm ² /s]	D_P , [cm ² /s]	$D_\text{interface}$, [cm ² /s]
Nanocomposite			
600°C	$\geq 6 \times 10^{-14}$	2×10^{-14}	$\geq 1 \times 10^{-8}$
700°C	$\geq 30 \times 10^{-14}$	9×10^{-14}	$\geq 5 \times 10^{-8}$
Perovskite			
700		6×10^{-14}	$\geq 0.4 \times 10^{-8}$
Fluorite			
	$> 7 \times 10^{-14}$		$> 0.2 \times 10^{-8}$

Much faster oxygen diffusion along interfaces