

# CHEMICAL-KINETIC SIMPLIFICATIONS FOR LEAN HYDROGEN DEFLAGRATION

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Detailed Chemistry; Crossover  
Reaction Rates; Falloff  
Explosion Limits; Burning Velocities  
Autoignition Comparisons  
Steady States; Partial Equilibria  
Five-Step Autoignition Description  
Four-Step Global Reduction for Flames  
Seven-Step Lean-Deflagration Description  
One-Step Global Reduction for Lean Deflagration  
General Three-Step Global Reduction

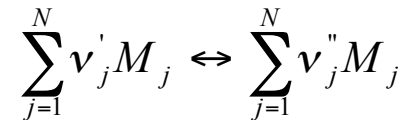
# HISTORY

C.N. Hinshelwood and A.T. Williams, 1934, “The Reaction Between Hydrogen and Oxygen”, Oxford University Press

R.N. Pease, 1956, “As many as a dozen individual steps (elementary reactions) have been assumed to contribute to the over-all [hydrogen oxidation] process.”

San Diego Mech, 2006, <http://www.mae.ucsd.edu/combustion/cermech> - 21 reversible elementary reactions

# ELEMENTARY REACTIONS



Bimolecular  $\sum_{j=1}^N \nu_j' = 2$

Trimolecular  $\sum_{j=1}^N \nu_j' = 3$

Reaction Rate (moles/volume time)

$$\omega = k_f \prod_{j=1}^N c_j^{\nu_j'} - k_b \prod_{j=1}^N c_j^{\nu_j''}$$

Equilibrium Constant  $K = k_f / k_b$

Tabulate  $k_f$  and Calculate  $k_b = k_f / K$

Three-Parameter Arrhenius

$$k = AT^n e^{-E/R^0T}$$

## THE DETAILED SAN DIEGO MECHANISM AND THE ASSOCIATED RATE PARAMETERS

Different mechanisms have different rate parameters and some different steps, but the predictions are qualitatively the same. No other current detailed mechanisms have fewer steps or simpler rate expressions or agree better with available experiments.

<sup>a</sup>Specific reaction-rate constant:

$$k = AT^n \exp(-E/RT)$$

All steps are reversible.

Equilibrium constants give reverse rates.

Units of rate parameters are mol/cm<sup>3</sup>, 1/s, K, kJ/mol; N<sub>2</sub> is the chaperon; there are efficiencies for other chaperons; falloff is Troe for steps 10 and 16, 10 with F<sub>c</sub>=0.5, 16 more complicated.

Reaction		<u>A<sup>a</sup></u>	<u>n<sup>a</sup></u>	E <sup>a</sup>
Hydrogen-oxygen chain				
1. H + O <sub>2</sub> → OH + O		3.52×10 <sup>16</sup>	-0.7	71.4
2. H <sub>2</sub> + O → OH + H		5.06×10 <sup>4</sup>	2.7	26.3
3. H <sub>2</sub> + OH → H <sub>2</sub> O + H		1.17×10 <sup>9</sup>	1.3	15.2
4. H <sub>2</sub> O + O → OH + OH		7.60×10 <sup>0</sup>	3.8	53.4
Direct recombination				
5. H + H + M → H <sub>2</sub> + M		1.30×10 <sup>18</sup>	-1.0	0.0
6. H + OH + M → H <sub>2</sub> O + M		4.00×10 <sup>22</sup>	-2.0	0.0
7. O + O + M → O <sub>2</sub> + M		6.17×10 <sup>15</sup>	-0.5	0.0
8. H + O + M → OH + M		4.71×10 <sup>18</sup>	-1.0	0.0
9. O + OH + M → HO <sub>2</sub> + M		8.00×10 <sup>15</sup>	0.0	0.0
Hydroperoxyl reactions				
10. H + O <sub>2</sub> + M → HO <sub>2</sub> + M	k <sub>0</sub>	5.75×10 <sup>19</sup>	-1.4	0.0
	k <sub>∞</sub>	4.65×10 <sup>12</sup>	0.4	0.0
11. HO <sub>2</sub> + H → OH + OH		7.08×10 <sup>13</sup>	0.0	1.2
12. HO <sub>2</sub> + H → H <sub>2</sub> + O <sub>2</sub>		1.66×10 <sup>13</sup>	0.0	3.4
13. HO <sub>2</sub> + H → H <sub>2</sub> O + O		3.10×10 <sup>13</sup>	0.0	7.2
14. HO <sub>2</sub> + O → OH + O <sub>2</sub>		2.00×10 <sup>13</sup>	0.0	0.0
15. HO <sub>2</sub> + OH → H <sub>2</sub> O + O <sub>2</sub>		2.89×10 <sup>13</sup>	0.0	-2.1
Hydrogen peroxide reactions				
16. OH + OH + M → H <sub>2</sub> O <sub>2</sub> + M	k <sub>0</sub>	2.30×10 <sup>18</sup>	-0.9	-7.1
	k <sub>∞</sub>	7.40×10 <sup>13</sup>	-0.4	0.0
17. HO <sub>2</sub> + HO <sub>2</sub> → H <sub>2</sub> O <sub>2</sub> + O <sub>2</sub>		3.02×10 <sup>12</sup>	0.0	5.8
18. H <sub>2</sub> O <sub>2</sub> + H → HO <sub>2</sub> + H <sub>2</sub>		4.79×10 <sup>13</sup>	0.0	33.3
19. H <sub>2</sub> O <sub>2</sub> + H → H <sub>2</sub> O + OH		1.00×10 <sup>13</sup>	0.0	15.0
20. H <sub>2</sub> O <sub>2</sub> + OH → H <sub>2</sub> O + HO <sub>2</sub>		7.08×10 <sup>12</sup>	0.0	6.0
21. H <sub>2</sub> O <sub>2</sub> + O → HO <sub>2</sub> + OH		9.63×10 <sup>6</sup>	2.0	2.0

# FALLOFF

The Form of the Falloff Expression is due to Troe.

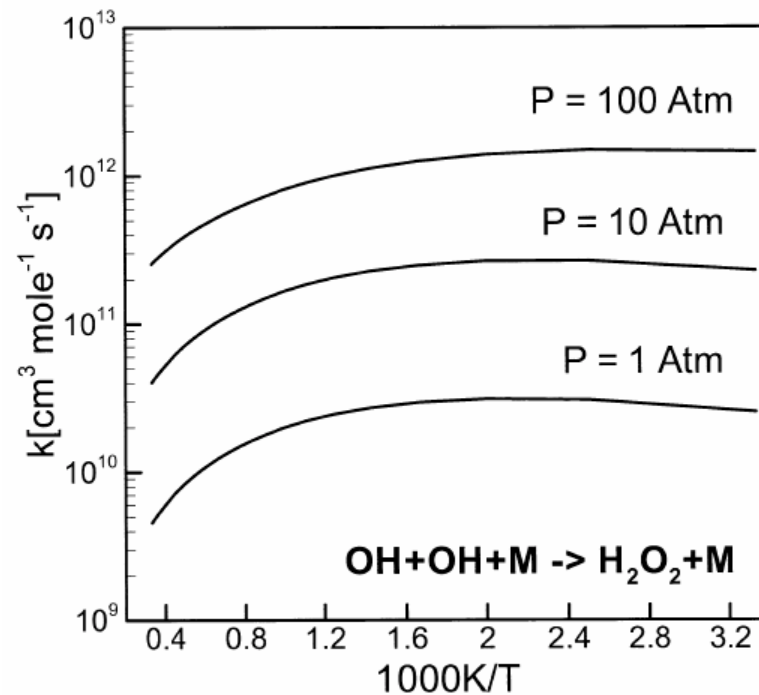
Troe Falloff: 3'rd-body concentration is  $c_M = \sum_{j=1}^N \eta_j c_j$

$$k = \frac{k_\infty k_0 c_M}{k_\infty + k_0 c_M} F_c^{\{1 + [(0.75 - 1.27 \log F_c)^{-1} \log(k_0 c_M / k_\infty)]^2\}^{-1}}$$

$$F_c = a e^{-T/T_1} + (1 - a) e^{-T/T_2} + b e^{-T_3/T} \quad (b = 0, 1)$$

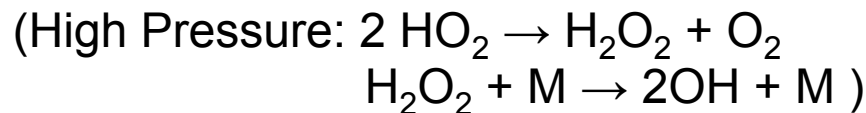
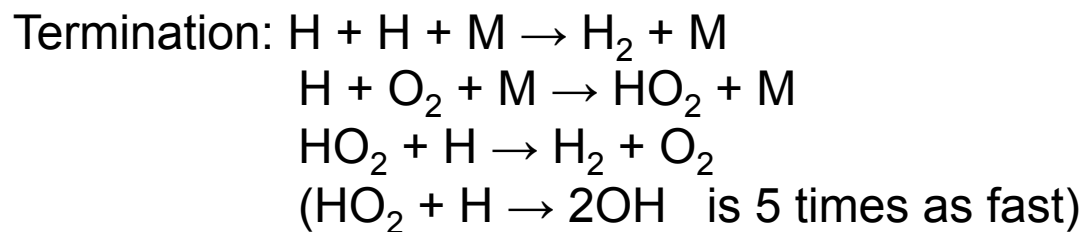
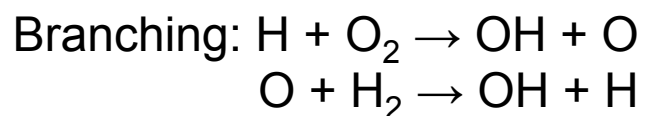
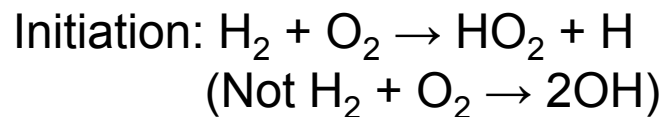
Eleven Parameters; Three in each  $k$ , three  $T$ 's,  $a$  and  $b$ ..

Inconsistent with Temperature-Dependent Chaperon Efficiencies,  $\eta_j$  .



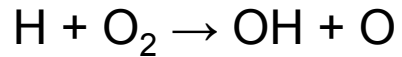
The dependence of the specific reaction-rate constant on temperature at three different pressures, for step 16 of Table 1,  $\text{OH} + \text{OH} + \text{M} \rightarrow \text{H}_2\text{O}_2 + \text{M}$  expressed in bimolecular form (that is, the plot shows  $k c_M$  for the trimolecular form).

# CHAIN MECHANISM



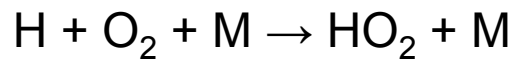
# CROSSOVER

Branching Step:



Rate Increases with Temperature

Termination Step:

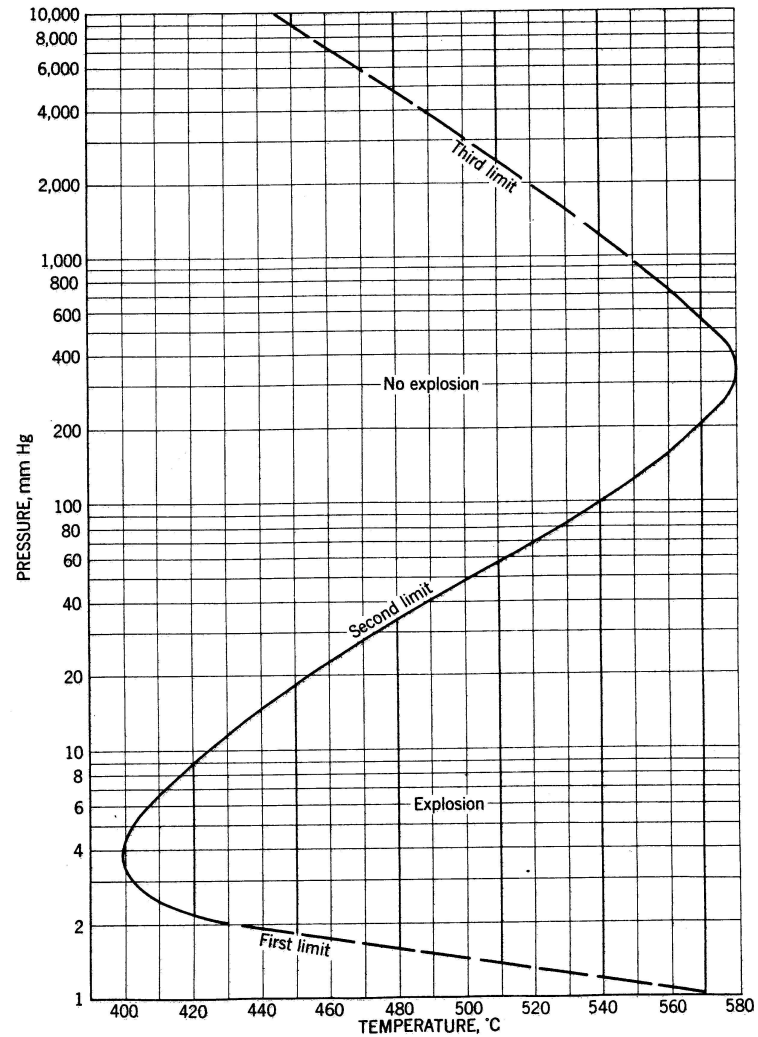


Rate Independent of Temperature

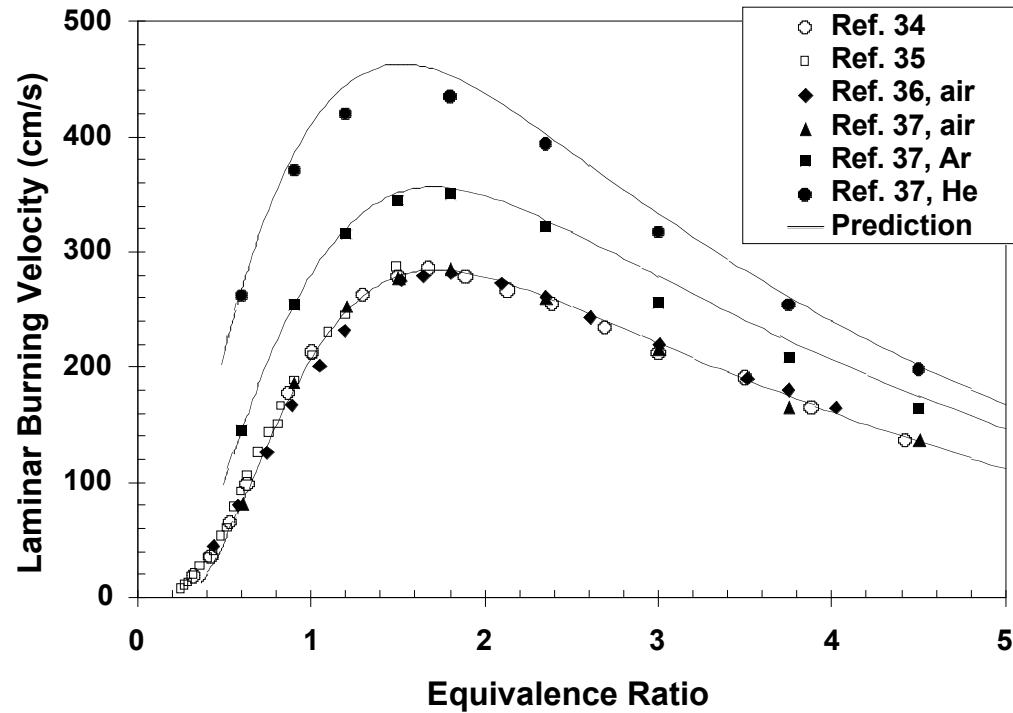
Rates Equal at Crossover Temperature

~ 1000 K at 1 bar, 1500 K at 50 bar.





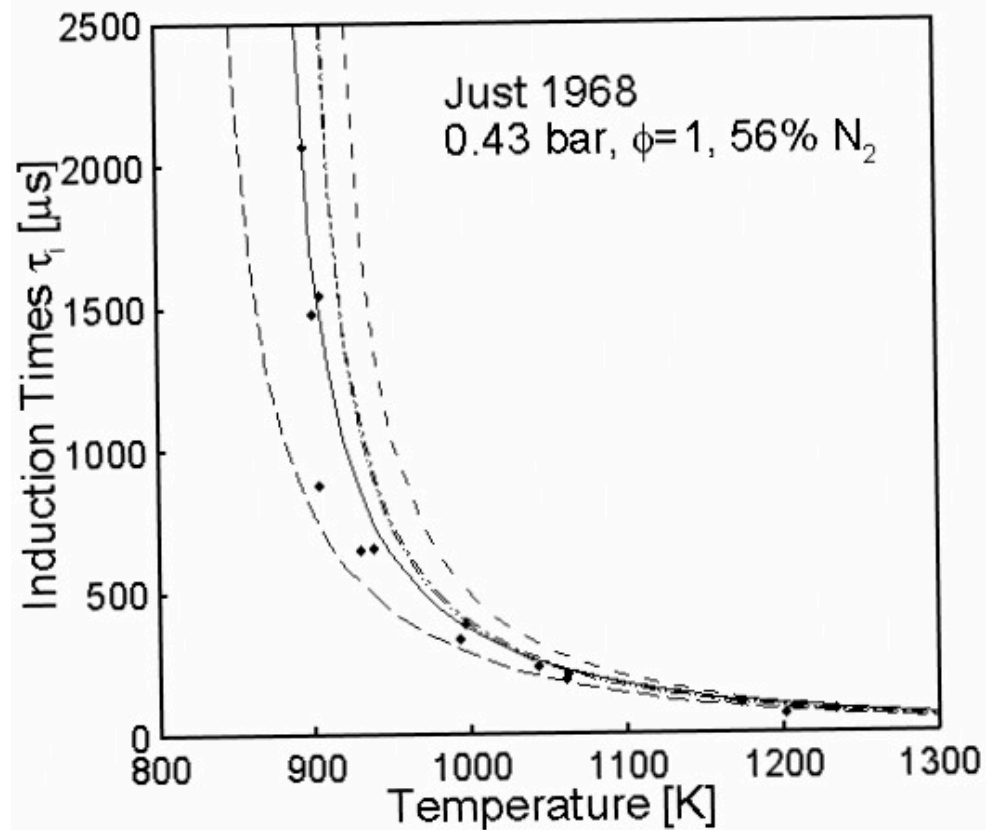
Explosion limits for stoichiometric mixtures of hydrogen and oxygen in a spherical vessel, 7.4 cm in diameters, with its interior surface coated with potassium chloride (explosion is defined as observing that reaction occurs after the mixture is admitted to the vessel at the specified temperature and pressure).



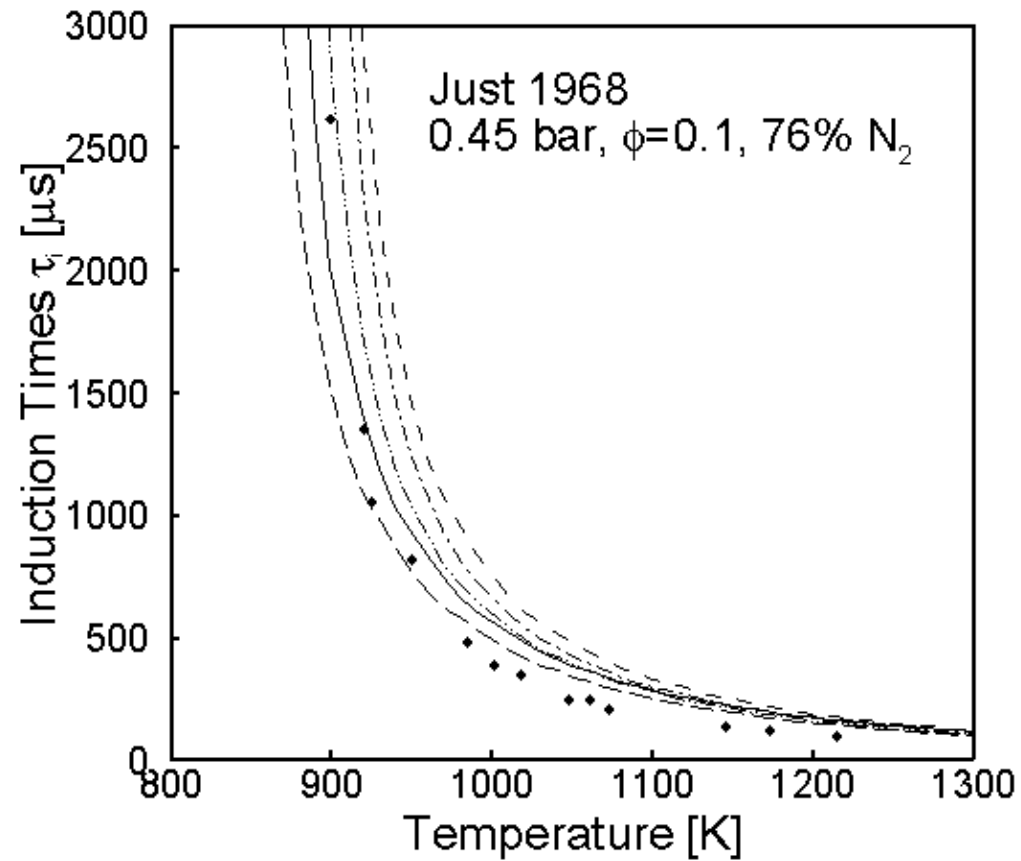
Comparisons of predicted laminar burning velocities with experiment, as a function of the equivalence ratio (the fuel-air ratio divided by the stoichiometric fuel-air ratio for  $2\text{H}_2 + \text{O}_2 \rightarrow 2\text{H}_2\text{O}$ ), at 1 atm and initially 298 K, with a ratio of the oxygen concentration to the sum of the oxygen and inert concentrations of 0.214 (corresponding to air), for inerts being nitrogen, argon and helium.

**LITERATURE ON SHOCK-TUBE MEASUREMENTS OF HYDROGEN-OXYGEN INDUCTION TIMES**

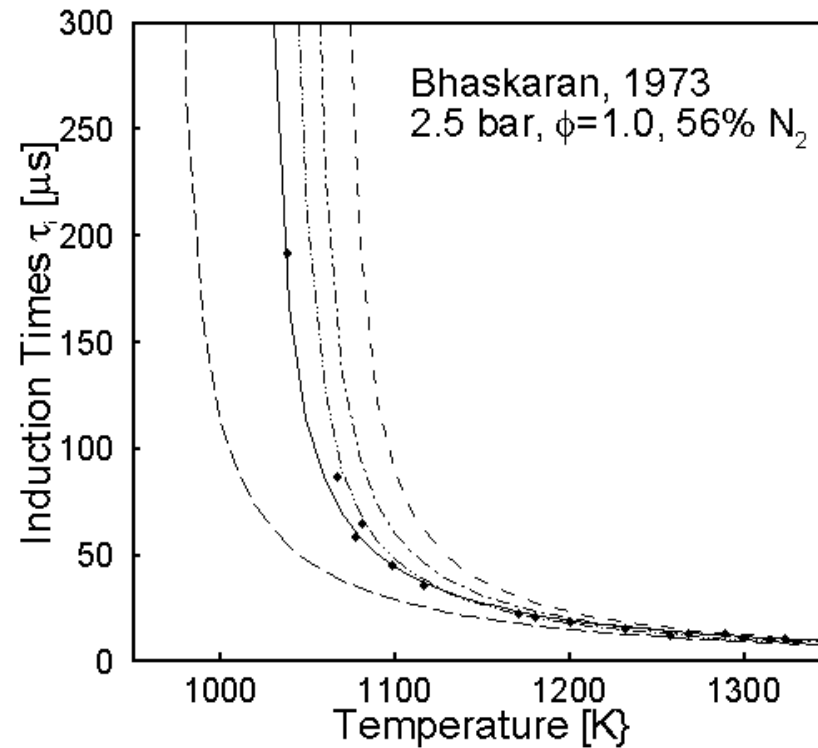
First author	Technique	Diluent%	$\phi$	P(bar)	T(K)	Induction Period End
Steinberg (1955)	Reflected	-	1	4.5-9	700-1000	Light emission onset
Schott (1958)	Incident and Reflected	Ar 75-99%	0.125-9	0.15-9.5	1050-2650	OH absorption onset
Strehlow (1962)	Reflected	Ar 25-94%	1	0.026-0.052	920-1820	Pressure inflection
Fujimoto (1963)	Reflected	Ar 70%	1	0.88-2.7	800-1400	Pressure inflection and light emission onset
Miyama (1964)	Reflected	Ar 70-90%	0.25-1	4.5-5.6	890-1350	OH absorption onset and pressure rise
Asaba (1965)	Incident	Ar 96-99%	0.085-1.5	0.2-0.5	1400-2400	OH absorption and emission onset
Belles (1965)	Incident	N <sub>2</sub> 63-75%	0.125-0.595	0.1-0.5	1100-1900	OH emission maximum and UV emission onset
Skinner (1965)	Reflected	Ar 90%	2	5	900-1100	OH emission maximum
Snyder (1965)	Reflected	N <sub>2</sub> 55-65%	0.5-1	1.0-9.0	800-1100	Pressure inflection and UV emission onset
Voevodsky (1965)	Reflected	-	0.5	0.5-4.0	800-1700	Pressure inflection and UV emission onset
White (1965)	Incident and Reflected	Ar 0-33%	0.0037-50	0.04-0.12	1100-2200	Inflection of density profiles
Craig (1966)	Reflected	N <sub>2</sub> 55%	1	1.0-2.0	875-1000	OH emission onset
Cohen (1967)	Reflected	Ar 0-94%	1.0-2.0	0.25-8.3	900-1650	Pressure maximum and UV emission and absorption
Just (1968)	Reflected	N <sub>2</sub> 55-76%	0.1-1.0	0.4-1.4	900-1250	Light Emission Onset
Jachimowski (1971)	Incident	Ar 91-95%	0.063-2	0.2-0.75	1200-1800	OH absorption at 5% of Maximum
Bhaskaran (1973)	Reflected	N <sub>2</sub> 55%	1	2.5	800-1400	Pressure inflection and Light Emission Onset
Cheng (1977)	Reflected	Ar 90%	0.5-1	1.0-3.0	1000-1800	Pressure inflection
Blumenthal (1996)	Reflected	N <sub>2</sub> 67%	0.42	3-50	700-1200	OH emission onset and pressure inflection
Petersen (1996)	Reflected	Ar 97-99.9%	1	33-87	1100-1900	Inflection of OH absorption
Wang (2003)	Reflected	N <sub>2</sub> 10-18%, Steam 0-40%	0.42	3.0-5.0	1100-1400	Inflection of OH absorption



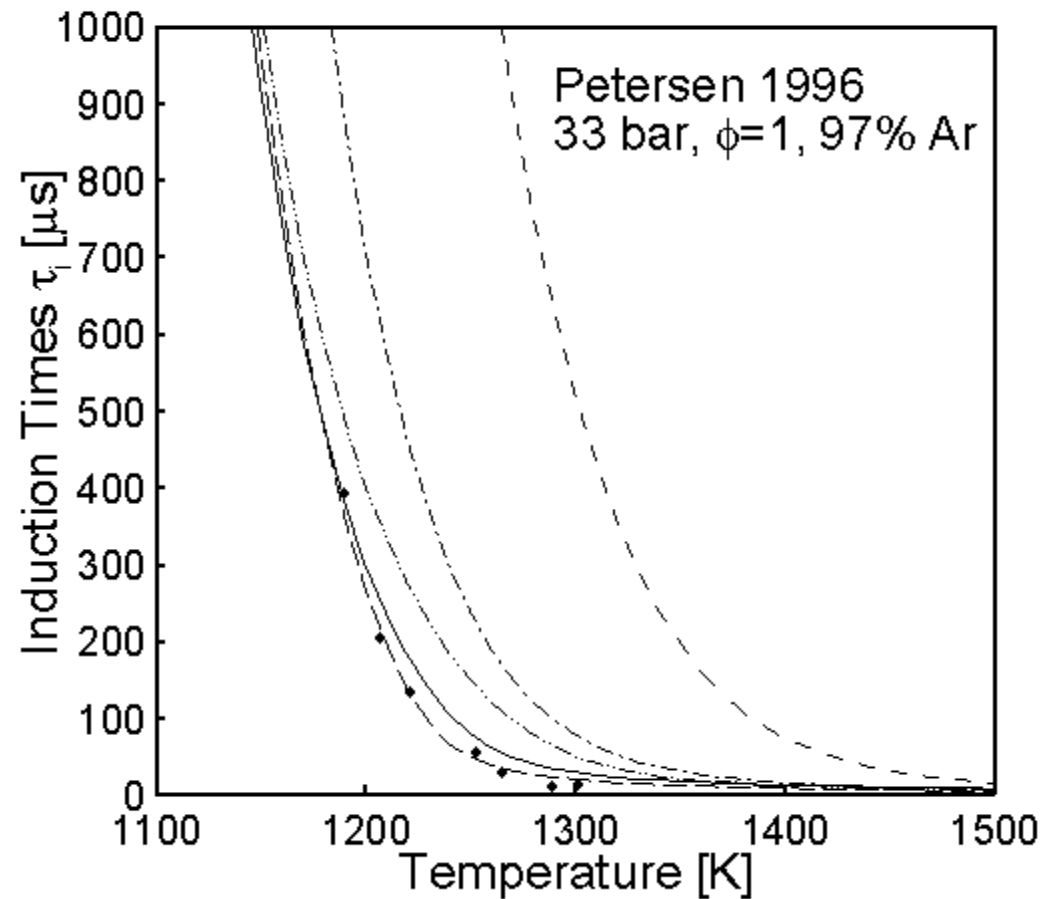
Variation with temperature of the induction time as obtained from detailed-chemistry numerical calculations (solid curve [23], short-dashed curve [11], long-dashed curve [20], dot-dashed curve [15], dot-dot-dashed curve [18]) and from shock-tube experimental results [52] ( $p = 0.43$  bar,  $f = 1$ , solid points).



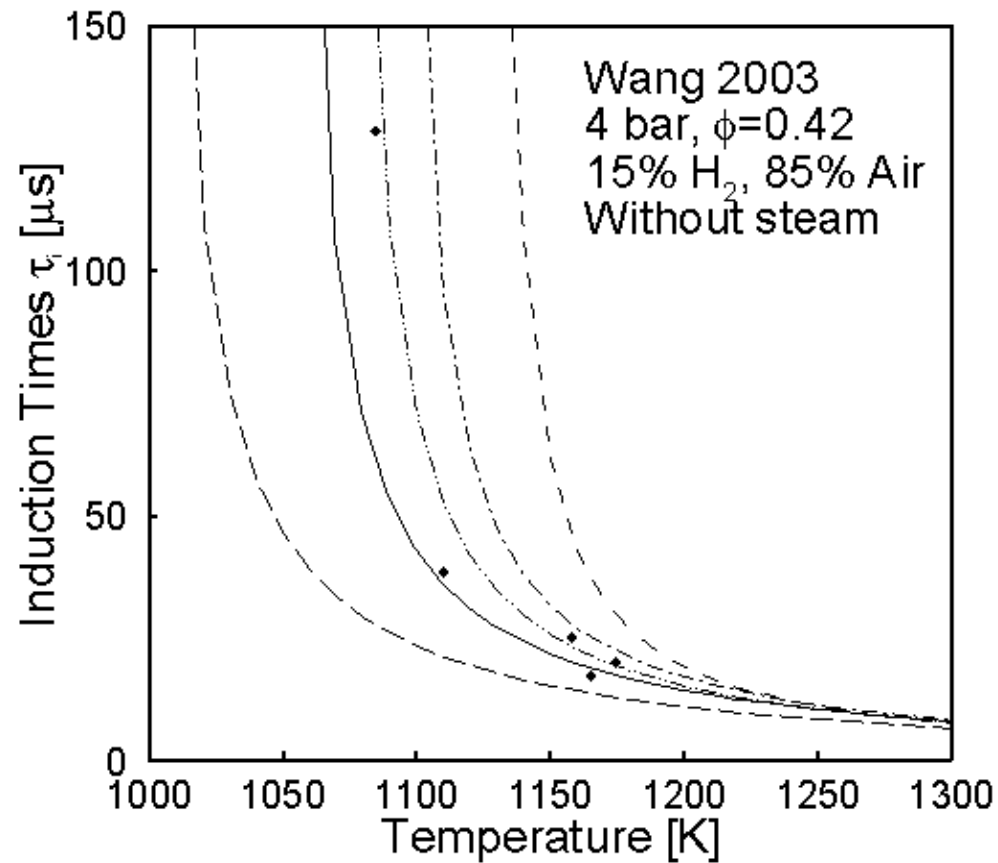
Variation with temperature of the induction time as obtained from detailed-chemistry numerical calculations (solid curve [23], short-dashed curve [11], long-dashed curve [20], dot-dashed curve [15], dot-dot-dashed curve [18]) and from shock-tube experimental results [52] ( $p = 0.45$  bar,  $f = 0.1$ , solid points).



Variation with temperature of the induction time as obtained from detailed-chemistry numerical calculations (solid curve [23], short-dashed curve [11], long-dashed curve [20], dot-dashed curve [15], dot-dot-dashed curve [18]) and from shock-tube experimental results [54] ( $p = 2.5$  bar,  $f = 1$ , solid points).

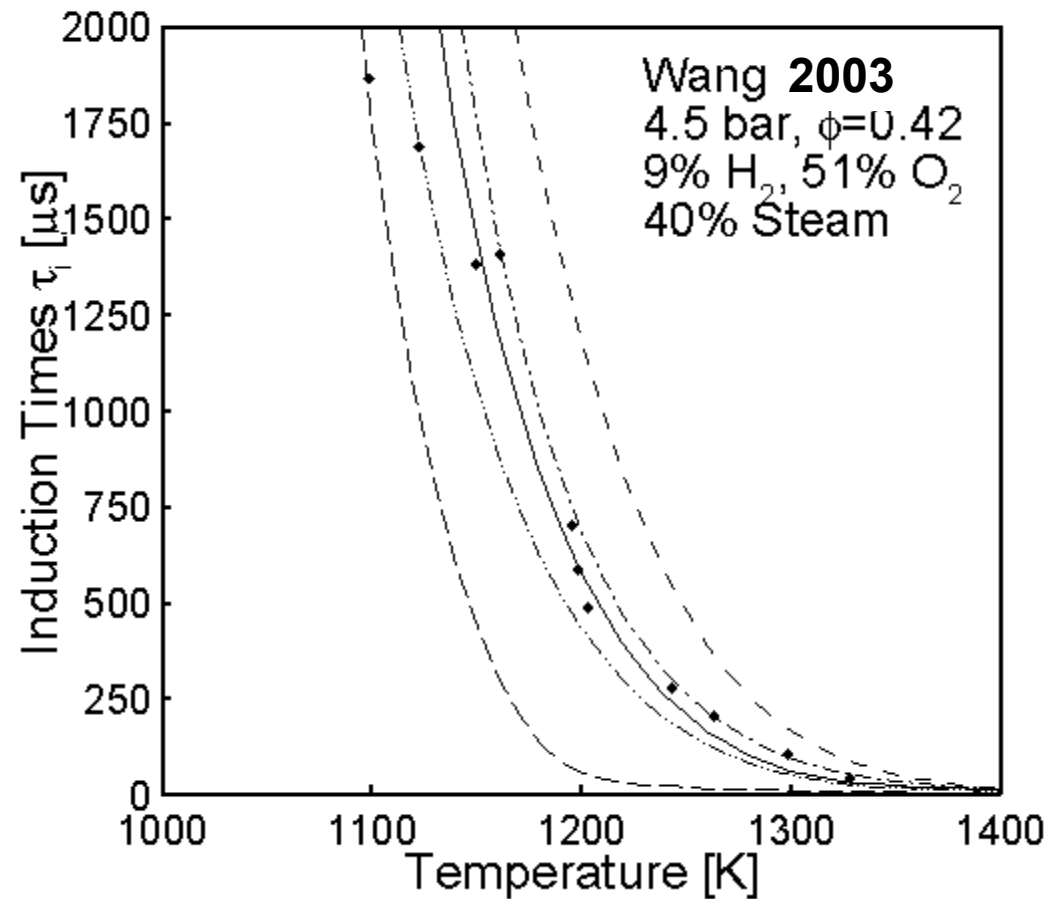


Variation with temperature of the induction time as obtained from detailed-chemistry numerical calculations (solid curve [23], short-dashed curve [11], long-dashed curve [20], dot-dashed curve [15], dot-dot-dashed curve [18]) and from shock-tube experimental results [58] ( $p = 33$  bar,  $f = 1$ , solid points).

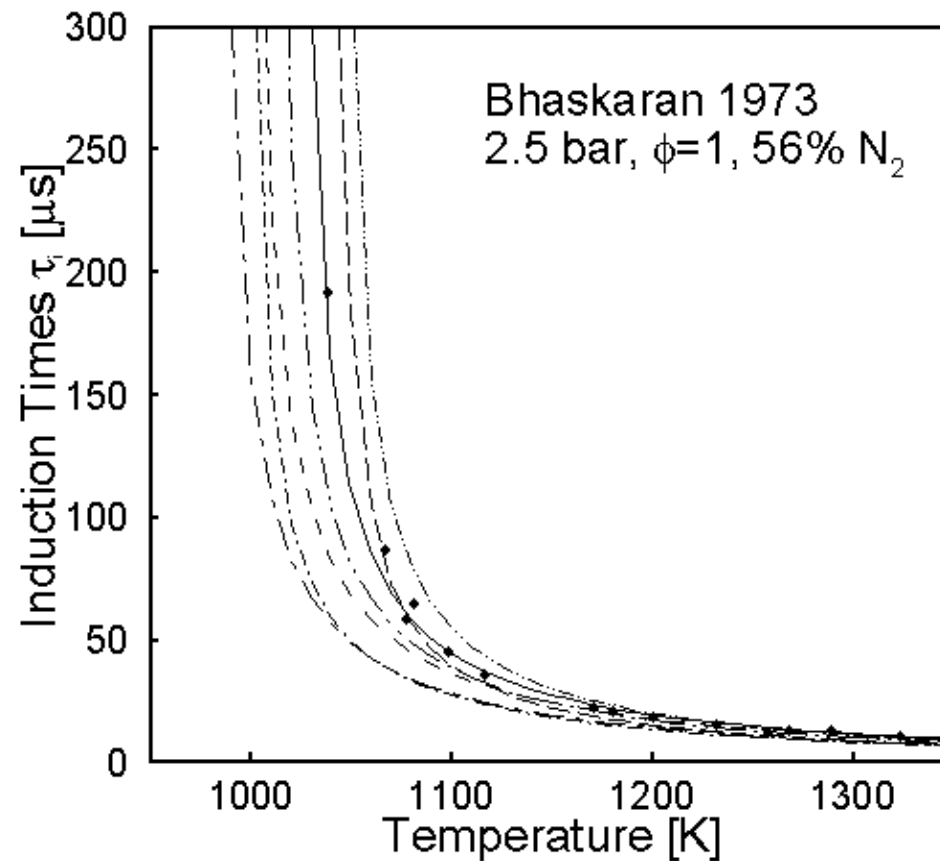


Variation with temperature of the induction time as obtained from detailed-chemistry numerical calculations (solid curve [23], short-dashed curve [11], long-dashed curve [20], dot-dashed curve [15] version 3.0, dot-dot-dashed curve [18]) and from shock-tube experimental results [59] ( $p = 3-5$  bar,  $f = 0.42$ , without steam, solid points).





Variation with temperature of the induction time as obtained from detailed-chemistry numerical calculations (solid curve [23], short-dashed curve [11], long-dashed curve [20], dot-dashed curve [15], dot-dot-dashed curve [18]) and from shock-tube experimental results [59] ( $p = 3-5$  bar,  $f = 0.42$ , 40% steam, solid points).



Variation with temperature of the induction time as obtained from detailed-chemistry numerical calculations (solid curve [23], short-dashed curve [15] version 2.11, long-dashed curve [16], long-dot-dashed curve [17], short-dot-dashed curve [12], short-dash-dot-dot curve [19], long-dash-dot-dot curve [14]) and from shock-tube experimental results [54] ( $p = 2.5$  bar,  $f = 1$ , solid points).

# COMAPRISONS OF MECHANISMS

San Diego, Ranzi and Dryer are Equally Good

San Diego is the Smallest

GRI 2.11 Better than 3.0

More Details in Write-up.

# Reduced Chemistry

- The detailed chemistry often can be used in computations.
- For many of the more complicated problems, detailed chemistry is too long.
- Development of reduced chemistry also contributes to understanding.
- Systematic reduction leads to a small number of overall (global) steps.

# GLOBAL REDUCED MECHANISMS FOR HYDROGEN OXIDATION

Eight Species;  $H_2$ ,  $O_2$ ,  $H_2O$ ,  $H$ ,  $OH$ ,  $O$ ,  $HO_2$ ,  $H_2O_2$   
Minus Two Element (or atom) Conservation Equations  
Implies Only Six Independent Differential Equations with Nonzero Source Terms

∴ A 6-STEP GLOBAL MECHANISM EXISTS  
WITHOUT REDUCTION

Reduced chemistry therefore must seek fewer than six global steps.

# SPECIES CONSERVATION

$$L(Y_i) \equiv \rho \frac{\partial Y_i}{\partial t} + \rho \vec{v} \cdot \nabla Y_i + \nabla \cdot (\rho \vec{V}_i Y_i)$$

Mole Fraction:  $X_i \equiv c_i R^0 T / p$

Mass Fraction:  $Y_i = W_i X_i / \sum_{j=1}^N W_j X_j$

Conservation:  $L(Y_i) = W_i \sum_{k=1}^M (\nu_{ik}'' - \nu_{ik}') \omega_k$

Replace Differential Equations by Algebraic Equations through Steady-State and Partial-Equilibrium Approximations

# STEADY STATE

$$\sum_{k=1}^M v_{ik} \omega_k = \omega_{i+} - \omega_{i-} = 0$$

Solve Algebraic Equation for  $Y_i$

Error Measure:  $e_i = L(Y_i) / (W_i \omega_{i+})$

# PARTIAL EQUILIBRIUM

$$\omega_{k+} = \omega_{k-}$$

Solve Algebraic Equation for  $Y_i$

$$L(Y_i) = W_i \sum_{k=2}^M (v_{ik}'' - v_{ik}') \omega_k + \frac{v_{i1}}{v_{11}} \left[ L(Y_i) - W_i \sum_{k=2}^M (v_{ik}'' - v_{ik}') \omega_k \right]$$

∃ Generalizations; Truncation Needed

## GENERAL REDUCTION PROCEDURE

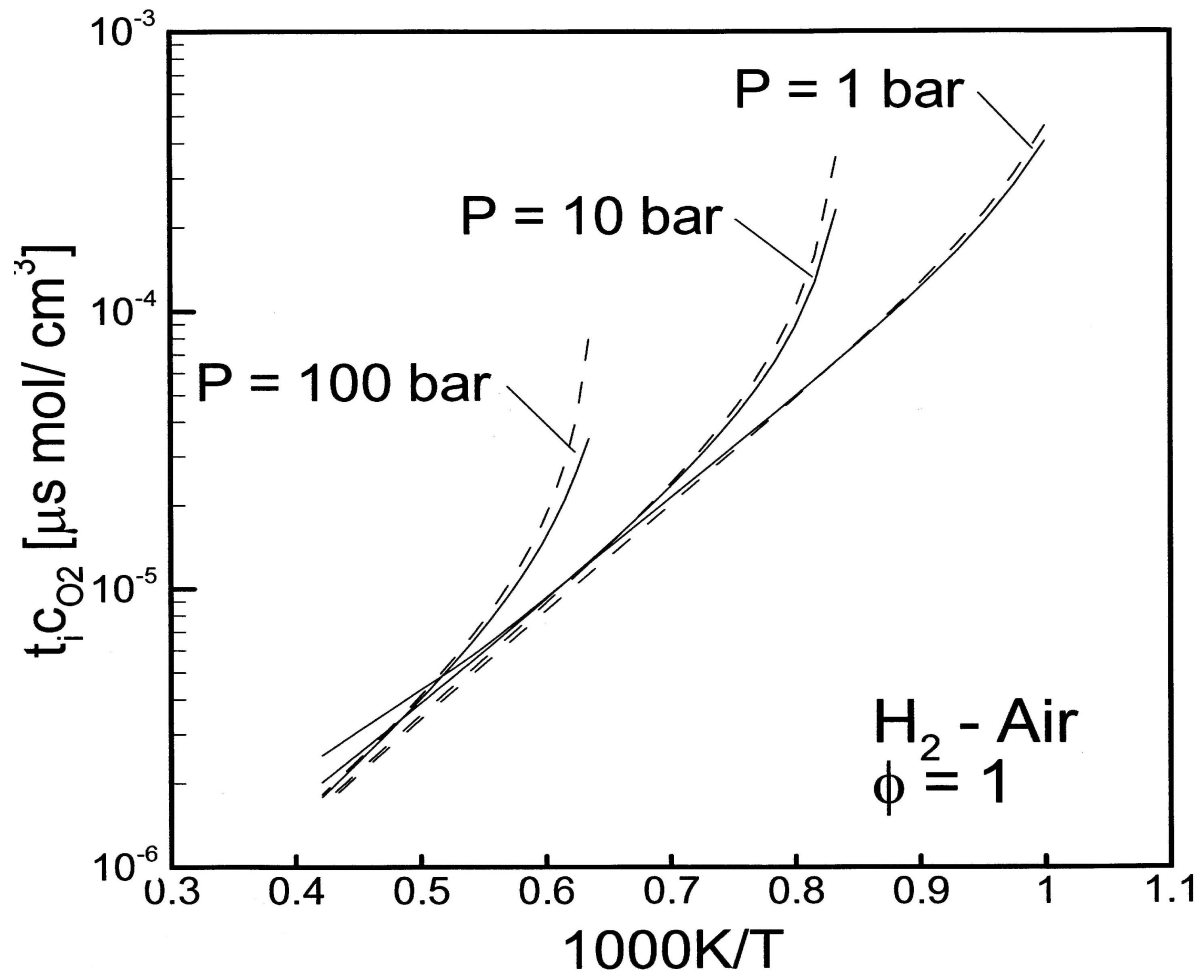
1. Delete irrelevant elementary steps.
2. Identify steady-state species.
3. Identify main chains for conversion of non-steady-state species.
4. Identify operable set of overall (global) reactions.
5. Simplify resulting rate formulas by truncation.
6. Test accuracies of steady states and truncations.
7. Revise if necessary and identify limitations of final mechanism.



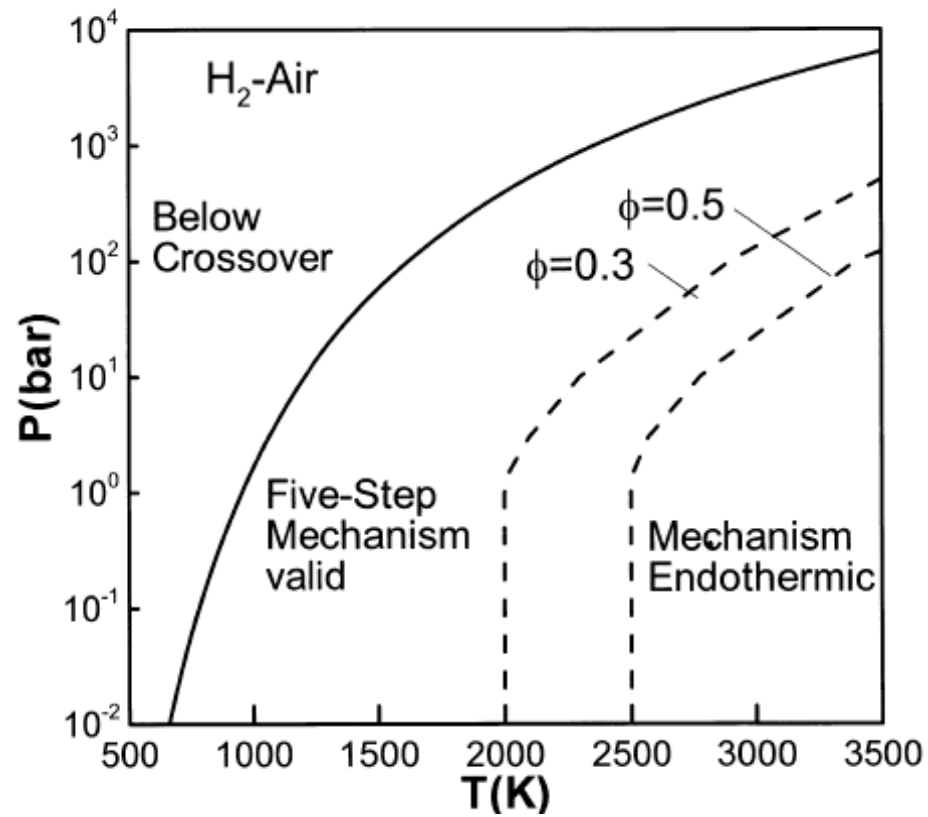
# FIVE-STEP AUTOIGNITION MECHANISM

Table 3

Number	Reaction	Step in Table 1
1	$\text{H}_2 + \text{O}_2 \rightarrow \text{HO}_2 + \text{H}$	Step 12 backward
2	$\text{H} + \text{O}_2 \rightarrow \text{OH} + \text{O}$	Step 1 forward
3	$\text{O} + \text{H}_2 \rightarrow \text{OH} + \text{H}$	Step 2 forward
4	$\text{OH} + \text{H}_2 \rightarrow \text{H}_2\text{O} + \text{H}$	Step 3 forward
5	$\text{H} + \text{O}_2 + \text{M} \rightarrow \text{HO}_2 + \text{M}$	Step 10 forward



The temperature dependence of the product of the ignition time and the oxygen concentration for stoichiometric hydrogen-air mixtures at three different pressures according to the temperature-inflection criterion, for the detailed mechanism of Table 1 (solid curves) and for the reduced mechanism of Table 3 (dashed curves).

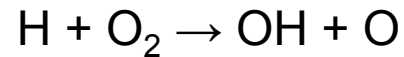


Estimated region of validity, in a pressure-temperature plane, for autoignition-time predictions by the five-step mechanism for hydrogen-air mixtures.

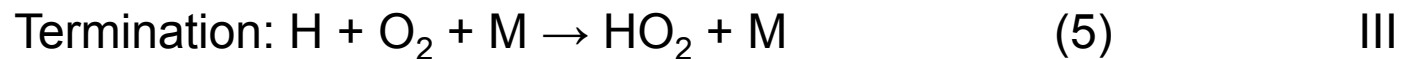
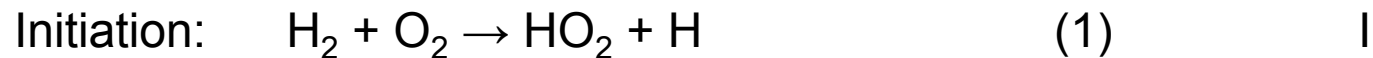
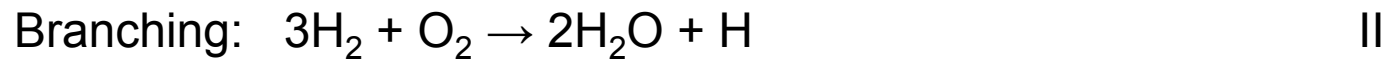
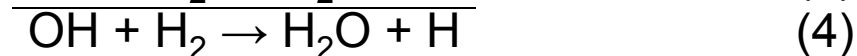
# AUTOIGNITION

Very lean: H steady state

Stoichiometric and rich: O and OH steady state



(2)



A three-step global reduced mechanism

$$\omega_{II} = k_2 c_H c_{O_2} \quad , \quad \omega_I = k_1 c_{H_2} c_{O_2} \quad , \quad \omega_{III} = k_5 c_H c_{O_2} c_M$$

# IGNITION-TIME CRITERIA

## 1. Partial Equilibrium of $\text{H} + \text{O}_2 \rightarrow \text{OH} + \text{O}$ with Reactant Depletion Neglected

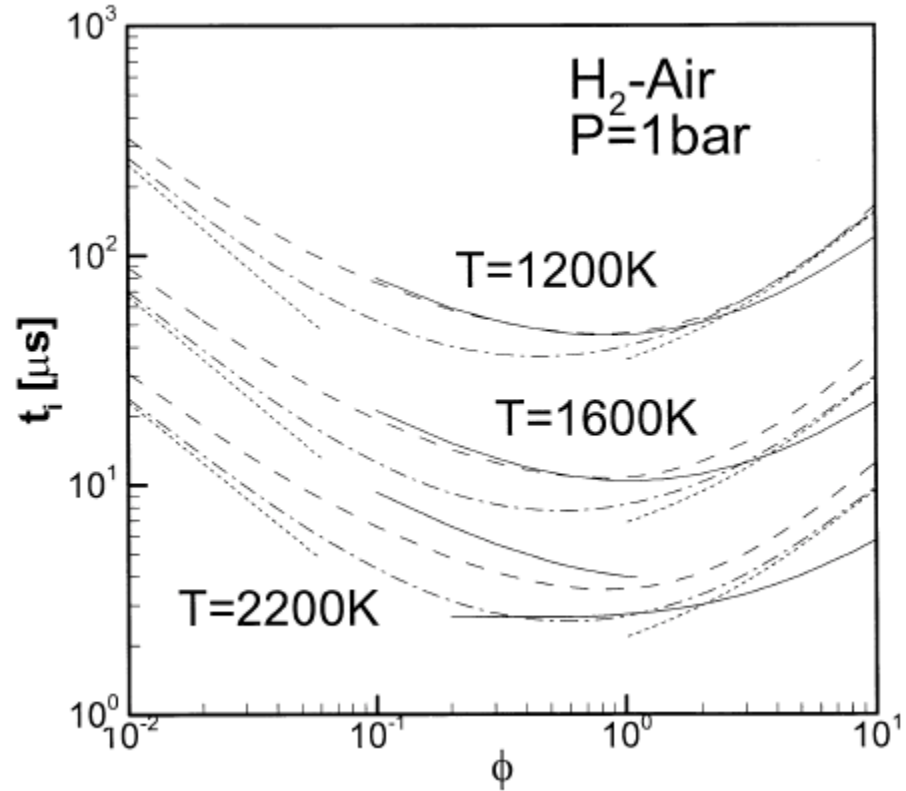
$$t_R = \frac{1}{(2k_2 - k_5c_M)c_{O_2}} \ln \left[ \frac{K_2 k_3 k_1 (2k_2 - k_5c_M)c_{H_2}}{2k_1 k_2^2 c_{O_2}} \right]$$

$$t_L = \text{More Messy.} \quad t_i = t_R + t_L$$

## 2. Thermal Runaway for Large Activation Energy of Branching Step 2

$$t_i = \frac{1}{(2k_2 - k_5c_M)c_{O_2}} \left\{ \ln \left[ \frac{k_2(1-c)^2}{k_1\theta_2(q_2 + cq_5)} \right] - (1-c)K(b,c) \right\}$$

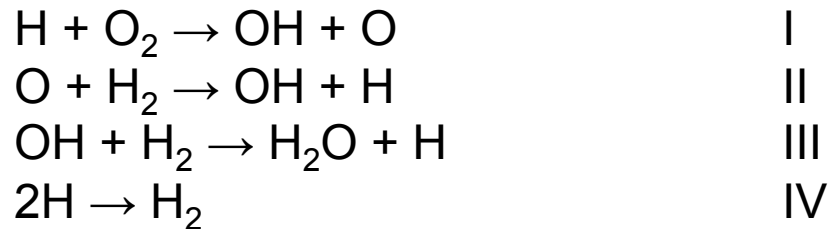
$$q_k = \frac{Q_k}{c_p T_0}, \quad \theta_2 = \frac{E_2}{R^0 T_0}, \quad b = \frac{Q_5}{Q_{II}}, \quad c = \frac{k_5 c_M}{2k_2}$$



Hydrogen-air autoignition times as functions of the equivalence ratio at 1 bar for three different temperatures.  
 Dot-dash curves from  $t_i = t_R + t_L$   
 Dashed curves from isothermal integration of detailed mechanism with 95% criterion 1.  
 Solid curves from adiabatic integration of detailed mechanism with temperature-inflection criterion.

# FOUR-STEP GLOBAL REDUCED MECHANISM FOR FLAMES

Neglect  $\text{H}_2\text{O}_2$  (15 Elementary Step)



$$\omega_I = \omega_1 - \omega_7 - \omega_9 - \omega_{11} + \omega_{13}$$

$$\omega_{II} = \omega_2 + \omega_4 + \omega_7 + \omega_8 + \omega_{11} + \omega_{14}$$

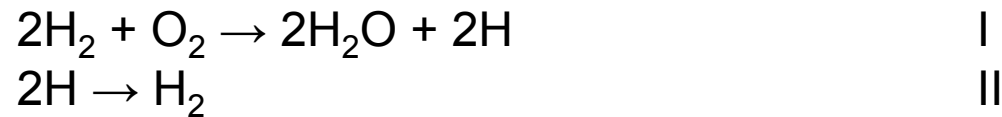
$$\omega_{III} = \omega_3 - \omega_4 + \omega_6 + \omega_{13} + \omega_{15}$$

$$\omega_{IV} = \omega_5 + \omega_6 + \omega_7 + \omega_8 + \omega_9 + \omega_{10}$$

# TWO-STEP GLOBAL MECHANISM FOR FLAMES

Put O and OH in Steady State as well

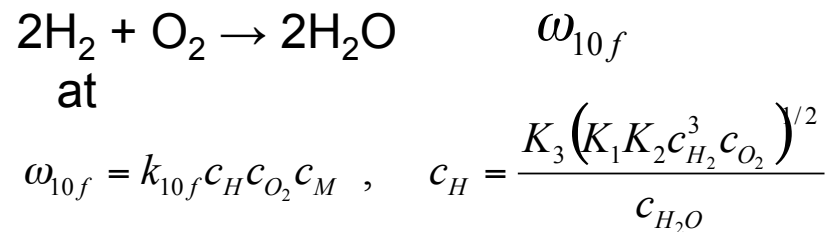
(Note: There are a number of three-step mechanisms)



$$\omega_I \approx \omega_{1f} \quad , \quad \omega_{II} \approx \omega_{10f} \left( \frac{\omega_{12f}}{\omega_{11f} + \omega_{12f}} \right)$$

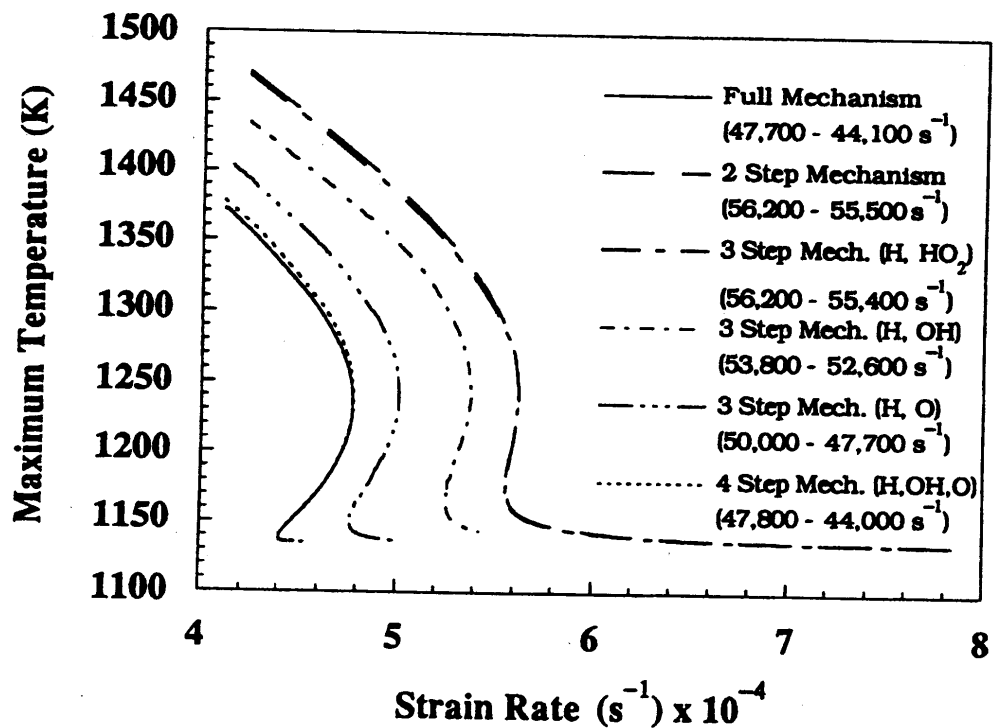
## ONE-STEP MECHANISM

Put H in Steady State as well



This is too slow unless H concentration is calculated correctly.





The maximum calculated temperature in the diffusion flame, as a function of the air-side strain rate, for a steady, axisymmetric counterflow flame between air at 1135 K and a molar mixture of 40% hydrogen and 60% nitrogen, according to the full mechanism of Table 1, the four-step mechanism, three different three-step mechanisms, and the two-step mechanism.

## TEN-STEP ( 7-STEP, 3 REVERSIBLE) DETAILED MECHANISM FOR LEAN HYDROGEN FLAMES

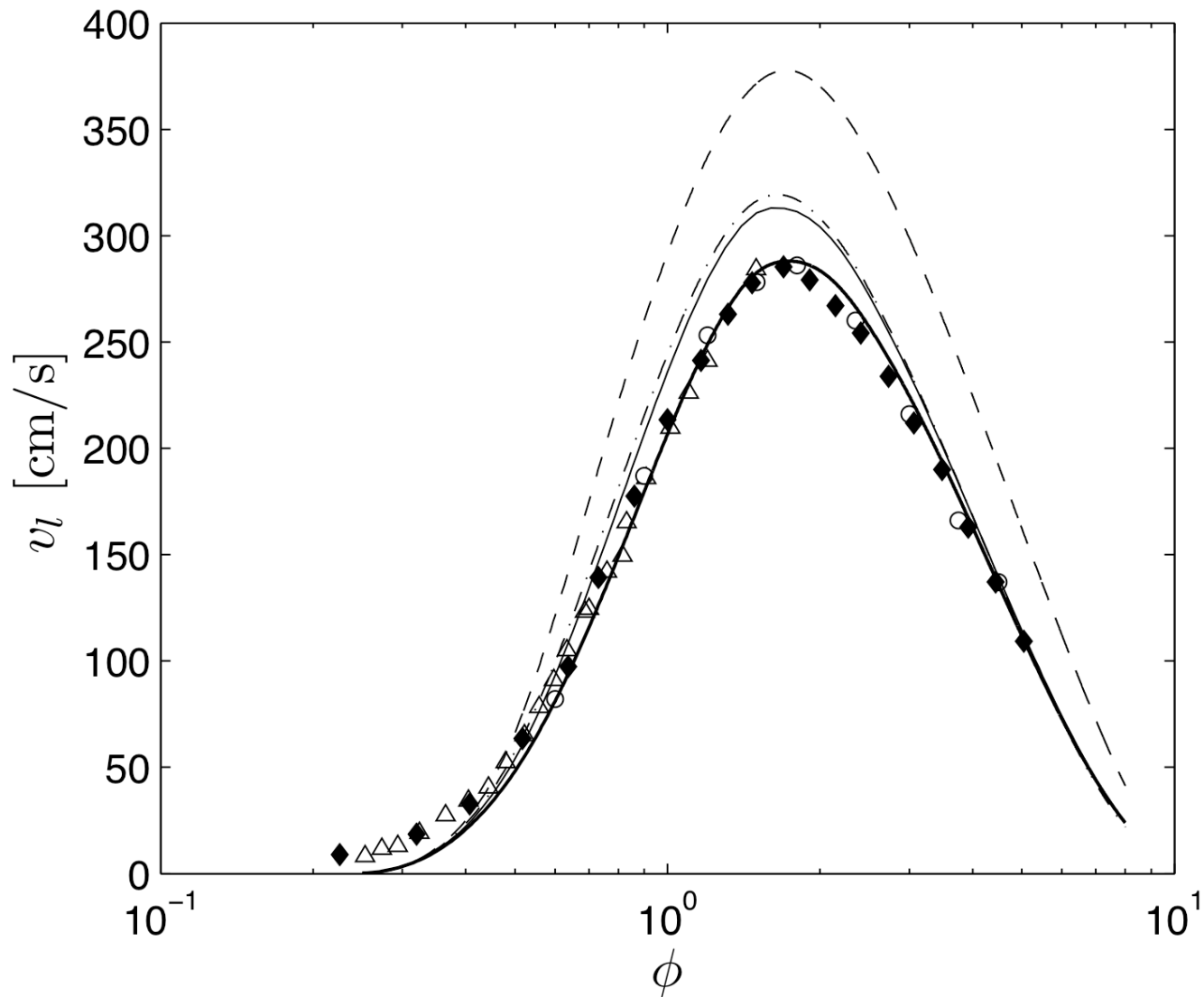
(1 bar, 300 K, equivalence ratio below 0.6)

Number	Reaction	Step in Table 1
1	$\text{H} + \text{O}_2 \begin{matrix} \rightarrow \\ \leftarrow \end{matrix} \text{OH} + \text{O}$	Step 1
2	$\text{H}_2 + \text{O} \begin{matrix} \rightarrow \\ \leftarrow \end{matrix} \text{OH} + \text{H}$	Step 2
3	$\text{H}_2 + \text{OH} \begin{matrix} \rightarrow \\ \leftarrow \end{matrix} \text{H}_2\text{O} + \text{H}$	Step 3
4f	$\text{H} + \text{O}_2 + \text{M} \rightarrow \text{HO}_2 + \text{M}$	Step 10 forward
5f	$\text{HO}_2 + \text{H} \rightarrow \text{OH} + \text{OH}$	Step 11 forward
6f	$\text{HO}_2 + \text{H} \rightarrow \text{H}_2 + \text{O}_2$	Step 12 forward
7f	$\text{HO}_2 + \text{OH} \rightarrow \text{H}_2\text{O} + \text{O}_2$	Step 14 forward

Extends to all equivalence ratios when direct recombination steps  $\text{H}+\text{H}+\text{M}$  and  $\text{H}+\text{OH}+\text{M}$  are added.

(Fourth shuffle reaction affects only OH/O balance.)

Burning Velocity: Dashed, 7-step; Light, detailed & 9-step; Soret excluded.



## ONE-STEP APPROXIMATION FOR LEAN DEFLAGRATIONS

( $2\text{H}_2 + \text{O}_2 \rightarrow 2\text{H}_2\text{O}$ ; Steady states for H, O, OH and  $\text{HO}_2$ )

Rate is:

$$\omega_{4f} = \frac{1}{G} \left( \frac{k_{1f}}{k_{4f} c_M} \frac{F + G}{\gamma_6 F + G} - 1 \right) \frac{k_{2f} k_{3f}}{k_{1b}} c_{\text{H}_2}^2,$$

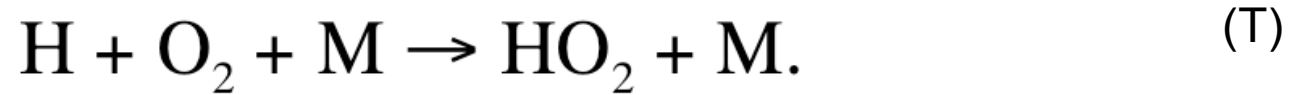
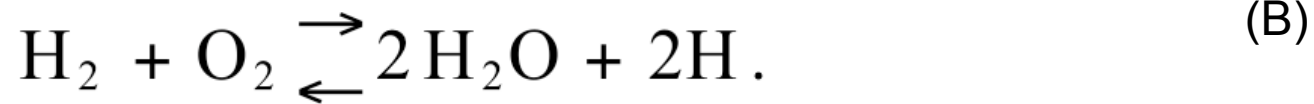
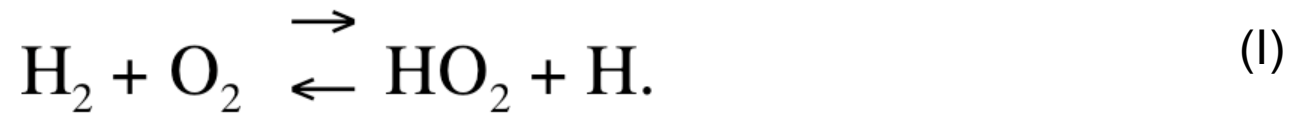
where

$$F = \frac{k_{5f} + k_{6f}}{k_{7f}} \frac{k_{3f}}{k_{4f} c_M} \frac{c_{\text{H}_2}}{c_{\text{O}_2}},$$

$$G = \frac{1 + \gamma_{3b}}{2} + \frac{F}{2} \left\{ \left[ 1 + 2(3 + \gamma_{3b})/F + (1 + \gamma_{3b})^2/F^2 \right]^{1/2} - 1 \right\}$$

$$\gamma_6 = \frac{k_{6f}}{k_{5f} + k_{6f}}, \quad \gamma_{3b} = \frac{k_{3b} c_{\text{H}_2\text{O}}}{k_{4f} c_M c_{\text{O}_2}}$$

THREE-STEP REDUCED CHEMISTRY FOR  
BOTH AUTOIGNITION AND FLAMES



## GLOBAL RATE FORMULAS

$$\omega_I = k_I [H_2][O_2] - 2(k_I/K_I)[HO_2][H] - k_H [HO_2]^2 H (T-2500) + k_D \{p/(R^\circ T) + 1.5[H_2] + 11[H_2O]\} (K_D [H_2] - [H]^2)$$

$$\omega_B = k_B [H][O_2] - (k_B/K_B)[H]^3 [H_2O]^2 / \{[H_2 + 10^{-5}p/(R^\circ T)]^3 + (k_I/K_I)[HO_2][H] + k_H [HO_2]^2 H (T-2500)\}$$

$$\omega_T = k_T \{p/(R^\circ T) + 1.5[H_2] + 15[H_2O]\} [H][O_2] - k_H [HO_2]^2 H (T-2500) + k_D \{p/(R^\circ T) + 1.5[H_2] + 11[H_2O]\} ([H]^2 - K_D [H_2])$$

Term	A <sup>a</sup>	n <sup>a</sup>	C <sup>a</sup>	B <sup>b</sup>	D <sup>b</sup>
B	3.52 × 10 <sup>16</sup>	-0.7	8,600	1.6	-6,000
D	2.00 × 10 <sup>15</sup>	-1.0	0.0	0.052	52,500
I	1.40 × 10 <sup>14</sup>	0.0	30,000	1.5	29,600
H	2.00 × 10 <sup>12</sup>	0.0	0.0		
T	5.75 × 10 <sup>19</sup>	-1.4	0.0		

<sup>a</sup> Specific reaction-rate constant  $k = AT^n e^{-C/T}$ ; units mol/cm<sup>3</sup>, s<sup>-1</sup>, K.

<sup>b</sup> Equilibrium constant  $K = Be^{-D/T}$ ; units mol/cm<sup>3</sup>, K.

# CONCLUSIONS

The four-step global reduced mechanism is accurate for flames.

A two-step reduced mechanism is good for autoignition.

A one-step reduced mechanism is good for lean deflagrations.

A three-step reduced mechanism applies to both autoignition and flames.

In flames,  $\text{HO}_2$  maintains an excellent steady state, but it is a product in high-temperature, low pressure autoignition.

Steady-state approximations usually are better for O and OH than for H.

The 21-step detailed mechanism can be used in many applications.

Since there are at most 6 global steps, applications requiring reduction can best focus in 4-step or, if necessary, 2-step mechanisms.